

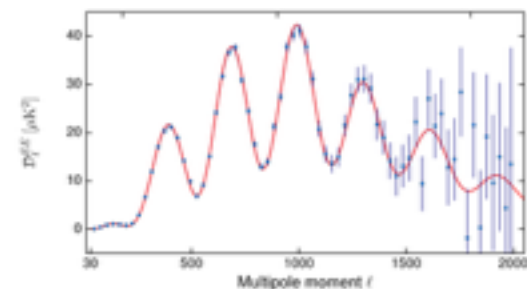
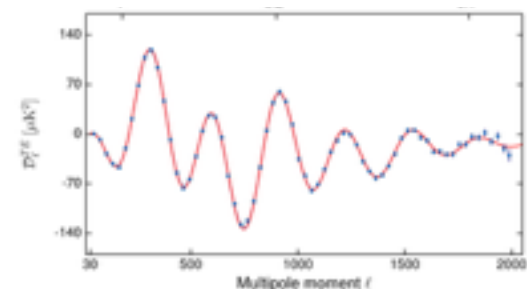
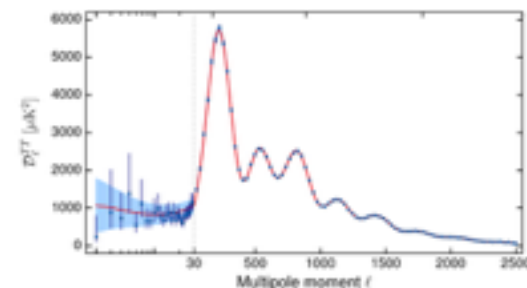
CMB

Angular Power Spectra and their Likelihoods: in Theory and in (Planck) Practice

E. Hivon & S. Galli

Planck likelihood: A hybrid approach

- Low- ℓ ($\ell < 30$):
 - TT: Pixel-based approach based on $N_{\text{side}}=16$ Commander component separated map, 92% sky, **all Planck frequencies used+WMAP+Haslam**
 - TE and EE: Pixel based approach based on **Planck LFI 70GHz** map, 46% of the sky. 30 GHz and 353GHz used for foreground cleaning.
- High- ℓ ($30 < \ell < 2500$):
 - TT: Gaussian likelihood based on **HFI 100, 143, 217GHz** at (70, 60, 50% sky)
 - TE, EE: Gaussian likelihood, **HFI 100, 143, 217GHz** at (70, 50, 40% sky).



Planck 2015 results

XI. CMB power spectra, likelihoods, and robustness of parameters

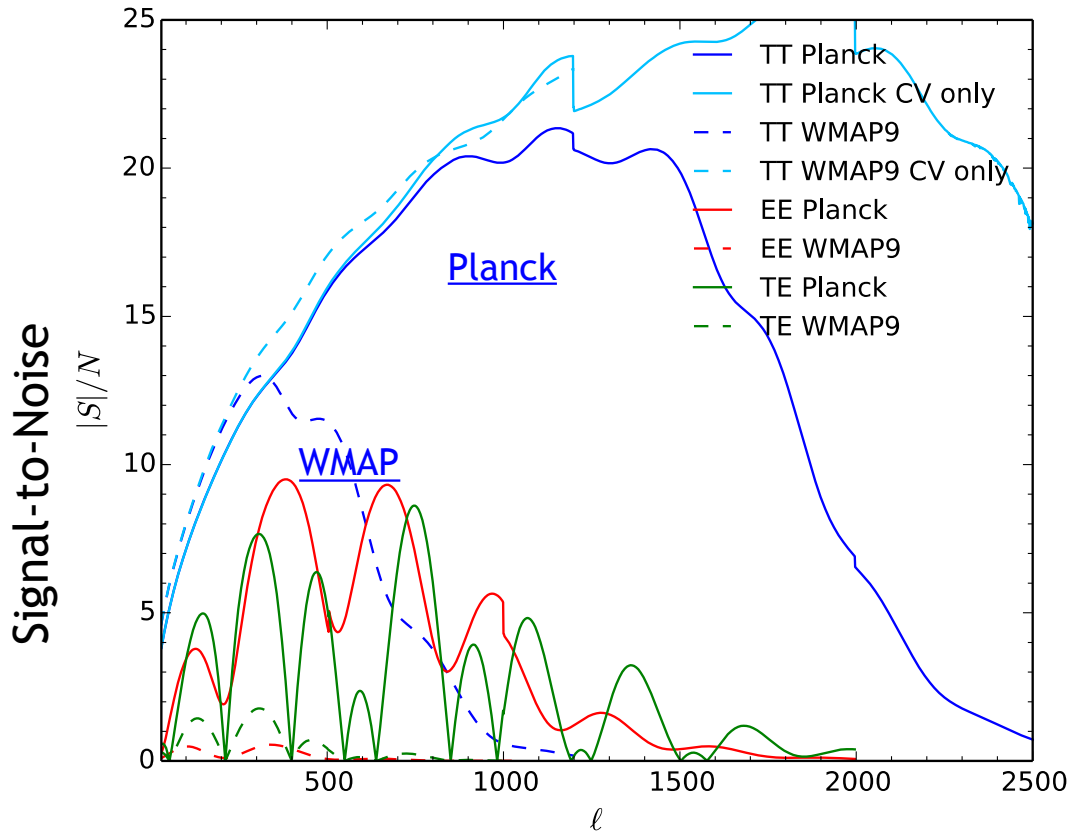
Planck Collaboration: N. Aghanim⁶³, M. Arnaud⁷⁸, M. Ashdown^{74,6}, J. Aumont⁶³, C. Baccigalupi⁹¹, A. J. Banday^{103,10}, R. B. Barreiro⁶⁹, J. G. Bartlett^{1,71}, N. Bartolo^{32,70}, E. Battaneo^{105,106}, K. Benabed^{64,102}, A. Benoît⁶¹, A. Benoit-Lévy^{24,64,102}, J.-P. Bernard^{103,10}, M. Bersanelli^{35,51}, P. Bielewicz^{86,10,91}, J. J. Bock^{71,12}, A. Bonaldi⁷², L. Bonavera²⁰, J. R. Bond⁹, J. Borrill^{15,96}, F. R. Bouchet^{64,94,*}, F. Boulanger⁶³, M. Bucher¹, C. Burigana^{50,33,52}, R. C. Butler⁵⁹, E. Calabrese³⁹, J.-F. Cardoso^{79,1,64}, A. Catalano^{80,77}, A. Challinor^{66,74,13}, H. C. Chiang^{28,7}, P. R. Christensen^{87,38}, D. L. Clements²⁹, L. P. L. Colombo^{23,71}, C. Combet⁸⁰, A. Coulais⁷⁷, B. P. Crill^{71,12}, A. Curto^{69,6,74}, F. Cuttaia⁵⁰, L. Danese⁹¹, R. D. Davies⁷², R. J. Davis⁷², P. de Bernardis³⁴, A. de Rosa⁵⁰, G. de Zotti^{47,91}, J. Delabrouille¹, F.-X. Désert⁵⁷, E. Di Valentino^{64,94}, C. Dickinson⁷², J. M. Diego⁶⁹, K. Dolag^{104,84}, H. Dole^{63,62}, S. Donzelli⁵¹, O. Doré^{71,12}, M. Douspis⁶³, A. Ducour^{64,59}, J. Dunkley⁹⁸, X. Dupac⁴⁰, G. Efstathiou⁶⁶, F. Elsner^{24,64,102}, T. A. Enßlin⁸⁴, H. K. Eriksen⁶⁷, J. Fergusson¹³, F. Finelli^{30,52}, O. Fornì^{103,10}, M. Frailis⁴⁹, A. A. Fraisse²⁸, E. Franceschi⁵⁰, A. Frejsel⁸⁷, S. Galeotta⁴⁹, S. Galli⁷³, K. Gangui¹, C. Gauthier^{1,83}, M. Gerbino^{100,89,34}, M. Giard^{103,10}, E. Gjerløw⁶⁷, J. González-Nuevo^{20,69}, K. M. Górski^{71,107}, S. Gratton^{74,66}, A. Gregorio^{36,49,56}, A. Gruppuso^{50,52}, J. E. Gudmundsson^{100,89,28}, J. Hamann^{101,99}, F. K. Hansen⁶⁷, D. L. Harrison^{66,74}, G. Helou¹², S. Henrot-Versillé⁷⁶, C. Hernández-Monteagudo^{14,84}, D. Herranz⁶⁹, S. R. Hildebrandt^{71,12}, E. Hivon^{64,102}, W. A. Holmes⁷¹, A. Hornstrup¹⁷, K. M. Huffenberger²⁶, G. Hurier⁶³, A. H. Jaffe⁵⁹, W. C. Jones²⁸, M. Juvela²⁷, E. Keihänen²⁷, R. Keskitalo¹⁵, K. Kiiveri^{27,45}, J. Knoche⁸⁴, L. Knox²⁹, M. Kunz^{18,63,3}, H. Kurki-Suonio^{27,45}, G. Lagache^{5,43}, A. Lähteenmäki^{2,45}, J.-M. Lamarre⁷⁷, A. Lasenby^{6,74}, M. Lattanzi^{33,53}, C. R. Lawrence⁷¹, M. Le Jeune¹, R. Leonardi⁸, J. Lesgourgues^{65,101}, F. Levrier⁷⁷, A. Lewis²⁵, M. Liguori^{32,70}, P. B. Lilje⁶⁷, M. Lilley^{64,94}, M. Linden-Vørnle¹⁷, V. Lindholm^{27,45}, M. López-Caniço⁴⁹, J. F. Macías-Pérez⁸⁰, B. Maffei⁷², G. Maggio⁴⁹, D. Maino^{35,51}, N. Mandolesi^{50,33}, A. Mangilli^{63,76}, M. Maris⁴⁹, P. G. Martin⁹, E. Martínez-González⁶⁹, S. Masi³⁴, S. Matarrese^{32,70,42}, P. R. Meinhold³⁰, A. Melchiorri^{34,54}, M. Migliaccio^{66,74}, M. Millea²⁹, S. Mitra^{58,71}, M.-A. Miville-Deschênes^{63,9}, A. Moneti⁶⁴, L. Montier^{103,10}, G. Morgante⁵⁰, D. Mortlock⁵⁹, S. Mottet^{64,94}, D. Munshi⁹³, J. A. Murphy⁸⁵, A. Narimani²², P. Naselsky^{88,39}, F. Nati²⁸, P. Natoli^{133,4,53}, F. Noviello⁷², D. Novikov⁸², I. Novikov^{87,82}, C. A. Oxborrow¹⁷, F. Paci⁹¹, L. Pagano^{34,54}, F. Pajot⁶³, D. Paoletti^{50,52}, B. Partridge⁴⁴, F. Pasian⁴⁹, G. Patanchon¹, T. J. Pearson^{152,60}, O. Perdereau⁷⁶, L. Perotto⁸⁰, V. Pettorino⁴³, F. Piacentini³⁴, M. Piat¹, E. Pierpaoli²³, D. Pietrobon⁷¹, S. Plaszczynski⁷⁶, E. Pointecouteau^{103,10}, G. Polenta^{4,48}, N. Ponthieu^{63,57}, G. W. Pratt⁷⁸, S. Prunet^{64,102}, J.-L. Puger⁶³, J. P. Rachen^{21,84}, M. Reinecke⁸⁴, M. Remazeilles^{72,63,1}, C. Renault⁸⁰, A. Renzi^{37,35}, I. Ristorcelli^{103,10}, G. Rocha^{71,12}, M. Rossetti^{35,51}, G. Roudier^{1,77,71}, B. Rouillé d'Orfeuill⁷⁶, J. A. Rubiño-Martín^{68,19}, B. Rusholme⁶⁰, L. Salvati³⁴, M. Sandri³⁰, D. Santos⁸⁰, M. Savelainen^{27,45}, G. Savini⁹⁰, D. Scott²², P. Serra⁶³, L. D. Spencer⁹³, M. Spinelli⁷⁶, V. Stolyarov^{6,97,75}, R. Stompor¹, R. Sunyaev^{84,95}, D. Sutton^{66,74}, A.-S. Suur-Uuski^{27,45}, J.-F. Sygnet⁶⁴, J. A. Tauber⁴¹, L. Terenzi^{192,50}, L. Toffolatti^{20,69,50}, M. Tomasi^{35,51}, M. Tristram⁷⁶, T. Trombetti^{50,33}, M. Tucci¹⁸, J. Tuovinen¹¹, G. Umata⁴⁶, L. Valenziano⁵⁰, J. Valiviita^{27,45}, F. Van Tent⁸¹, P. Vielva⁶⁹, F. Villa⁵⁰, L. A. Wade⁷¹, B. D. Wandelt^{64,102,31}, I. K. Wehus^{71,67}, D. Yvon¹⁶, A. Zacchei⁴⁹, and A. Zonca³⁰

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- CI theory is simple, applying it to real data takes a lot of work
- Planck 2015 likelihood paper 99 pages, ~200 co-authors

Signal to noise



Planck sample variance limited till $l \sim 1600$ (data points till ~ 2500 , fsky $\sim 40-70\%$)

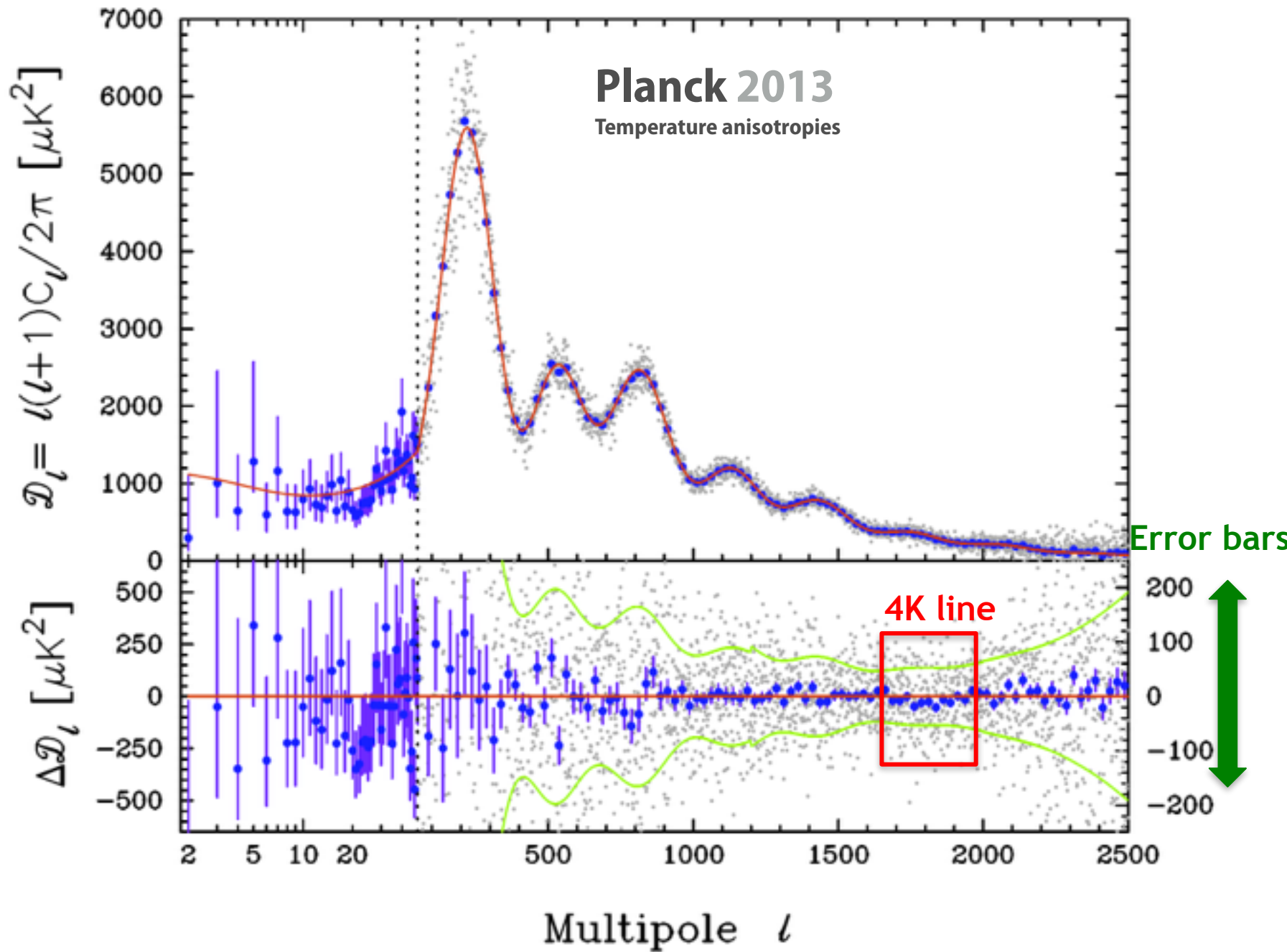
WMAP sample variance limited till $l \sim 600$ (data points till $l \sim 1200$)

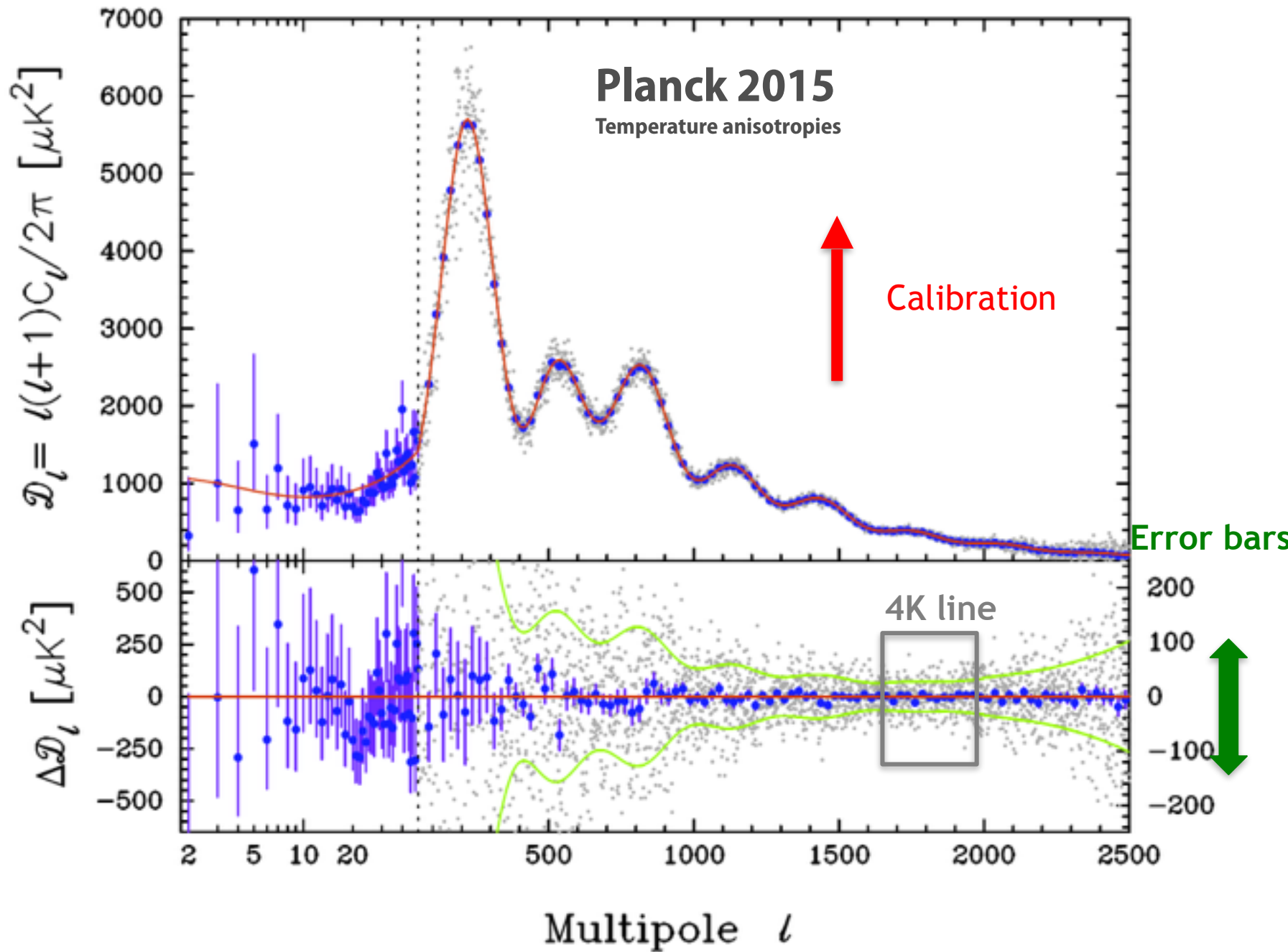
ACT and SPT use $< 5\%$ of the sky.

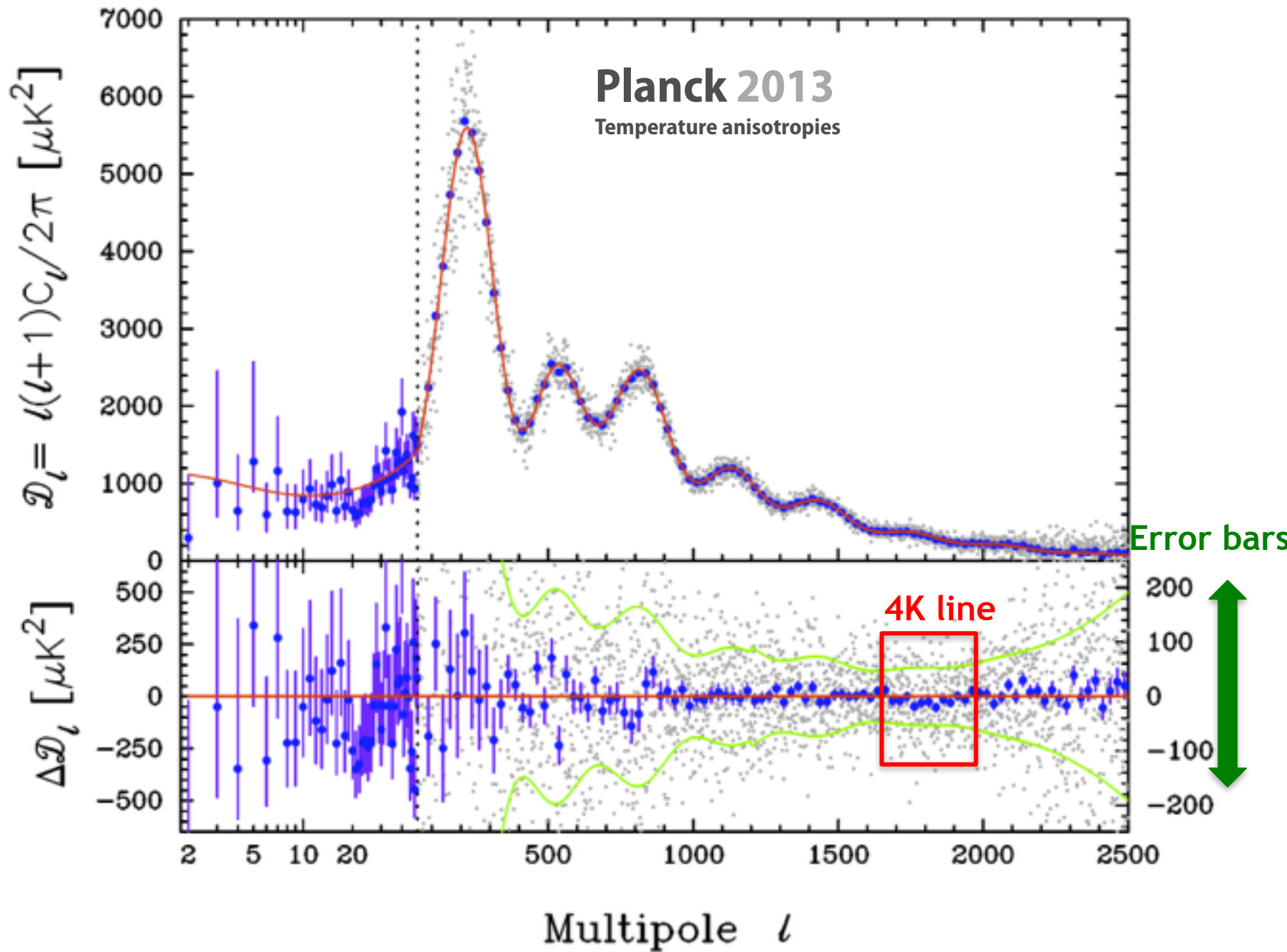
Error bar due to sample variance ~ 3 times larger than Planck at $l < 1500$!

From 2013 to 2015 data analysis

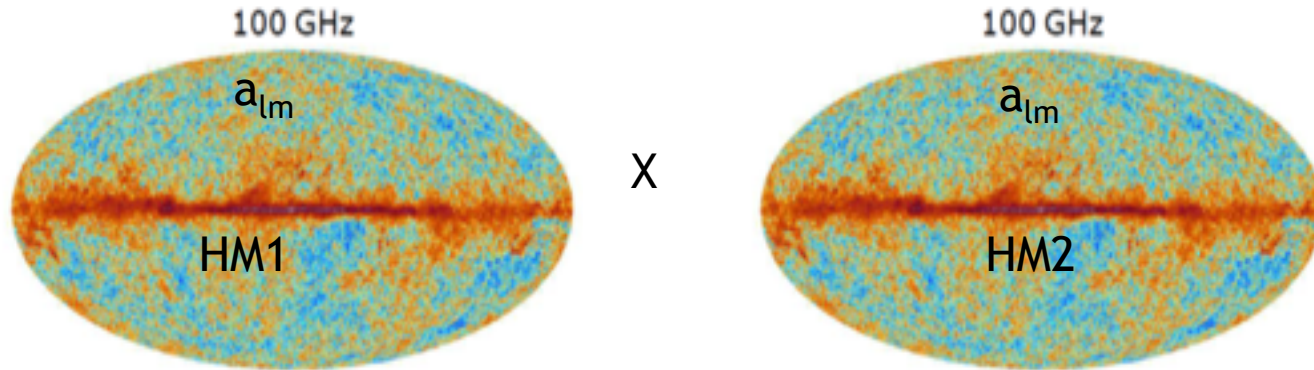
- Know your instrument
 - ▶ recalibration
 - ▶ 10x better beam knowledge
- Thou shalt commit (some) data alteration
 - ▶ remove “4K-cooler lines” from data
- Thou shalt covet more data
 - ▶ Polarisation !
 - ▶ Going from half-mission to full mission is good
 - ▶ Less correlated data splits are available







Datasets for the high- ℓ likelihood



- 100, 143, 217GHz (best HFI channels for CMB).
353 and 545 to estimate dust templates.
- Frequency maps from weighted average of all detectors at that frequency.
Maps for each of the two temporal halves \sim 15 months of the total mission.
- Spectra only calculated correlating maps from two different half missions. Avoids noise bias, avoids correlating co-temporal systematics across detectors.

Planck 2015

• Data: $\hat{\mathbf{C}} = (\hat{\mathbf{C}}^{TT}, \hat{\mathbf{C}}^{EE}, \hat{\mathbf{C}}^{TE})$

$$\hat{\mathbf{C}}^{TT} = (\hat{\mathbf{C}}_{100 \times 100}^{TT}, \hat{\mathbf{C}}_{143 \times 143}^{TT}, \hat{\mathbf{C}}_{143 \times 217}^{TT}, \hat{\mathbf{C}}_{217 \times 217}^{TT})$$

$$\hat{\mathbf{C}}^{EE} = (\hat{\mathbf{C}}_{100 \times 100}^{EE}, \hat{\mathbf{C}}_{100 \times 143}^{EE}, \hat{\mathbf{C}}_{100 \times 217}^{EE}, \hat{\mathbf{C}}_{143 \times 143}^{EE}, \hat{\mathbf{C}}_{143 \times 217}^{EE}, \hat{\mathbf{C}}_{217 \times 217}^{EE})$$

$$\hat{\mathbf{C}}^{TE} = (\hat{\mathbf{C}}_{100 \times 100}^{TE}, \hat{\mathbf{C}}_{100 \times 143}^{TE}, \hat{\mathbf{C}}_{100 \times 217}^{TE}, \hat{\mathbf{C}}_{143 \times 143}^{TE}, \hat{\mathbf{C}}_{143 \times 217}^{TE}, \hat{\mathbf{C}}_{217 \times 217}^{TE}).$$

$$-\ln \mathcal{L}(\hat{\mathbf{C}} | \mathbf{C}(\{\Omega\})) = \frac{1}{2} [\hat{\mathbf{C}} - \mathbf{C}(\{\Omega\})]^T \mathbf{M}^{-1} [\hat{\mathbf{C}} - \mathbf{C}(\{\Omega\})] + \text{const.}$$

Planck 2015

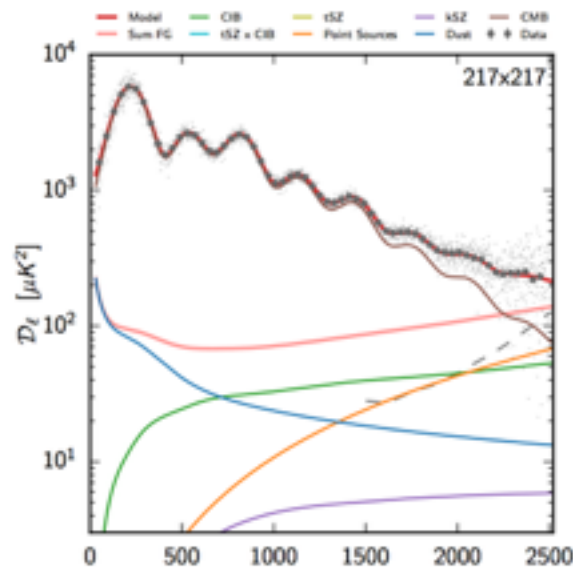
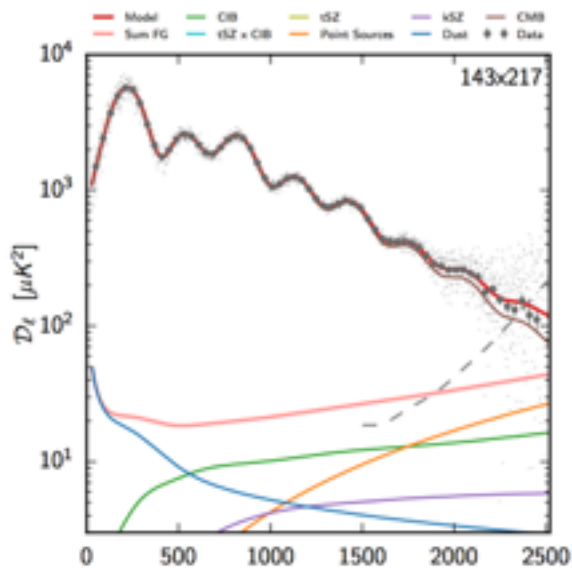
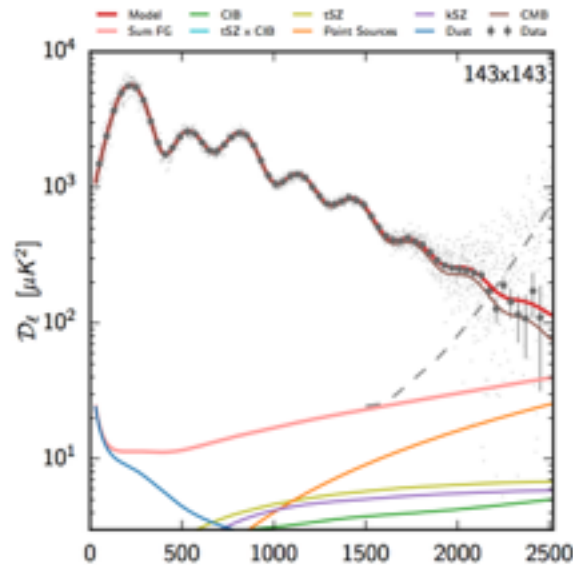
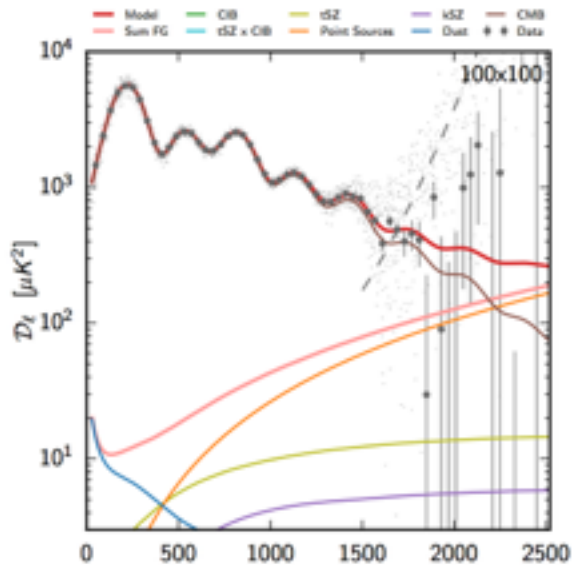
- Covariance matrix:

$$\mathbf{C} = \begin{pmatrix} C^{TTTT} & C^{TTEE} & C^{TTTE} \\ C^{EETT} & C^{EEEE} & C^{EETE} \\ C^{TETT} & C^{TEEE} & C^{TETE} \end{pmatrix}$$

$$C^{TTTT} = \begin{pmatrix} (100 \times 100) \times (100 \times 100) & (100 \times 100) \times (143 \times 143) & (100 \times 100) \times (217 \times 217) & (100 \times 100) \times (143 \times 217) \\ (143 \times 143) \times (100 \times 100) & (143 \times 143) \times (143 \times 143) & (143 \times 143) \times (217 \times 217) & (143 \times 143) \times (143 \times 217) \\ (217 \times 217) \times (100 \times 100) & (217 \times 217) \times (143 \times 143) & (217 \times 217) \times (217 \times 217) & (217 \times 217) \times (143 \times 217) \\ (143 \times 217) \times (100 \times 100) & (143 \times 217) \times (143 \times 143) & (143 \times 217) \times (217 \times 217) & (143 \times 217) \times (143 \times 217) \end{pmatrix}$$

Unbinned, this is a ~23000x23000 matrix!

Foreground model



- We mask regions of the sky most contaminated by dust, CO and extragalactic point sources. We retain 66, 57, 47% at 100, 143, 217GHz.
- We model the **foregrounds** in the remaining sky at the power spectrum level.
 - Galactic dust
 - Unresolved Point sources
 - Clustered CIB-cosmic infrared background
 - Thermal and Kinetic Sunyaev-Zeldovich from galaxy clusters
 - Cross-correlation between tSZxCIB

Foregrounds

- Dust

- ◆ TT: use 545GHz C_ℓ modelled (via difference of masks) as dust + CIB + PS
 - TE and EE: use 353GHz instead

- ◆ Subtract $A_{\nu 1\nu 2} C_\ell^{\text{DUST}}$ (n) template from all cross-spectra, with a free amplitude, and free spectral slope, which are marginalised over

- Unresolved Point sources

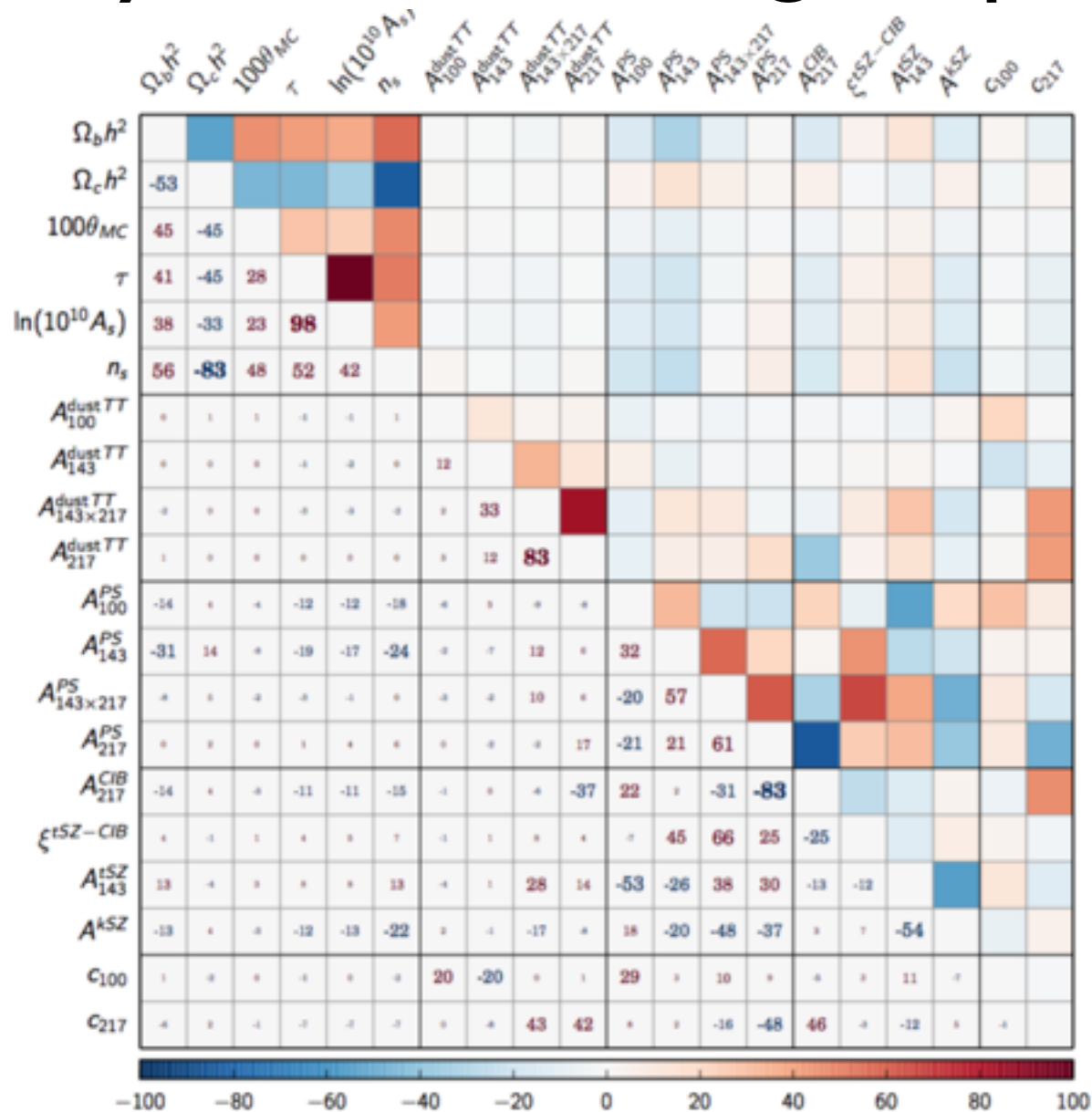
- ◆ TT only: flat spectrum fit on C_ℓ

Table 10. Parameters used for astrophysical foregrounds and instrumental modelling.

Parameter	Prior range	Definition
A_{100}^{CIB}	[0, 400]	Contribution of Poisson point-source power to D_{100}^{CIB} for Planck (in μK^2)
A_{143}^{CIB}	[0, 400]	As for A_{100}^{CIB} but at 143 GHz
A_{217}^{CIB}	[0, 400]	As for A_{100}^{CIB} but at 217 GHz
$A_{143 \times 217}^{\text{CIB}}$	[0, 400]	As for A_{100}^{CIB} but at 143 \times 217 GHz
A_{217}^{CIB}	[0, 200]	Contribution of CIB power to D_{217}^{CIB} at the Planck CMB frequency for 217 GHz (in μK^2)
A_{100}^{ISZ}	[0, 10]	Contribution of ISZ to D_{100}^{ISZ} at 143 GHz (in μK^2)
A_{143}^{ISZ}	[0, 10]	Contribution of ISZ to D_{143} (in μK^2)
$\rho^{\text{CIB-ISZ}}$	[0, 1]	Correlation coefficient between the CIB and ISZ
A_{200}^{Gal}	[0, 50]	Amplitude of Galactic dust power at $\ell = 200$ at 100GHz (in μK^2)
	(7 \pm 2)	
A_{143}^{Gal}	[0, 50]	As for A_{200}^{Gal} but at 143 GHz
	(9 \pm 2)	
$A_{143 \times 217}^{\text{Gal}}$	[0, 100]	As for A_{200}^{Gal} but at 143 \times 217 GHz
	(21 \pm 8.5)	
A_{217}^{Gal}	[0, 400]	As for A_{200}^{Gal} but at 217 GHz
	(80 \pm 20)	
C_{100}	[0, 3]	Power spectrum calibration for the 100 GHz
	(0.9990004 \pm 0.001)	
C_{217}	[0, 3]	Power spectrum calibration for the 217 GHz
	(0.99501 \pm 0.002)	
B_{flat}	[0.9, 1.1]	Absolute map calibration for Planck
	(1 \pm 0.0025)	
A_{500}^{Gal}	[0, 10]	Amplitude of Galactic dust power at $\ell = 500$ at 100GHz (in μK^2)
	(0.06 \pm 0.012)	
$A_{100 \times 143}^{\text{Gal}}$	[0, 10]	As for A_{500}^{Gal} but at 100 \times 143 GHz
	(0.05 \pm 0.015)	
$A_{100 \times 217}^{\text{Gal}}$	[0, 10]	As for A_{500}^{Gal} but at 100 \times 217 GHz
	(0.11 \pm 0.033)	
A_{143}^{Gal}	[0, 10]	As for A_{500}^{Gal} but at 143 GHz
	(0.1 \pm 0.02)	
$A_{143 \times 217}^{\text{Gal}}$	[0, 10]	As for A_{500}^{Gal} but at 143 \times 217 GHz
	(0.24 \pm 0.048)	
A_{217}^{Gal}	[0, 10]	As for A_{500}^{Gal} but at 217 GHz
	(0.72 \pm 0.14)	
A_{500}^{Gal}	[0, 10]	Amplitude of Galactic dust power at $\ell = 500$ at 100GHz (in μK^2)
	(0.14 \pm 0.042)	
$A_{100 \times 143}^{\text{Gal}}$	[0, 10]	As for A_{500}^{Gal} but at 100 \times 143 GHz
	(0.12 \pm 0.036)	
$A_{100 \times 217}^{\text{Gal}}$	[0, 10]	As for A_{500}^{Gal} but at 100 \times 217 GHz
	(0.3 \pm 0.09)	
A_{143}^{Gal}	[0, 10]	As for A_{500}^{Gal} but at 143 GHz
	(0.24 \pm 0.072)	
$A_{143 \times 217}^{\text{Gal}}$	[0, 10]	As for A_{500}^{Gal} but at 143 \times 217 GHz
	(0.6 \pm 0.18)	
A_{217}^{Gal}	[0, 10]	As for A_{500}^{Gal} but at 217 GHz
	(3.8 \pm 0.54)	

Notes. The columns indicate the symbol for each parameter, the prior used for exploration (square brackets denote uniform priors, parentheses indicate Gaussian priors), and definitions. Beam eigenmode amplitudes require a correlation matrix to fully describe their joint prior and so do not appear in the table; they are internally marginalized over rather than explicitly sampled. This table only lists the instrumental parameters that are explored in the released version, but we do consider more parameters to assess the effects of beam uncertainties and beam leakage; see Sect. 3.4.3.

Many non-cosmological parameters



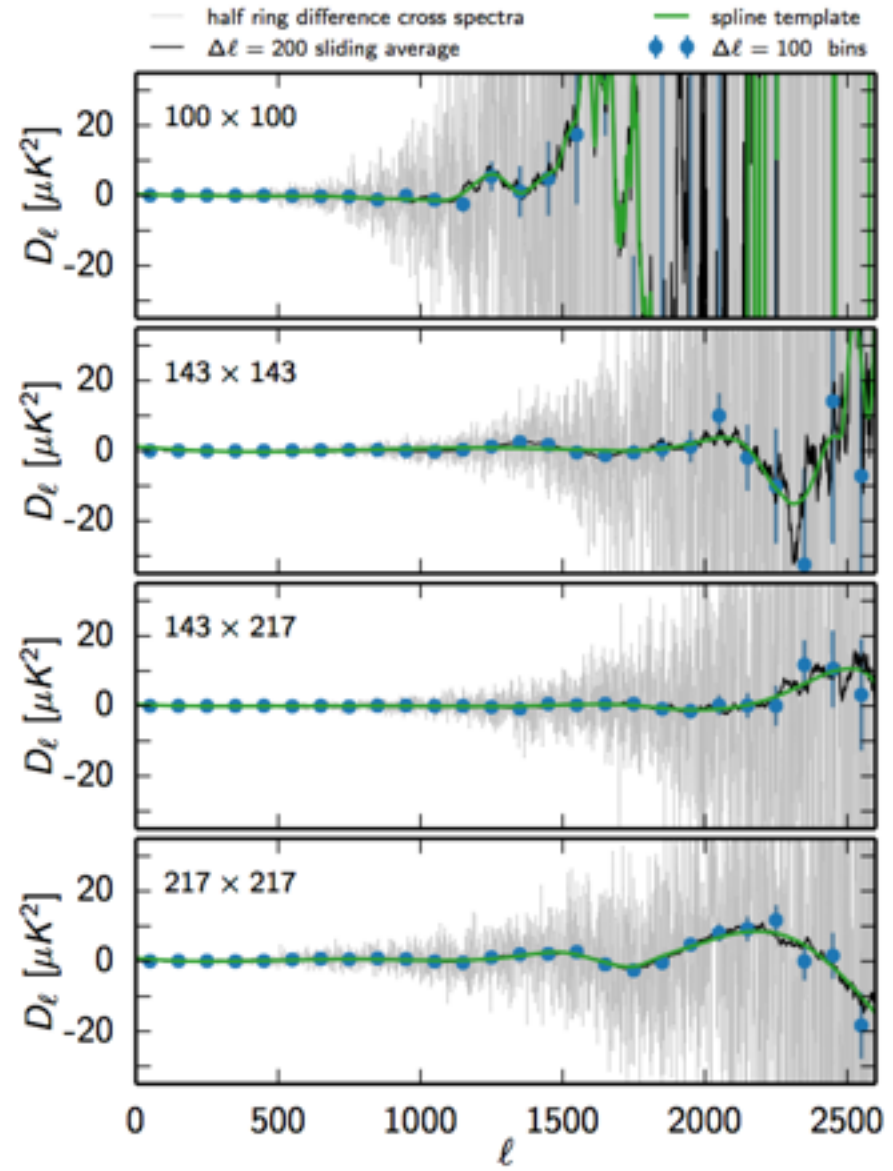
Correlated noise seen in detector sets (simultaneous observations)

used in 2013 analysis

Half-ring maps of detsets: $(\text{HRI-HR2})_{\text{DS1}} \times (\text{HRI-HR2})_{\text{DS2}}$

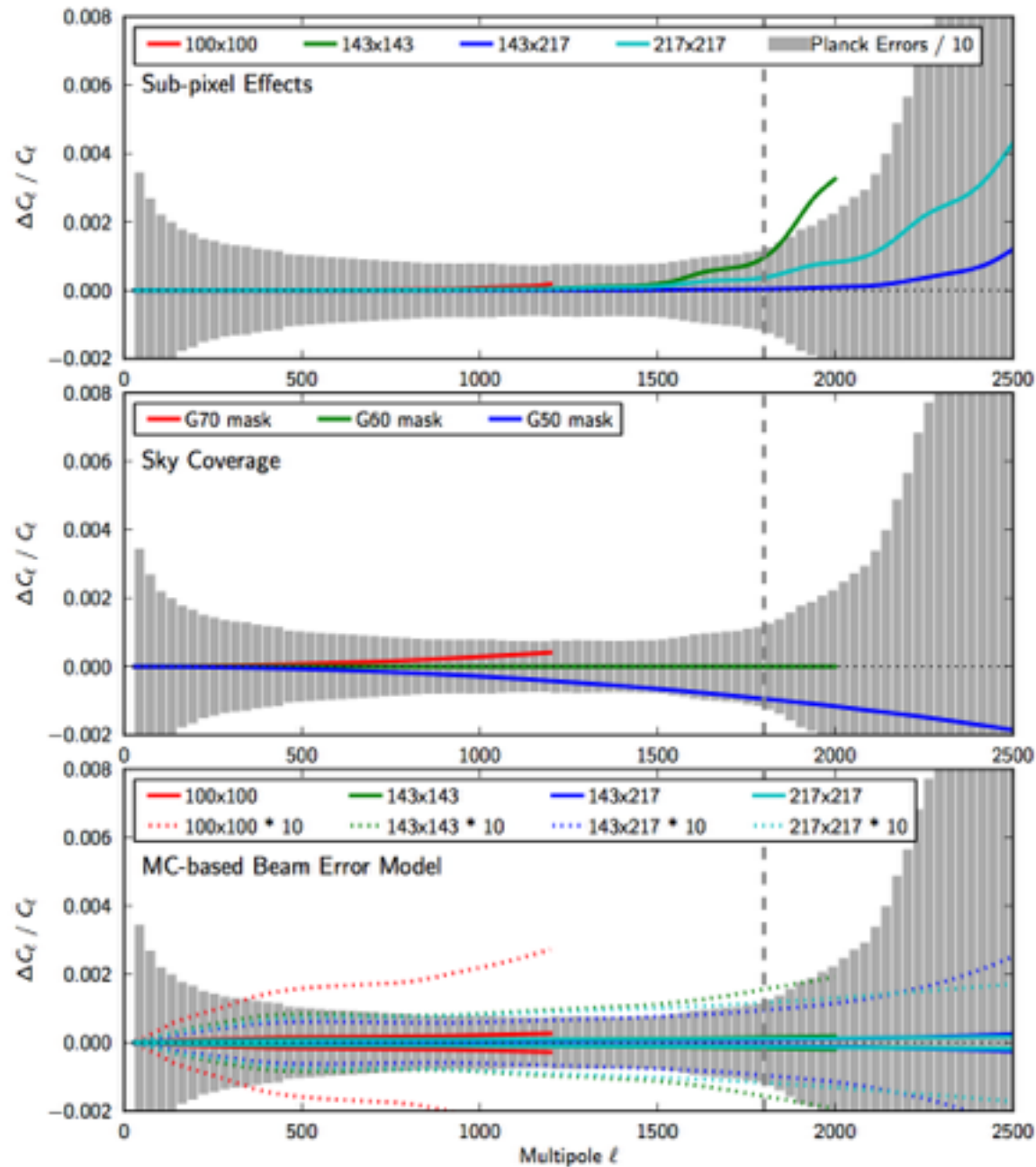
provide a correlated noise template added to cosmological analysis

No correlation seen in Half-Mission used in 2015, but deviation from white noise included in S+N covariance matrix calculation

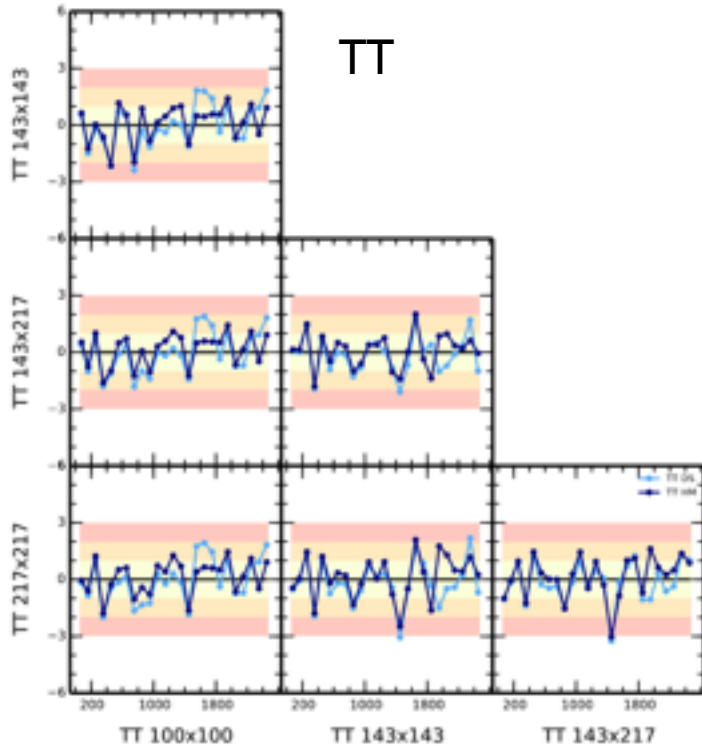


Systematics

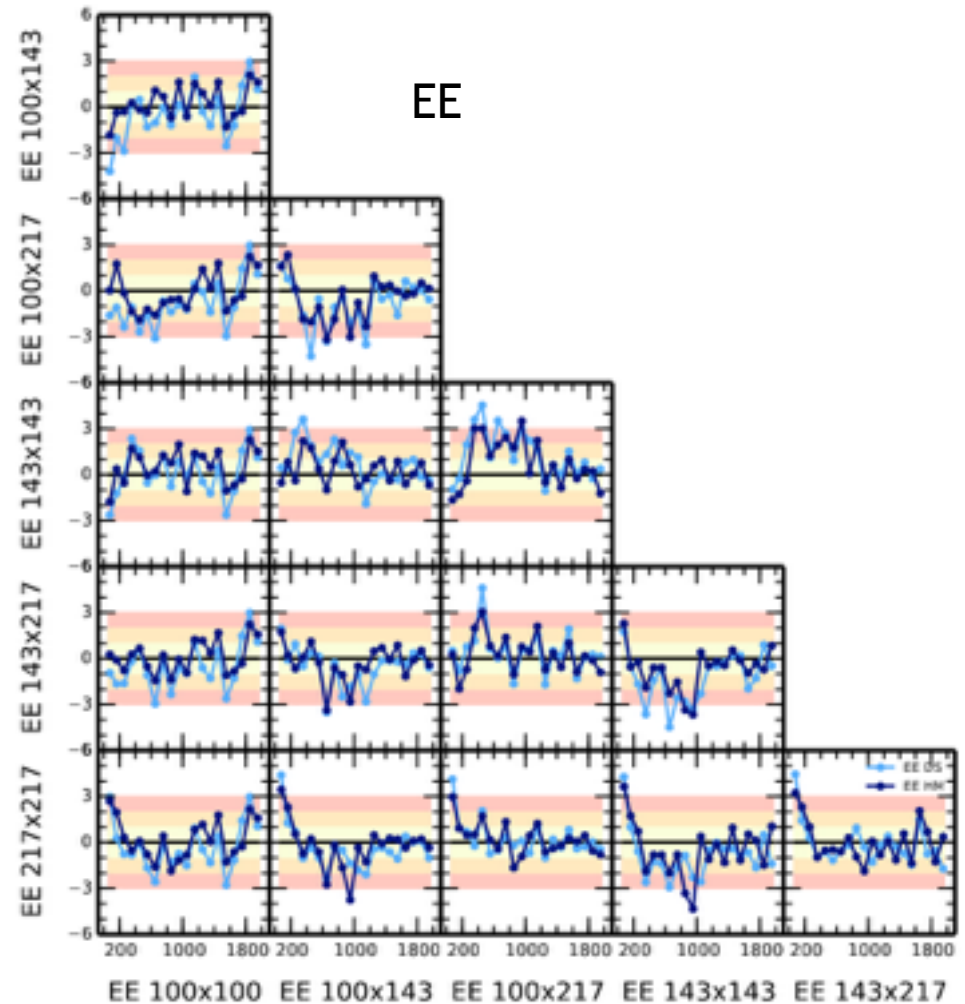
- Comparison of some systematics with statistical errors



Inter-frequency differences



TT behaves very well

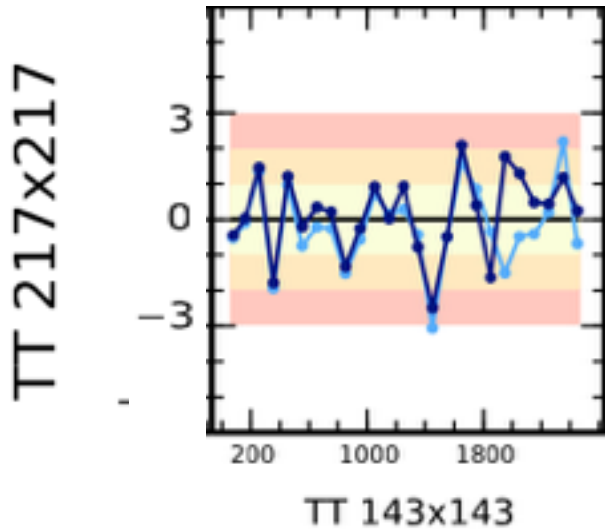


TE and EE too large deviations. A sign of remaining systematics.

Frequency redundancy allows us to check foregrounds cleaning and systematics.

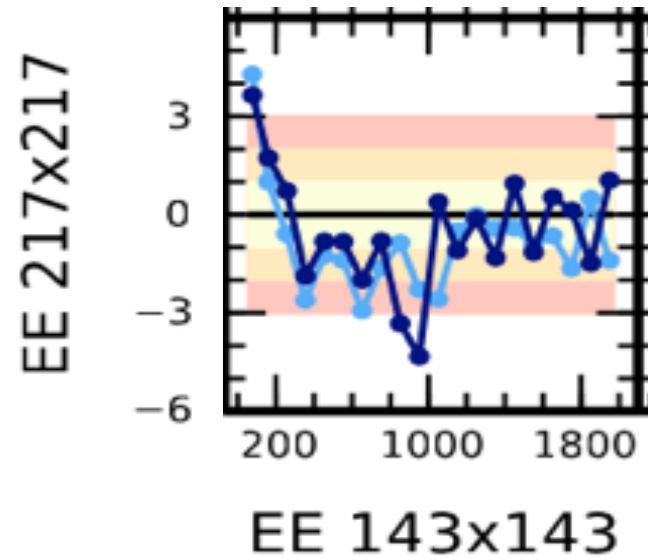
Inter-frequency differences

TT



TT behaves very well

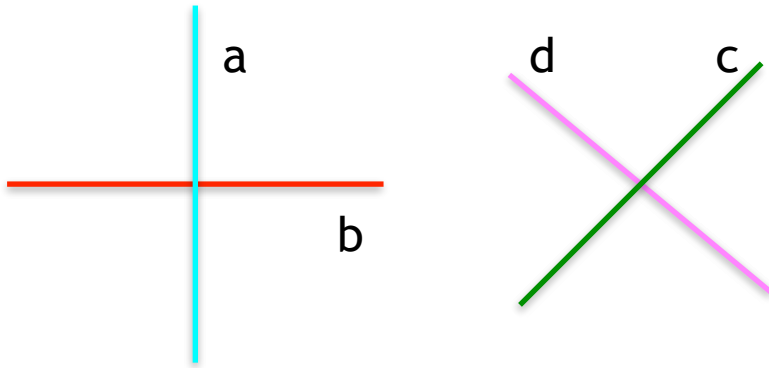
EE



TE and EE too large deviations. A sign of remaining systematics.

Frequency redundancy allows us to check foregrounds cleaning and systematics.

Beam related systematics



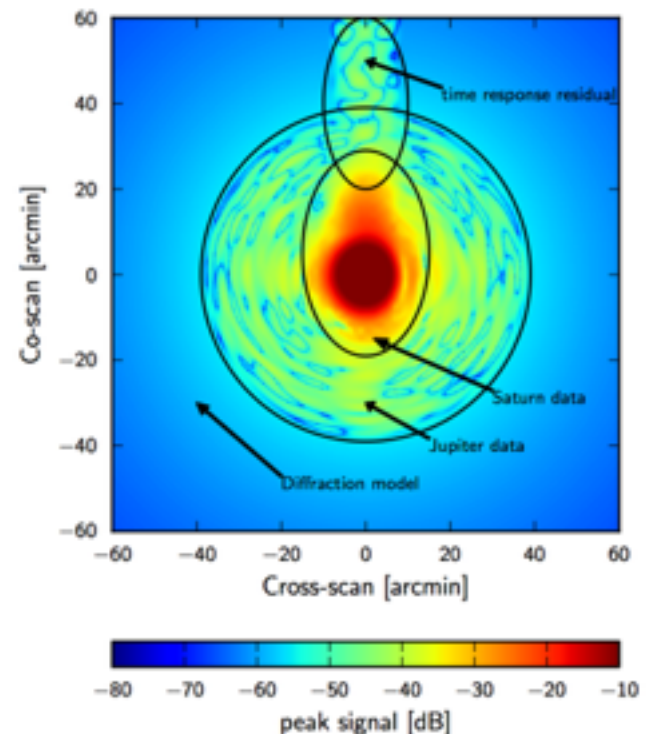
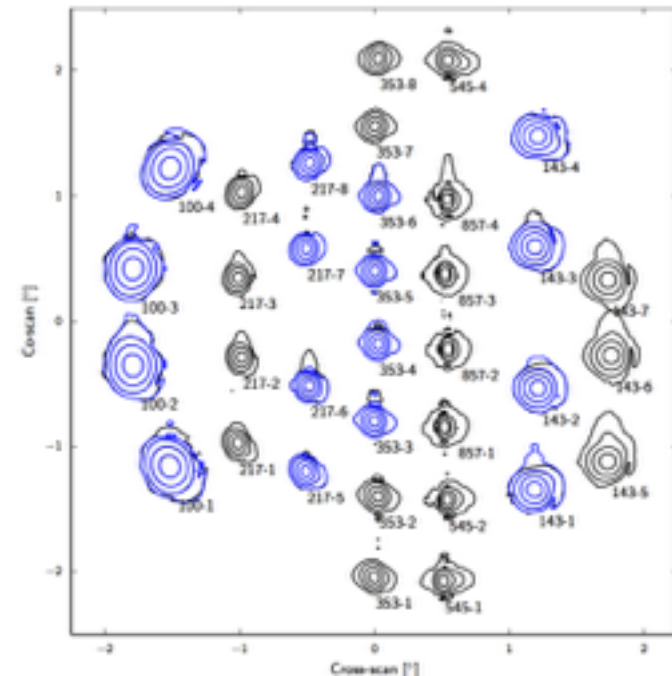
$$I = \langle E_x^2 \rangle + \langle E_y^2 \rangle = \langle E_{45}^2 \rangle + \langle E_{-45}^2 \rangle$$

$$Q = \langle E_x^2 \rangle - \langle E_y^2 \rangle = I_a - I_b$$

$$U = 2\langle E_x E_y \rangle = \langle E_{45}^2 \rangle - \langle E_{-45}^2 \rangle = I_c - I_d$$

- In the absence of polarisation modulation (eg rotating half-wave plate, rHWP*), polarisation is obtained by differencing 2 different orthogonal detectors
 → any detector mismatch (in gains, beams, band-passes, ...) creates fake polarisation ([Hu et al, 2003](#), and many others).

Note: *rHWP are still little used, and create their own kind of problems ([Takakura et al, 2017](#))



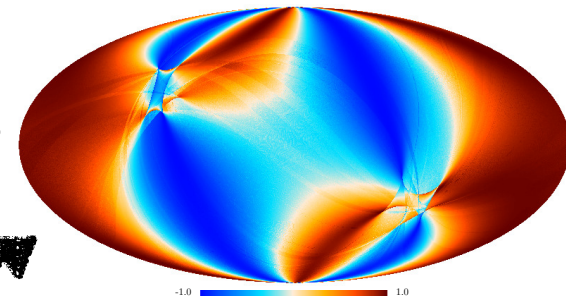
QuickPol

- Temperature QuickBeam (used in 2013 and 2015 analyses):

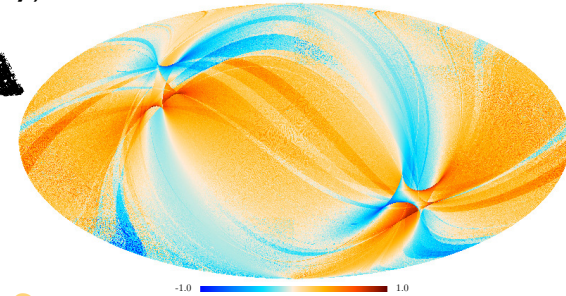
$$\diamond C'_\ell{}^{TT} = \sum_s \omega_s^2 b_{\ell s}^* b_{\ell s} C_\ell{}^{TT}$$

- ▶ $b_{\ell s}$: weighted combination of scanning beams in DetSet,
- ▶ ω_s^2 : encodes scanning strategy (assumed to vary slowly across the sky)

$\ell=2$



$\ell=1$



- Temperature + Polarisation QuickPol (in 2017 analysis):

$$\diamond C'_\ell = \sum_{sij} \Omega_{sij} \oplus B_{\ell si}^{*t} \cdot C_\ell \cdot B_{\ell sj}$$

- ▶ C : 3x3 $C(l)$ matrix
- ▶ B : weighted scanning polarised beams in DetSet or Half missions
- ▶ Ω : encodes scanning strategy weighted by map-making IQU inverse covariance matrix

Map(s) Power Spectra

Sky Power Spectra

◆ provides effective beam window matrix W_ℓ describing C_ℓ coupling, **without numerical simulations!**

◆ has been extended to gain and polar efficiency uncertainty

◆ Backward $C(l)$ fitting can then still be used as a rain check to detect/catch remaining systematics

$$\begin{pmatrix} \tilde{C}_\ell^{TT} \\ \tilde{C}_\ell^{EE} \\ \tilde{C}_\ell^{BB} \\ \tilde{C}_\ell^{TE} \\ \tilde{C}_\ell^{TB} \\ \tilde{C}_\ell^{EB} \\ \tilde{C}_\ell^{ET} \\ \tilde{C}_\ell^{BT} \\ \tilde{C}_\ell^{BE} \end{pmatrix} = \mathbf{W}_\ell \cdot \begin{pmatrix} C_\ell^{TT} \\ C_\ell^{EE} \\ C_\ell^{BB} \\ C_\ell^{TE} \\ C_\ell^{TB} \\ C_\ell^{EB} \end{pmatrix}$$

For each ℓ , W_ℓ is a 9x6 (diagonal dominated) matrix

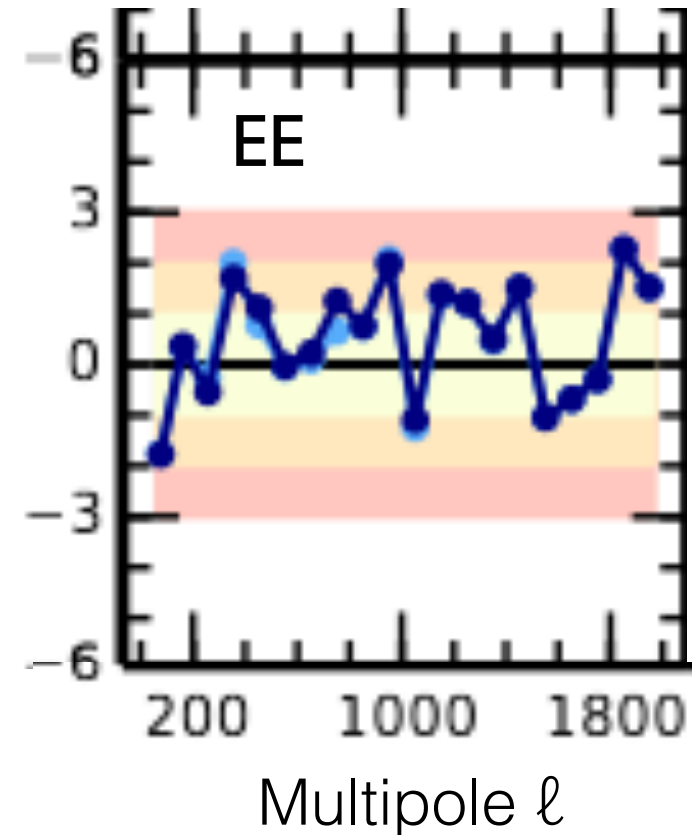
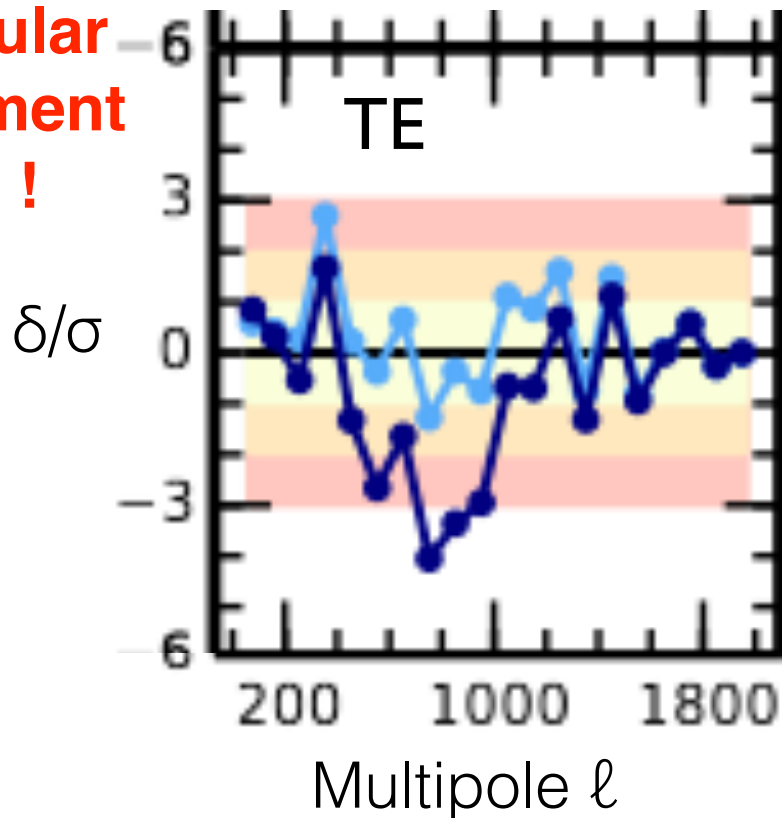
Inter-frequency consistency:
fg corrected C(l)
143x143 - 100x100

Preliminary!

Ignoring beam leakage (2015 analysis)

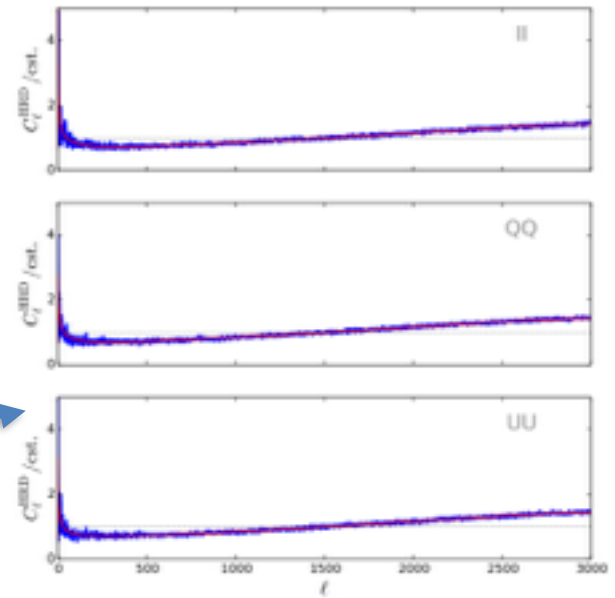
With beam leakage prediction+correction (2017-8 analysis)

**Spectacular
improvement
for TE !**



Covariance matrix

- Ingredients:
 - ▶ A fiducial CMB signal spectrum, based on your best estimate
 - ▶ Foreground fiducial models at relevant frequency, based on your best knowledge
 - ▶ A good estimate of the noise spectrum, C_l^{noise}
 - ▶ Systematics models and their uncertainty
e.g. for Gaussian beam: $B_\ell = \exp(-\ell(\sigma + \delta\sigma)^2)$



- Perform analytical calculations
- Validate with $N_{\text{sim}} = 10\,000$ Monte-Carlo simulations (see P. Natoli lecture)
 - ▶ limited accuracy $\Delta M_{ij} / M_{ij} \sim (2 / N_{\text{sim}})^{1/2} = 1\%$
 - ▶ mostly interesting for diagonal

TTT block:

$$\text{Var}(C_l^{TT}, C_l^{TT}) = \dots$$

TTTE block:

$$\text{Var}(C_l^{TT}, C_l^{TE}) = \dots$$

TTTE block:

$$\text{Var}(C_l^{TT}, C_l^{TE}) = \dots$$

TTTE block:

$$\text{Var}(C_l^{TT}, C_l^{TE}) = \dots$$

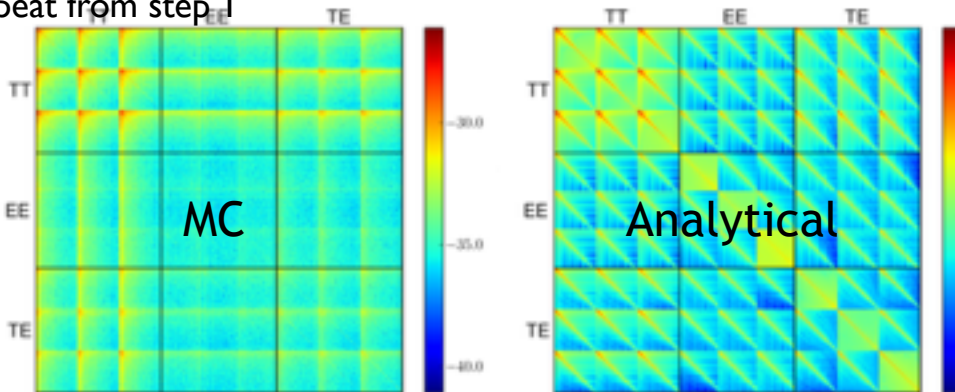
TTTE block:

$$\text{Var}(C_l^{TT}, C_l^{TE}) = \dots$$

In Fig. (C.3)-(C.7), we have introduced the projector functions \mathcal{P}_{TT} , \mathcal{P}_{EE} , and \mathcal{P}_{TE} to describe the coupling between multipoles induced by the mask.

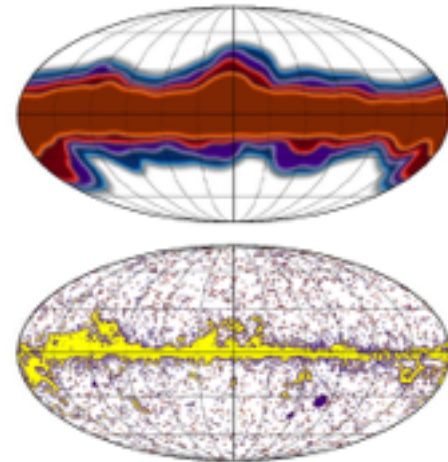
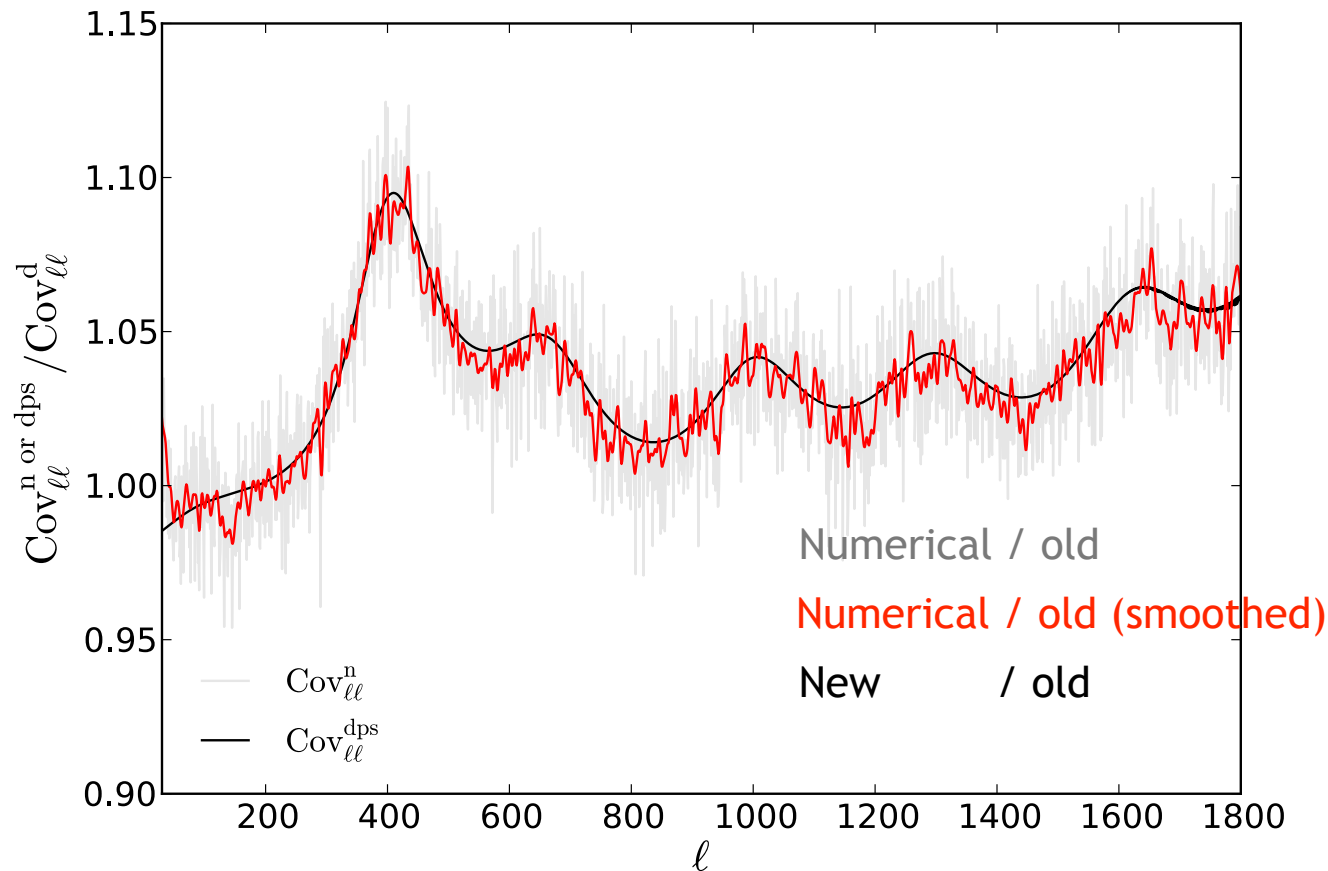
$$\mathcal{P}_{TT}[\ell, \ell', \alpha, \beta] = \sum_{\ell_1, \ell_2} \frac{2\ell+1}{4\pi} \begin{pmatrix} \ell & \ell_1 & \ell_2 \\ 0 & 0 & 0 \end{pmatrix}^2 \times \mathcal{W}^{TT}[\ell, \ell', \alpha, \beta], \quad (C.3)$$
$$\mathcal{P}_{EE}[\ell, \ell', \alpha, \beta] = \sum_{\ell_1, \ell_2} \frac{2\ell+1}{4\pi} (1 + (-1)^{\ell+\ell'}) \times \begin{pmatrix} \ell & \ell_1 & \ell_2 \\ 0 & 0 & 0 \end{pmatrix}^2 \mathcal{W}^{EE}[\ell, \ell', \alpha, \beta], \quad (C.4)$$
and
$$\mathcal{P}_{TE}[\ell, \ell', \alpha, \beta] = \sum_{\ell_1, \ell_2} \frac{2\ell+1}{4\pi} (1 + (-1)^{\ell+\ell'}) \times \begin{pmatrix} \ell & \ell_1 & \ell_2 \\ 0 & 0 & 0 \end{pmatrix} \begin{pmatrix} \ell & \ell_1 & \ell_2 \\ 2 & 2 & 0 \end{pmatrix} \mathcal{W}^{TE}[\ell, \ell', \alpha, \beta], \quad (C.5)$$
where $\ell, \ell' \in \{00, TT, EE\}$, and $\alpha, \beta \in \{TT, TE, TE, EE\}$. They make use of window functions \mathcal{W} .

- Apply to data,
- Repeat from step 1



Point sources mask and C_ℓ

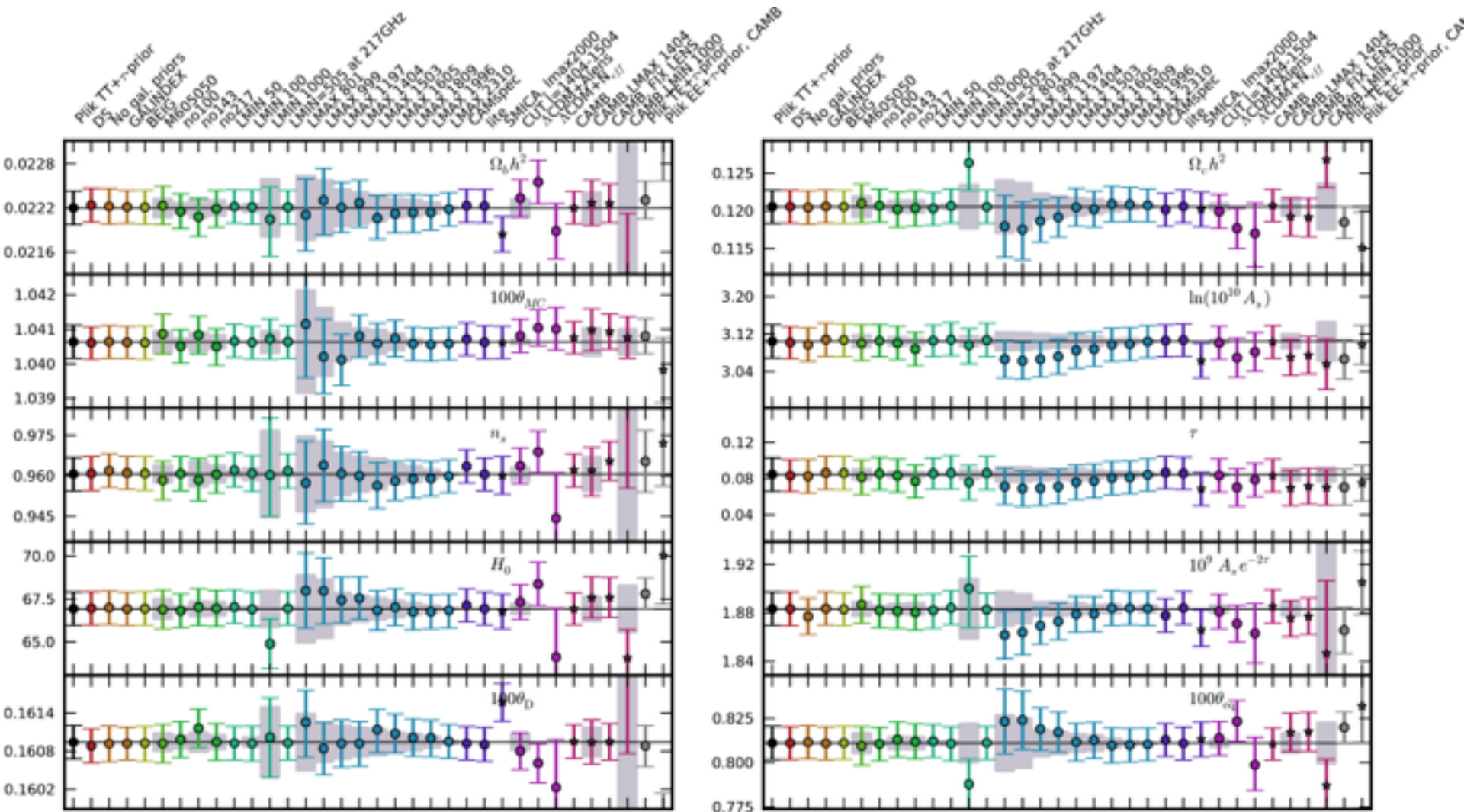
- In presence of a point source mask, the analytical computation of the covariance matrix (Efstathiou, 2004) that works fine for galactic masks, differ from Monte-Carlo based estimates, by up to 10 or 20%
- However, a new formalism, treating the point source 'holes' as a Poisson process, agrees much better with simulations (on going work with A. Challinor, F. Elsner, S. Gratton, M. Lilley & M. Migliaccio)



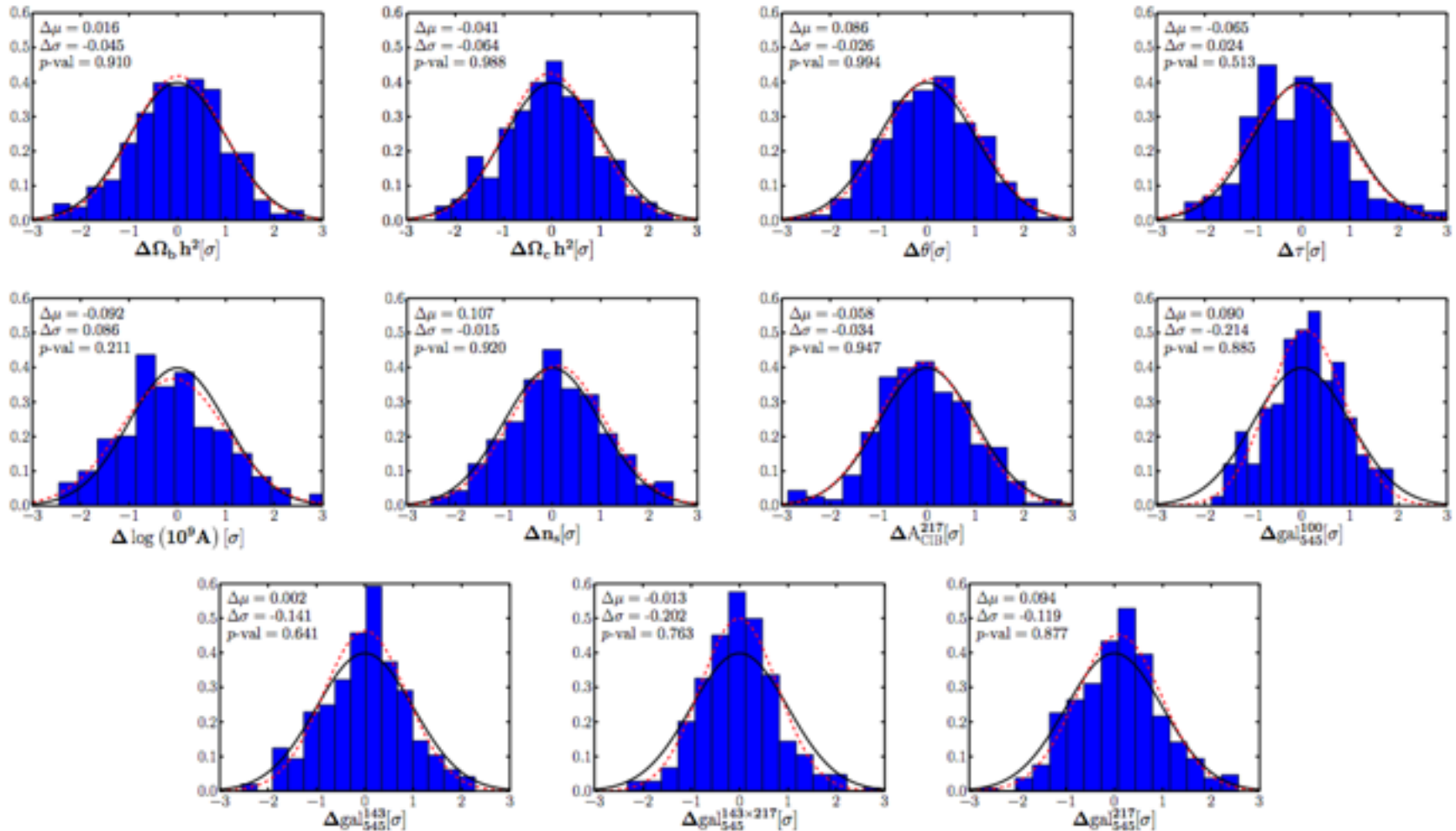
Validation

- tests, tests, and tests

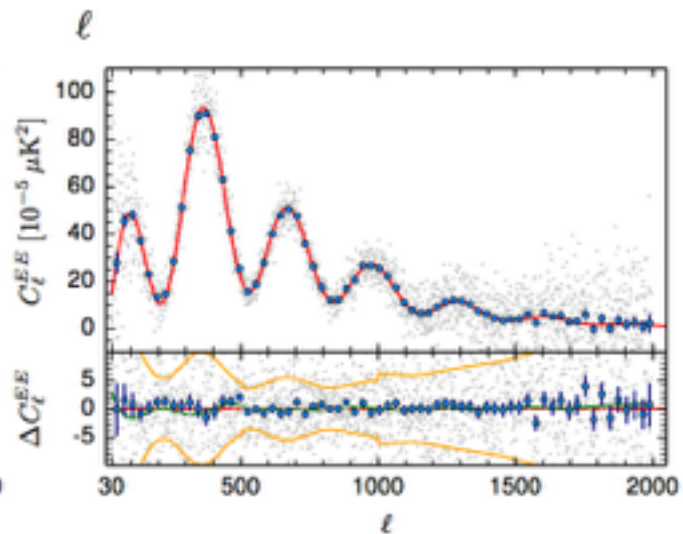
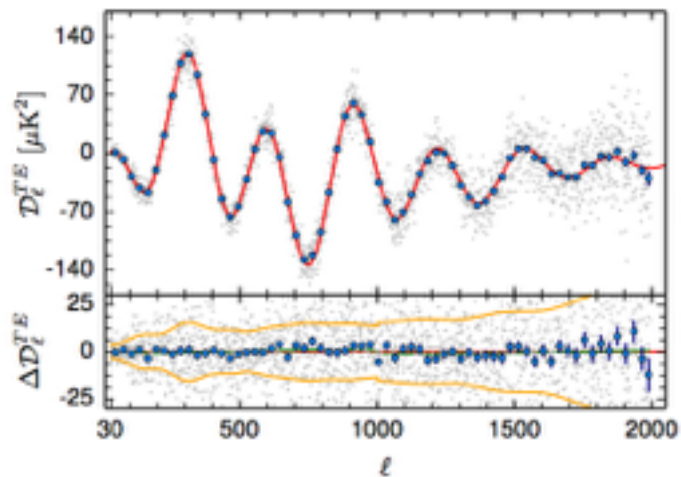
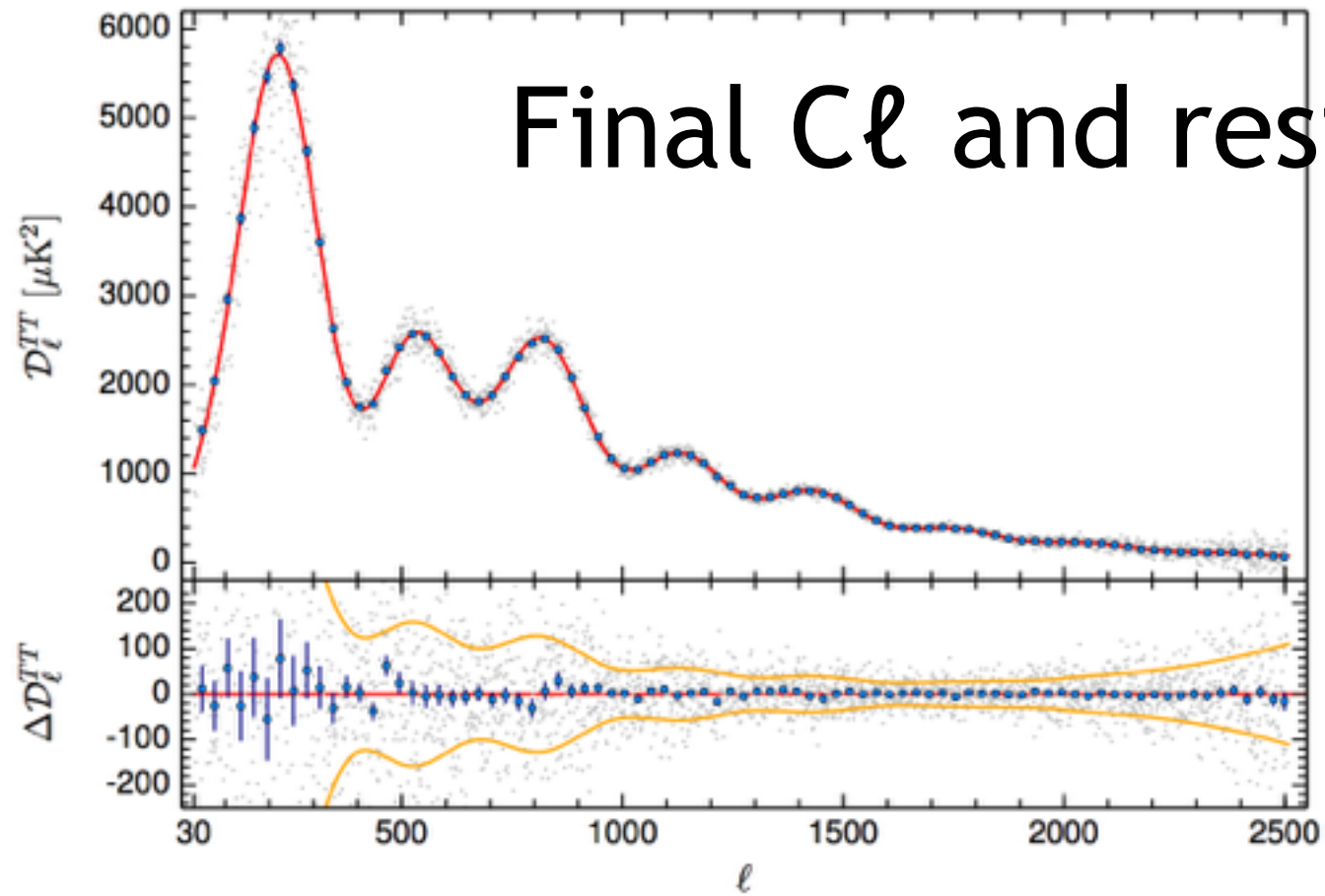
Test impact of various settings on final parameters



Tests final parameters of 300 end-to-end simulations



Final C_ℓ and residuals



Λ CDM results from TT

[1] Parameter	2013N(DS)	2015F(CHM) (Plik)	
$100\theta_{MC}$	1.04131 ± 0.00063	1.04086 ± 0.00048	
$\Omega_b h^2$	0.02205 ± 0.00028	0.02222 ± 0.00023	
$\Omega_c h^2$	0.1199 ± 0.0027	0.1199 ± 0.0022	
H_0	67.3 ± 1.2	67.26 ± 0.98	
n_s	0.9603 ± 0.0073	0.9652 ± 0.0062	
Ω_m	0.315 ± 0.017	0.316 ± 0.014	-1 sigma shift
σ_8	0.829 ± 0.012	0.830 ± 0.015	30% weaker
τ	0.089 ± 0.013	0.078 ± 0.019	constraint
$10^9 A_s e^{-2\tau}$	1.836 ± 0.013	1.881 ± 0.014	+3.5 sigma shift

2013=Planck Nominal 2013 TT+low-l WMAP polarization
 2015=Planck Full 2015 TT+low-l Planck LFI polarization.

- Very good consistency between 2013-2015.
- Error bars improved by ~30%
- Calibration change shifts $10^9 A_s e^{-2\tau}$.
- 2015 constraint on optical depth weaker and lower than 2013. We use large scale polarization from Planck LFI !
- Λ CDM is an excellent fit to the data!

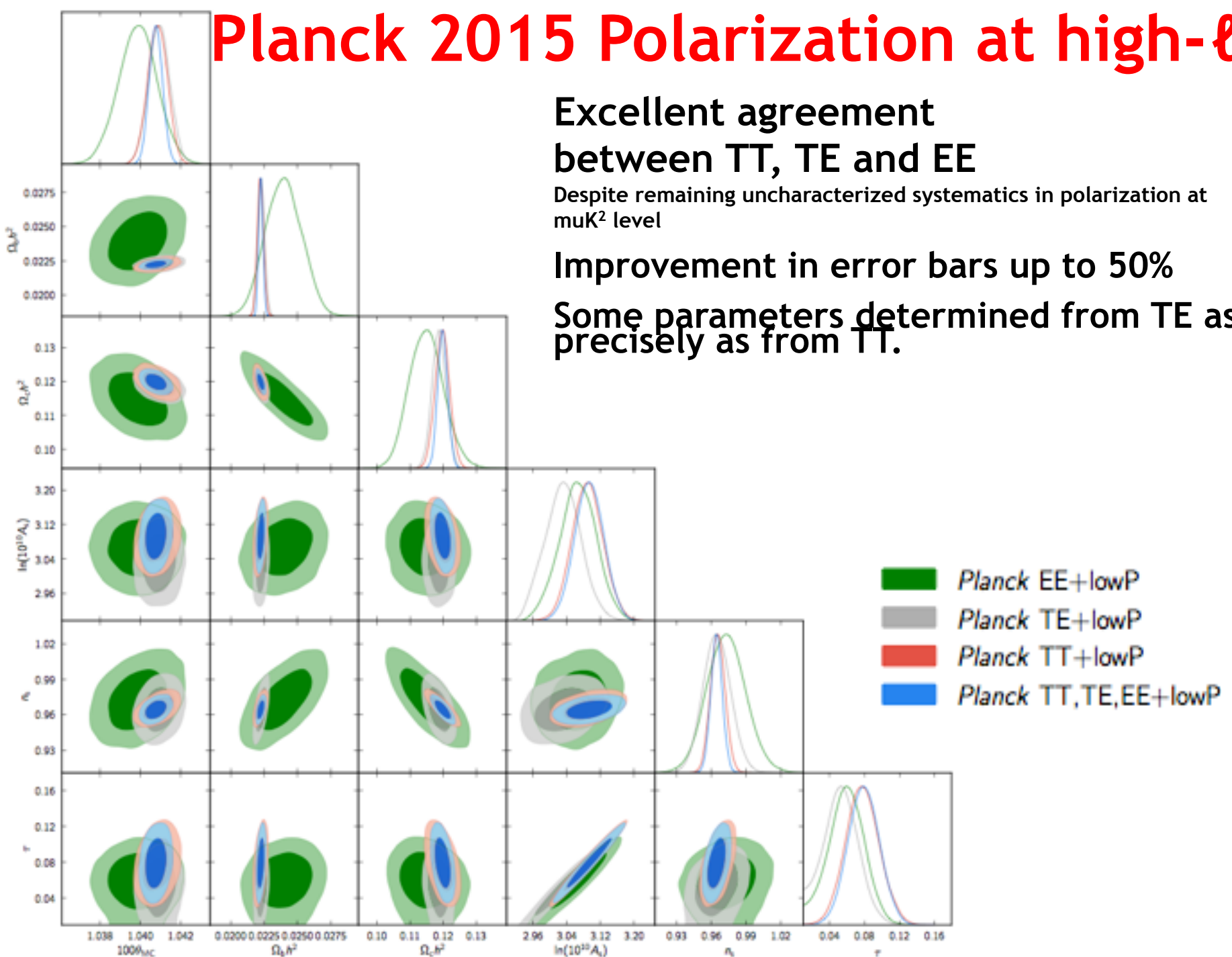
Planck 2015 Polarization at high- ℓ

Excellent agreement
between TT, TE and EE

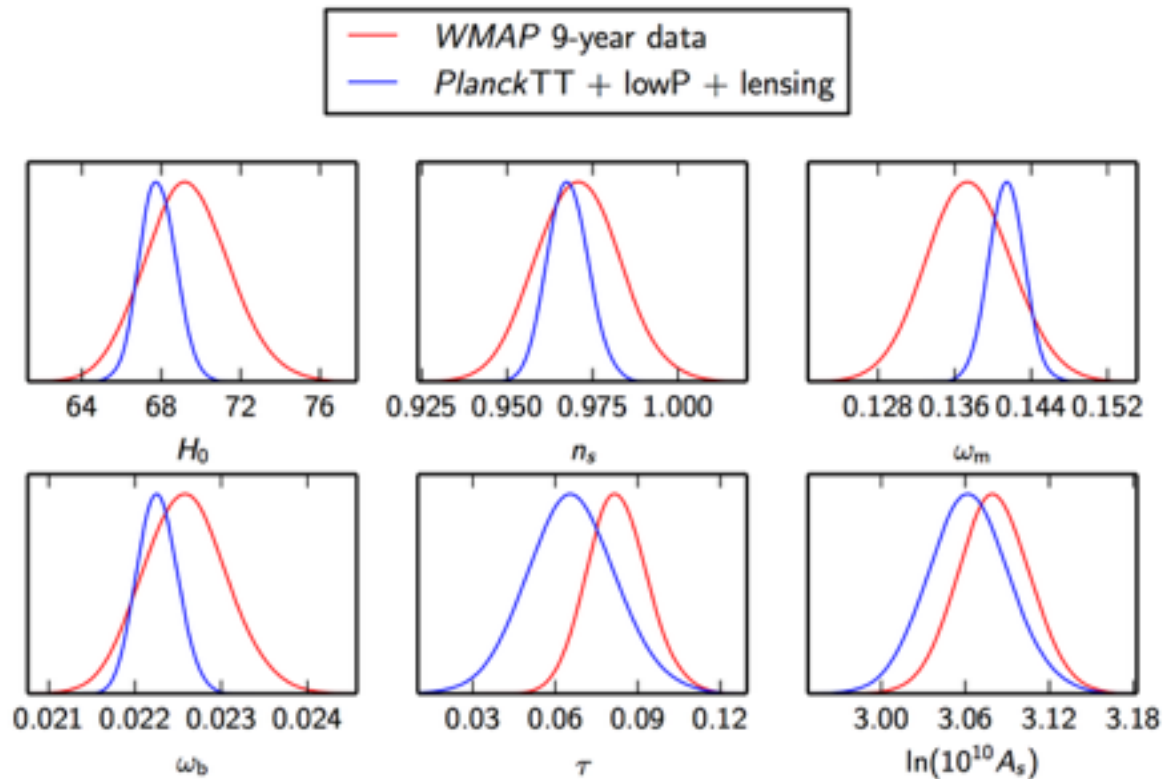
Despite remaining uncharacterized systematics in polarization at μK^2 level

Improvement in error bars up to 50%

Some parameters determined from TE as
precisely as from TT.



WMAP and Planck cosmologies



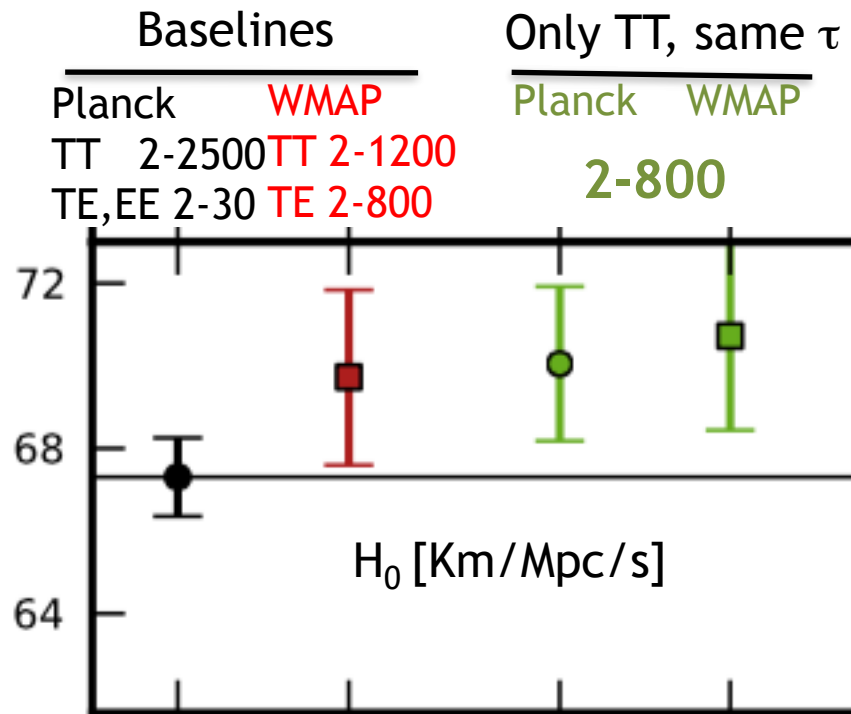
- WMAP and Planck parameters differ by ~ 1 σ_{WMAP} .
- WMAP errors factor 2 larger than Planck.

Hubble parameter
[Km/s/Mpc]

Planck	67.8 ± 0.92
WMAP	69.7 ± 2.1

Compare apples to apples

- Same prior on the optical depth, temperature only, same multipole region (although noise properties and fsky are still different).



- Planck and WMAP agree very well when compared properly
- **Still need to prove that shifts between $l_{\max}=800$ and $l_{\max}=2500$ for Planck itself are consistent with expectations!**

Recipes for successful CMB analysis

- To deal with **foregrounds**:
 - ◆ mask the most affected pixels,
 - ◆ then make a parametric fit of the remaining foreground Cl (where the foreground is dominant) using frequency differences, or masks differences, or a priori models,
 - ◆ then marginalise over the fit parameters.
- Poor knowledge of the **instrument**:
 - ◆ add as many free parameters as necessary, and fit and/or marginalise them (eg, polar efficiency, relative calibration with respect to 143GHz)
 - ◆ include the unknowns in the covariance matrix (non-diagonal, low rank terms), (eg, beam shape)
- Expected **systematic effects**:
 - ◆ model their impact on C_l , (eg, beam induced T to P leakage in 2017),
 - ◆ if not, find a template to be fit on the data, (eg, beam induced T to P leakage in 2015),
 - ◆ if not, find an upper limit on their impact.
- To assess **robustness** of the results:
 - ◆ compare various approaches, options, codes, hypotheses, ...
 - ▶ 5 pipelines at high- l , 4 CMB-only maps
 - ◆ compare to simulations,
 - ◆ test consistency across frequency, data splits, ...
- The analysis has to be repeated many, many times: need for a fast and robust pipeline

Bibliography

Hivon et al, 2017 (QuickPol) [2017A&A...598A..25H](#)

Hu et al, [2003PhRvD..67d3004H](#)

Planck 2015-XI, 2016 [2016A&A...594A..11P](#)

Takakura et al, 2017 (Polarbear) [2017JCAP...05..008T](#)

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The scientific results that we present today are a product of the Planck Collaboration, including individuals from more than 100 scientific institutes in Europe, the USA and Canada.



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