

*Galactic cosmic rays*  
+  $e^+/e^-$  asymmetry +  
++ dark matter signals ++

Julien Lavalle

Institute & Dept. of Theoretical Physics, Madrid Aut. Univ. & CSIC

III<sup>ième</sup> Ecole de Physique des Astroparticules, OHP 27-V-2011



# *Outline*

## *Part I: Cosmic-ray nuclei, propagation models*

- Generalities
- From a leaky box to slab models
- Secondary-to-primary ratios and constraints
- State-of-the-art; current predictions/issues

## *Part II: Cosmic-ray electrons and positrons*

- Energy-loss dominated propagation
- Interpretation of current data: the importance of local sources

## *Part III: Searches for dark matter annihilation signals*

- Gamma-rays and antimatter cosmic rays
- Constraints vs discovery potentials

# *Bibliography*

## **Part I: Cosmic-ray nuclei, propagation models**

- Longair, *High-energy astrophysics* vol.2, Cambridge University press (2<sup>nd</sup> ed. 1994).
- Berezinsky et al, *Astrophysics of cosmic rays*, Amsterdam:North-Holland, ed. Ginzburg (1990) – sold out.
- Ginzburg & Syrovastkii, *The origin of cosmic rays*, New-York:Macmillan (1964).
- Strong et al, *Cosmic-ray propagation and interactions in the Galaxy*, ARNPS 57 (2007) – astro-ph/0701517
- Maurin et al, *Galactic cosmic-ray nuclei as tools for astroparticle physics*, astro-ph/0212111

## **Part II: Cosmic-ray electrons and positrons**

- Delahaye et al, *Galactic electrons and positrons at the Earth*, A&A 524, A51 (2010), arXiv:

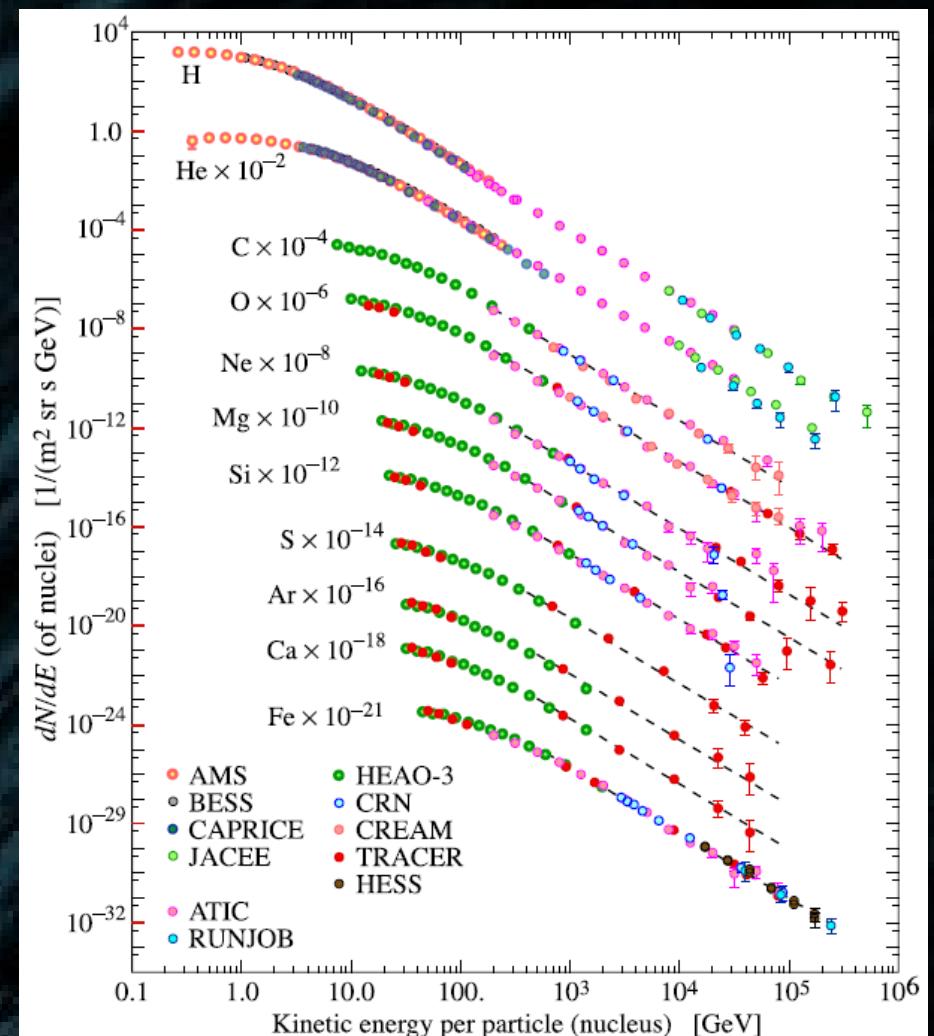
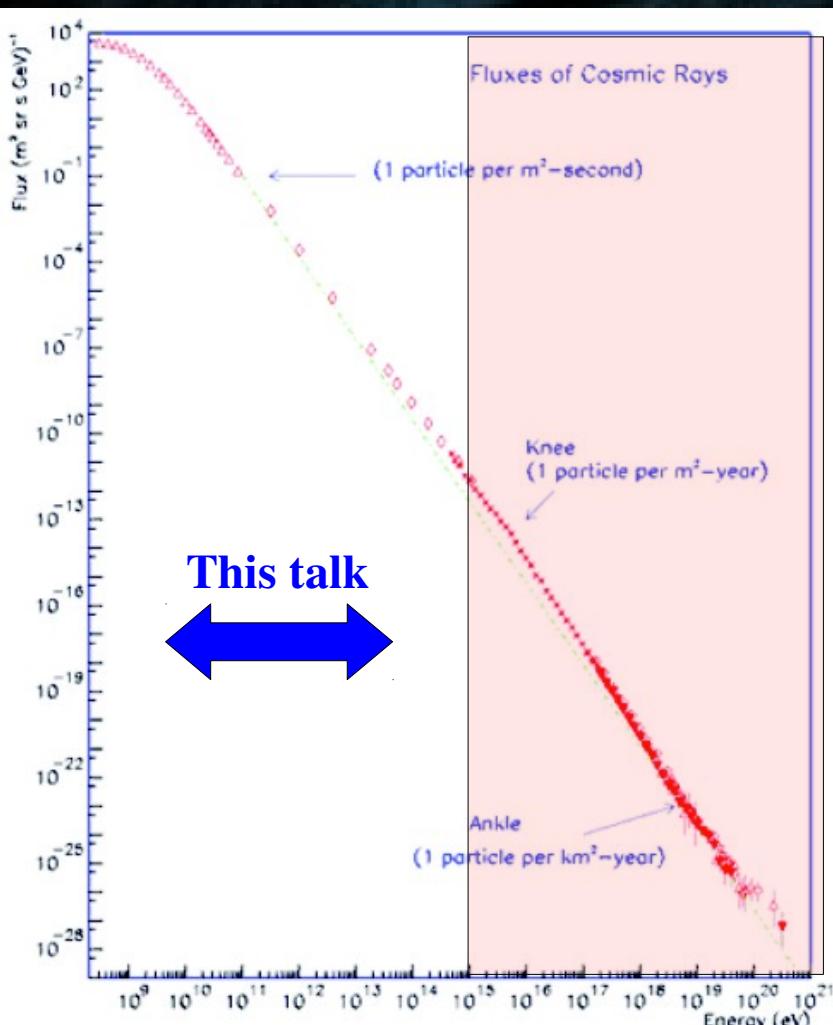
## **Part III: Searches for dark matter annihilation signals**

- Salati's lectures:  
[http://www.lapth.in2p3.fr/~salati/APP\\_ENS\\_11.pdf](http://www.lapth.in2p3.fr/~salati/APP_ENS_11.pdf) (in French, M2 lectures ENS-Lyon)  
[http://pos.sissa.it/archive//conference/049/009/cargese\\_009.pdf](http://pos.sissa.it/archive//conference/049/009/cargese_009.pdf) (in English, Cargese 07)

# Generalities

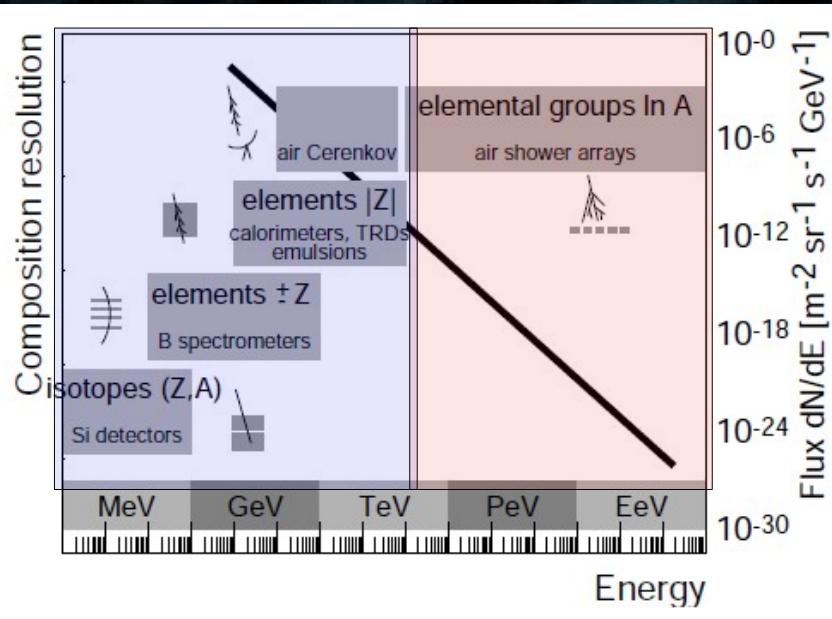
Cosmic rays (CRs) as tools for fundamental physics:

- 1900-1913: Victor Hess, Theodor Wulf and Domenico Pacini pioneer the discovery of CRs
- 1932: Anderson discovers the positron by chance in a bubble chamber (CR-induced shower)
  - positrons were predicted by Dirac in 1928.
- 1930-1953: discovery of muons, pions and kaons
- 1950's: beginning of the accelerators' era ( $> 1$  GeV)



# *Detection techniques: from balloons to space*

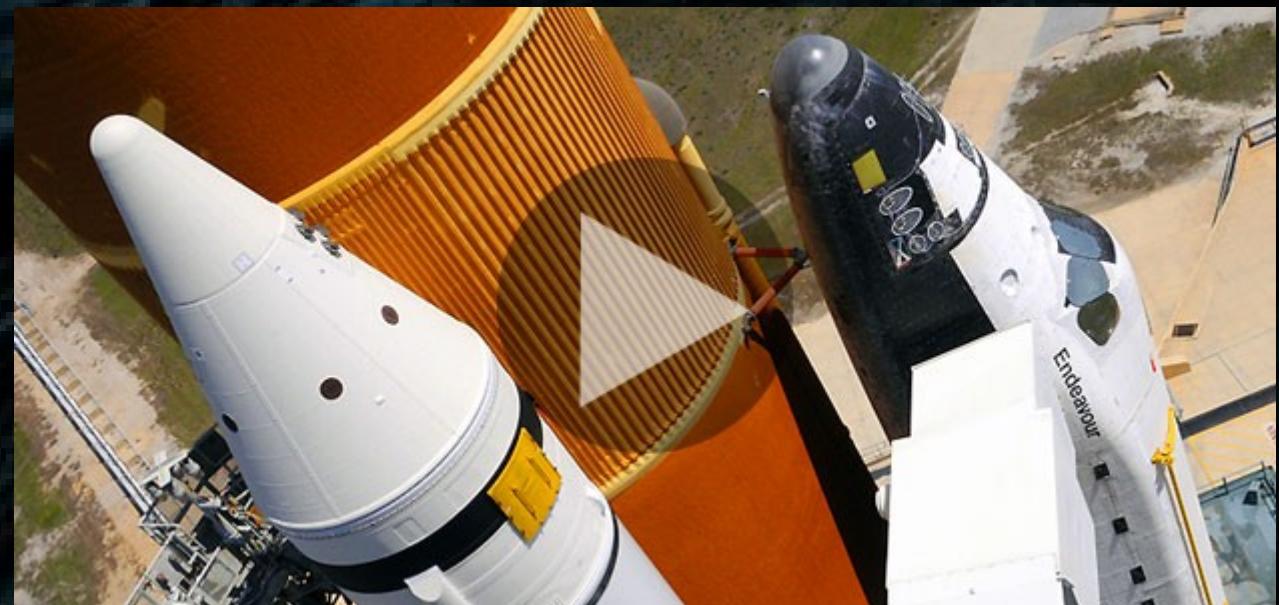
Hörandel (2007)



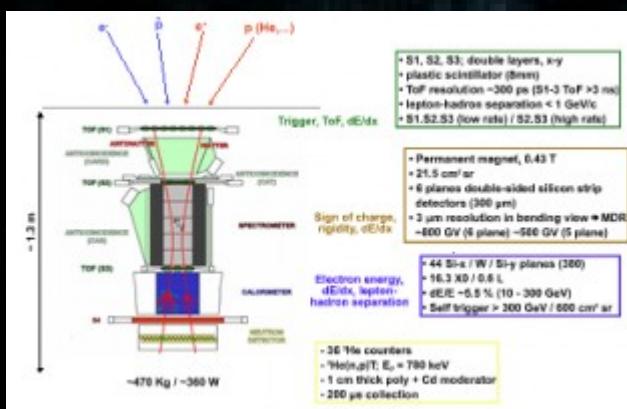
CREAM IV flight



Endeavour (AMS onboard)



PAMELA design

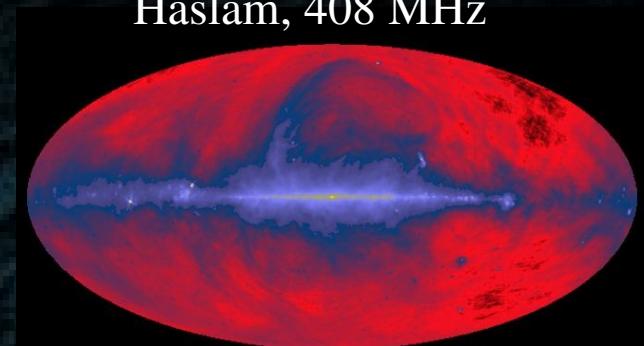


# Cosmic-ray transport throughout the Galaxy

$$\underbrace{\partial_t \mathcal{N}}_{\text{time evolution}} = \underbrace{\mathcal{Q}(\vec{x}, E, t)}_{\text{source}} + \vec{\nabla} \cdot \left\{ \left( K_{xx}(E) \vec{\nabla} - \vec{V}_c \right) \mathcal{N} \right\} - \partial_p \left\{ \left( \dot{p} - \frac{p}{3} \vec{\nabla} \cdot \vec{V}_c - p^2 K_{pp}(E) \partial_p \frac{1}{p^2} \right) \mathcal{N} \right\} - \underbrace{\frac{\tau_s + \tau_r}{\tau_s \tau_r} \mathcal{N}}_{\text{spallation, decay}}$$



The level of assumptions/simplifications should be defined for each specific problem under study



# *Link between diffusion and turbulence*

(Martin Lemoine's lecture)

$$\frac{d\vec{p}}{dt} = q \left( \vec{E} + \vec{\beta} \times \vec{B} \right)$$

$$\vec{B} = \vec{B}_0 + \delta\vec{B}$$

$$\langle (\Delta x)^2 \rangle = \langle (x(t) - x(0))^2 \rangle \propto t^\gamma$$

$$\vec{E} = \vec{E}_0 + \delta\vec{E}$$

$$K_{xx} = \lim_{t \rightarrow \infty} \frac{\langle (\Delta x)^2 \rangle}{2 t}$$

$$K_{xx} = K_{xx}(\mathcal{R}) \approx \beta K_0 \left[ \frac{\mathcal{R}}{\mathcal{R}_0} \right]^{2-a}$$

Galactic B-field difficult to model:  $\delta B \sim B_0$ , spiral structure for the regular field, etc.

=> Diffusion is treated semi-empirically in CR transport models

(usually homogeneous, with free  $K_0$  and  $\delta$ )

*A simplistic but pedagogical approach:  
the Leaky Box model*



$$\partial_t \mathcal{N}_i = 0$$

$$\frac{\mathcal{N}_i}{\tau_{\text{esc}}} + \Gamma_i \mathcal{N}_i = \mathcal{Q}_i + \sum_j \Gamma_{j \rightarrow i} \mathcal{N}_j$$

# *Leaky Box:* *escape time from secondary-to-primary ratios*

$$\frac{\mathcal{N}_p}{\tau_{\text{esc}}} + \Gamma_p \mathcal{N}_p = Q_p$$

Pure primary species: escape time  
degenerate with source

$$\frac{\mathcal{N}_s}{\tau_{\text{esc}}} + \Gamma_s \mathcal{N}_s = \Gamma_p \mathcal{N}_p$$

Pure secondary species: escape time  
degenerate with primary density

$$\frac{\mathcal{N}_s}{\mathcal{N}_p} = \frac{\Gamma_p}{\Gamma_s + 1/\tau_{\text{esc}}} \approx \tau_{\text{esc}}(E)$$

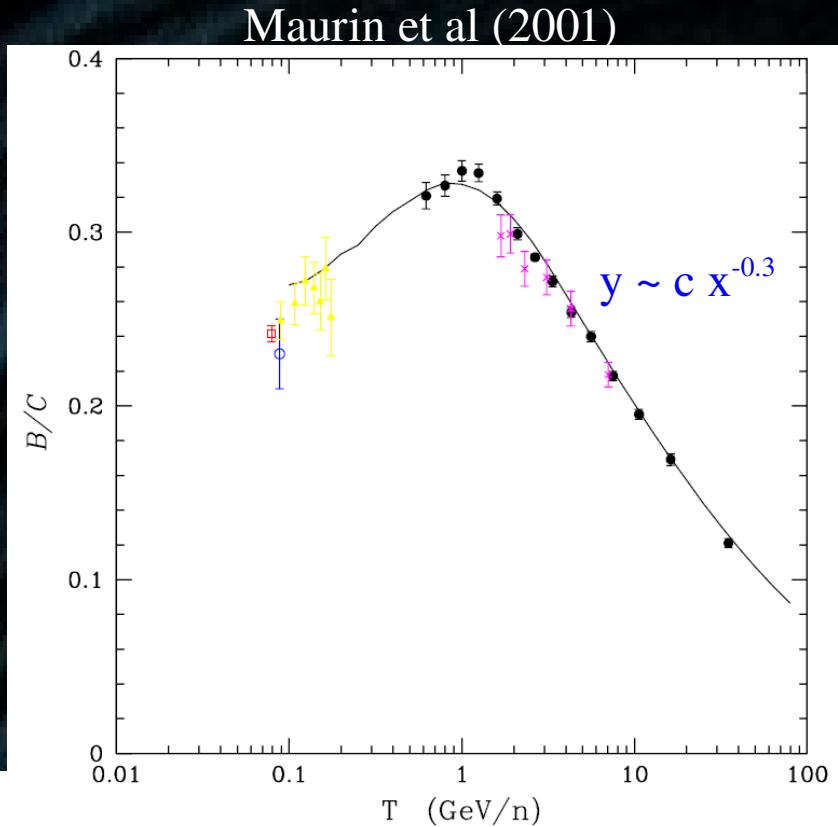
**Ratio: degeneracy broken!**

# *Leaky Box:* *escape time from secondary-to-primary ratios*

$$\frac{\mathcal{N}_p}{\tau_{\text{esc}}} + \Gamma_p \mathcal{N}_p = Q_p$$

$$\frac{\mathcal{N}_s}{\tau_{\text{esc}}} + \Gamma_s \mathcal{N}_s = \Gamma_p \mathcal{N}_p$$

$$\frac{\mathcal{N}_s}{\mathcal{N}_p} = \frac{\Gamma_p}{\Gamma_s + 1/\tau_{\text{esc}}} \approx \tau_{\text{esc}}(E)$$

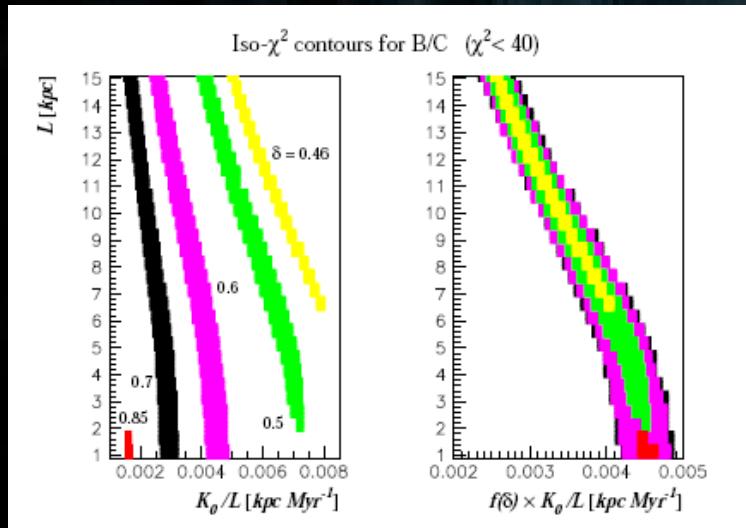
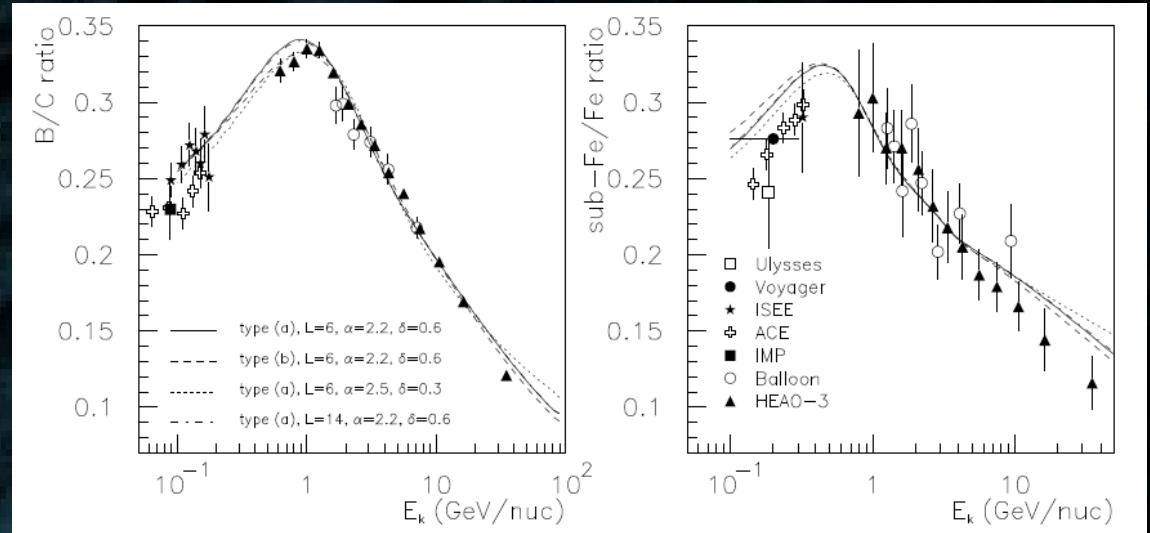


**Ratio: degeneracy broken!**

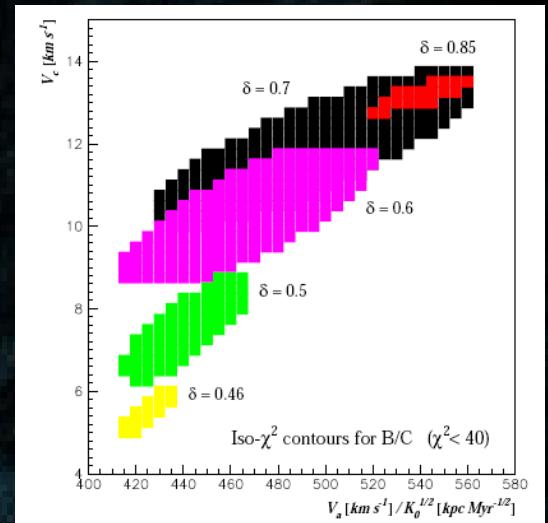
Escape time  $\sim 10\text{-}100$  Myr

# Transport parameter degeneracy

Propagation parameters constrained  
with data on **secondaries/primaries**  
(e.g. B/C): **degeneracies !!!!**



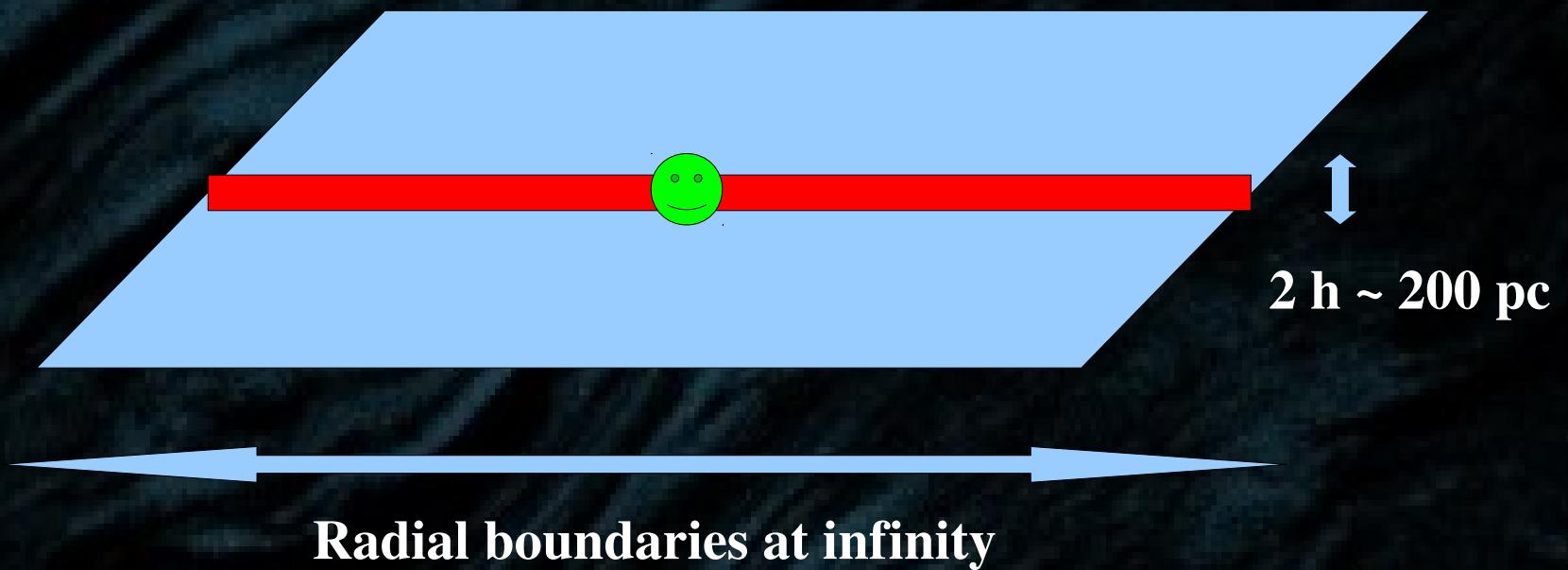
e.g.:  
Maurin's PhD thesis (2001)  
also Maurin et al (2001)



# *A more physical model: the infinite slab*

$$-K_{xx} \frac{d^2 \mathcal{N}}{dz^2} + 2 h \delta(z) n_{\text{ism}} v \sigma \mathcal{N} = 2 h \delta(z) q$$

$2 L \sim 10 \text{ kpc}$



$$\mathcal{N}(|z| = L) = 0$$



$$\begin{cases} \mathcal{N}(z) = \mathcal{N}(0) \frac{L - |z|}{L} \\ \frac{K_{xx}}{h L} \mathcal{N}(0) + n_{\text{ism}} v \sigma \mathcal{N}(0) = q \end{cases}$$

# *Link with the Leaky Box approximation: Key tool to understand degeneracies*

$$\begin{cases} \mathcal{N}(z) = \mathcal{N}(0) \frac{L - |z|}{L} \\ \frac{K_{xx}}{h L} \mathcal{N}(0) + n_{\text{ism}} v \sigma \mathcal{N}(0) = q \end{cases}$$

$$\frac{\mathcal{N}_p}{\tau_{\text{esc}}} + \Gamma_p \mathcal{N}_p = Q_p$$

$$\tau_{\text{esc}} = \frac{h L}{K_{xx}}$$

Secondary-to-primary ratios provide  
constraints on K/L, not K!  
 $\Leftrightarrow$  K and L degenerate

# Radioactive species: a way to break $\mathcal{K}$ - $\mathcal{L}$ degeneracy

$$-K_{xx} \frac{d^2 \mathcal{N}_r}{dz^2} + \frac{\mathcal{N}_r}{\tau_r} = 2 h \delta(z) n_{\text{ism}} v \sigma \mathcal{N}$$

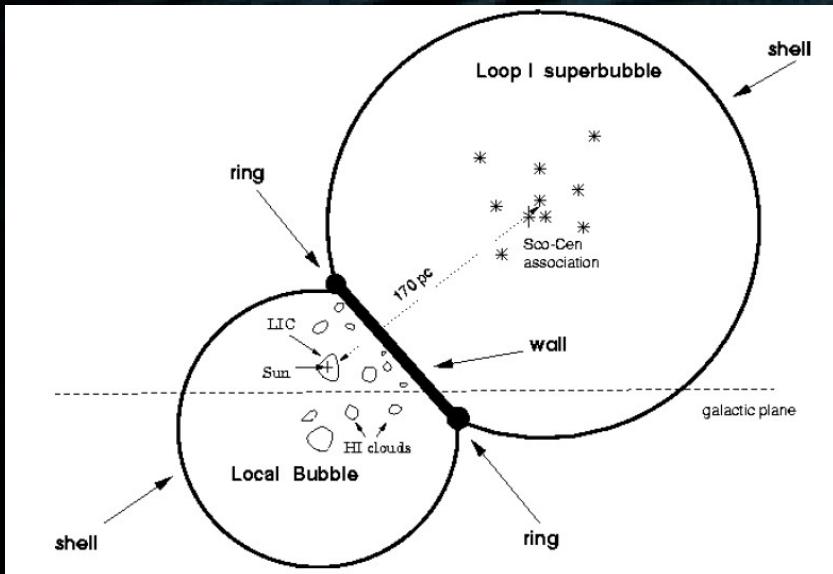
Make sure that  $K\tau_r \ll L^2$

$$\begin{cases} \mathcal{N}_r(z) = \mathcal{N}_r(0) \exp \left\{ -\frac{|z|}{\sqrt{K_{xx}\tau_r}} \right\} \\ \frac{\mathcal{N}_r(0)}{\mathcal{N}(0)} = \frac{h n_{\text{ism}} \sigma v}{\sqrt{K_{xx}\tau_r}} \end{cases}$$

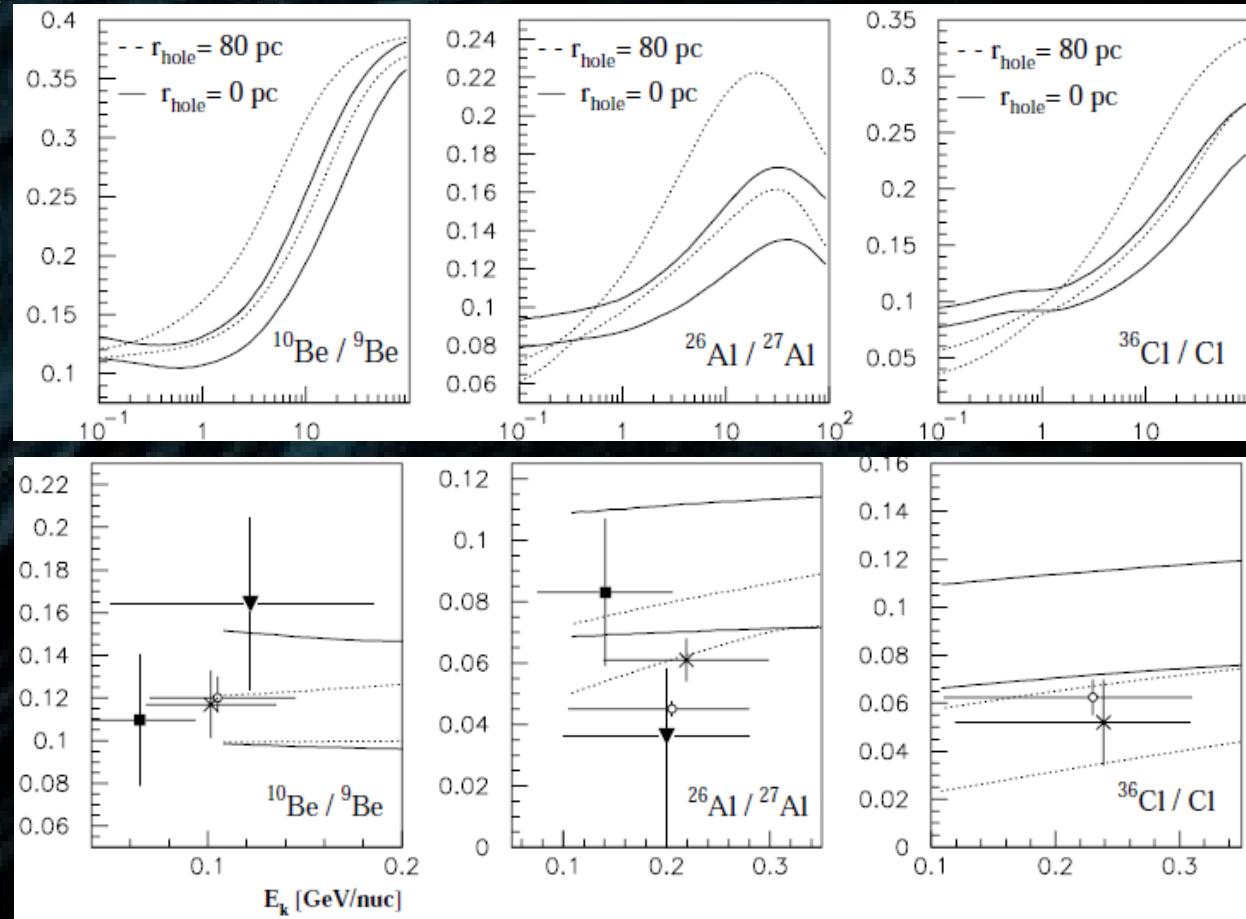
=> direct measure of K !!!!

# *Not that easy ... short propagation scale requires accurate description of LISM ...*

We are located in a low ISM density bubble (eg Breitshwerdt 2000)



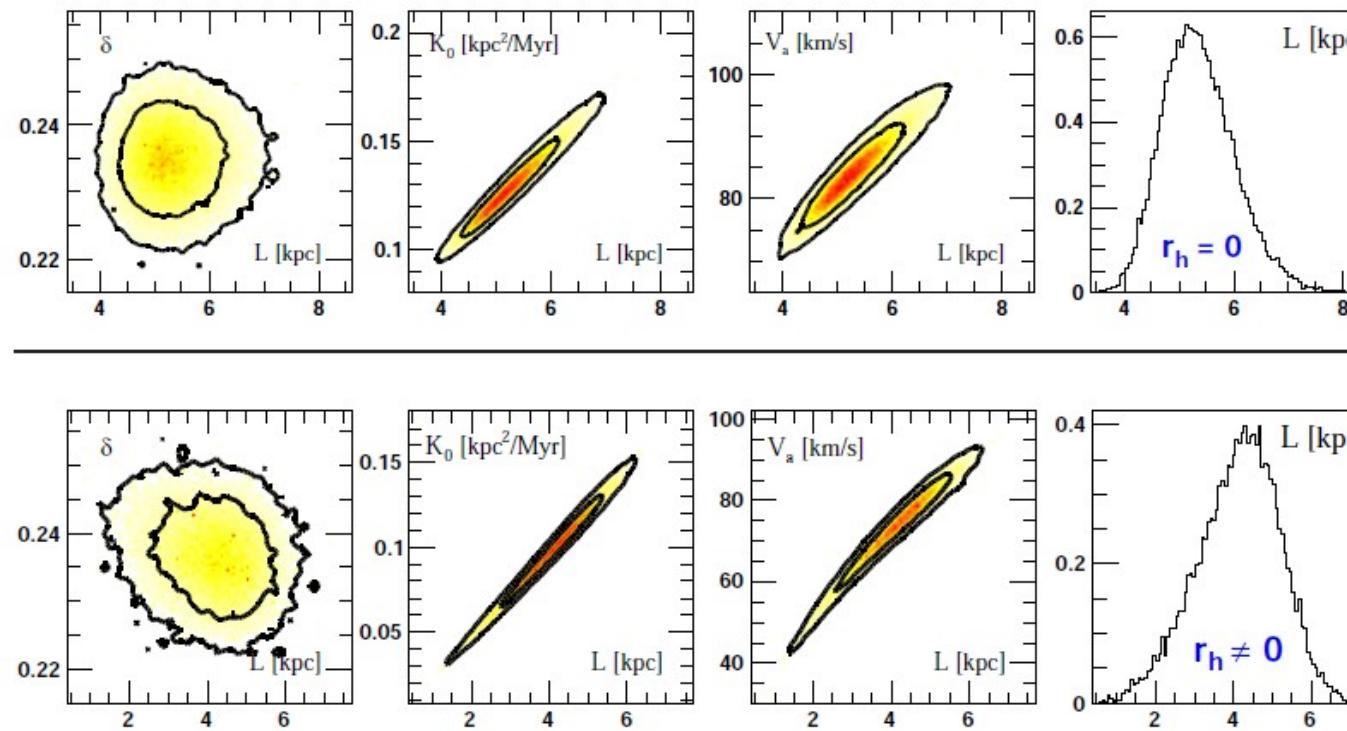
Donato et al (2002)



=> Predictions very sensitive to LISM modeling;  
data not accurate enough (waiting for AMS02)

# *Current state of the art: Statistical analysis and constraints*

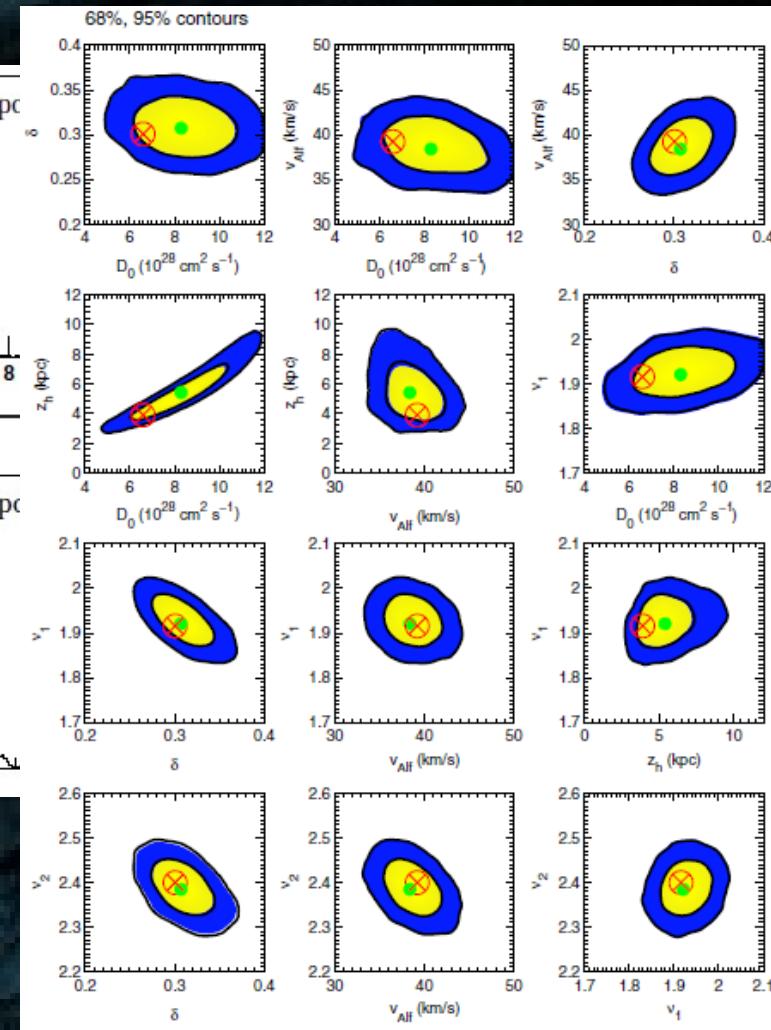
Putze, Maurin et al (2010-xxxx)  
MCMC analysis, semi-analytical models



=> Phenomenological analyses providing sets  
of parameters associated with statistical  
significances.

=> Do not forget initial assumptions!

Trotta et al (2010) – Galprop



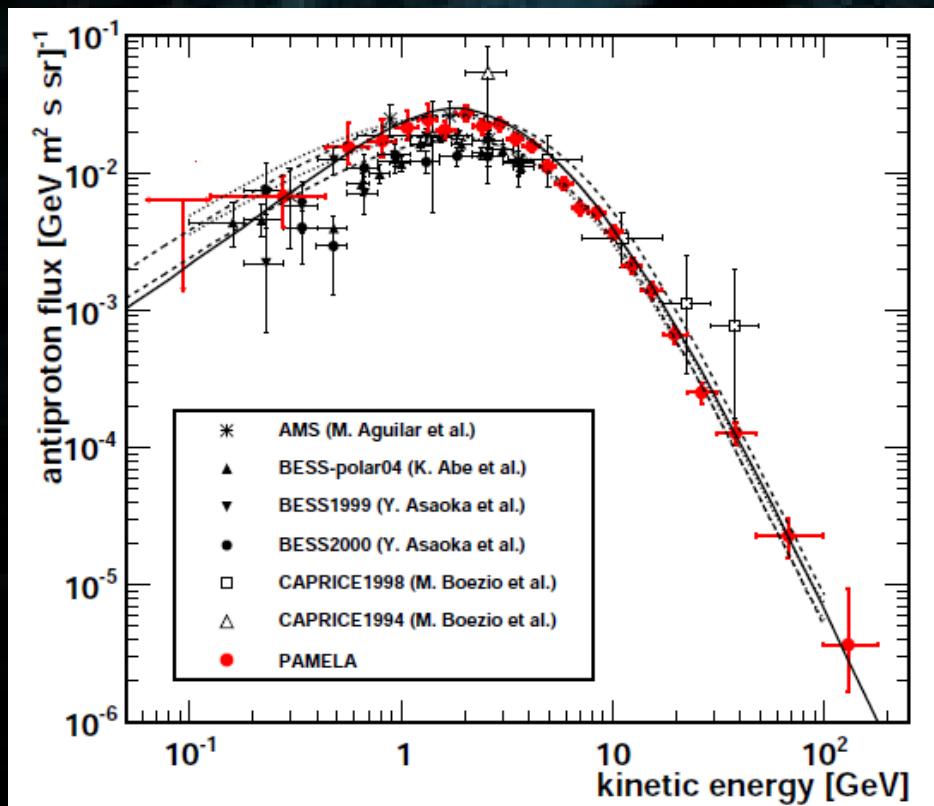
# *Transport of CR nuclei: summary*

- Diffusion equation hard to solve in a general context: approximations needed.
- Different complementary approaches: full numerical / semi-analytical.
- Transport parameters are somewhat degenerate (eg K and L).
- Modelings of sources (spatial distribution) and ISM have some impact.
- Still some uncertainties in the nuclear cross sections.
- Current state-of-the-art: Full statistical analyses of Sub-C/C, sub-Fe/Fe and isotopic ratios => AMS-02 will improve error bars!

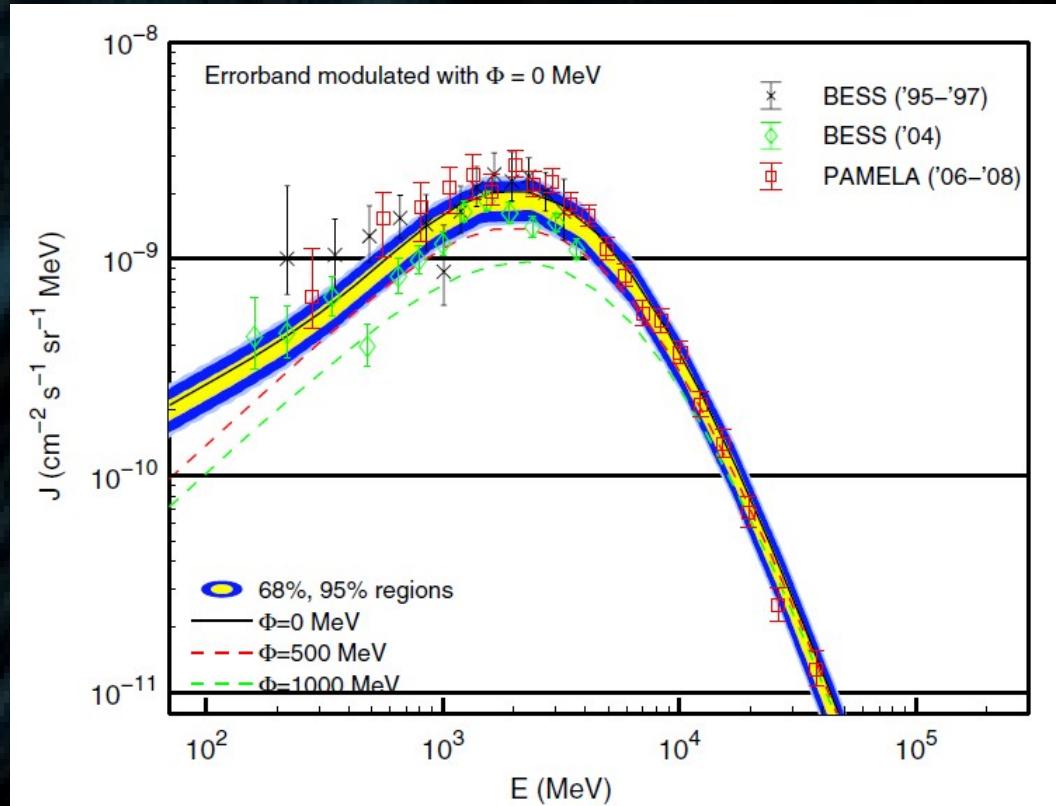
# $\text{CR}$ nuclei transport models: applications

## 1) Antiprotons

PAMELA antiproton data (Adriani et al 10)  
vs predictions by Donato et al 01, Ptuskin et al 06



Galprop predictions (Trotta et al 10)

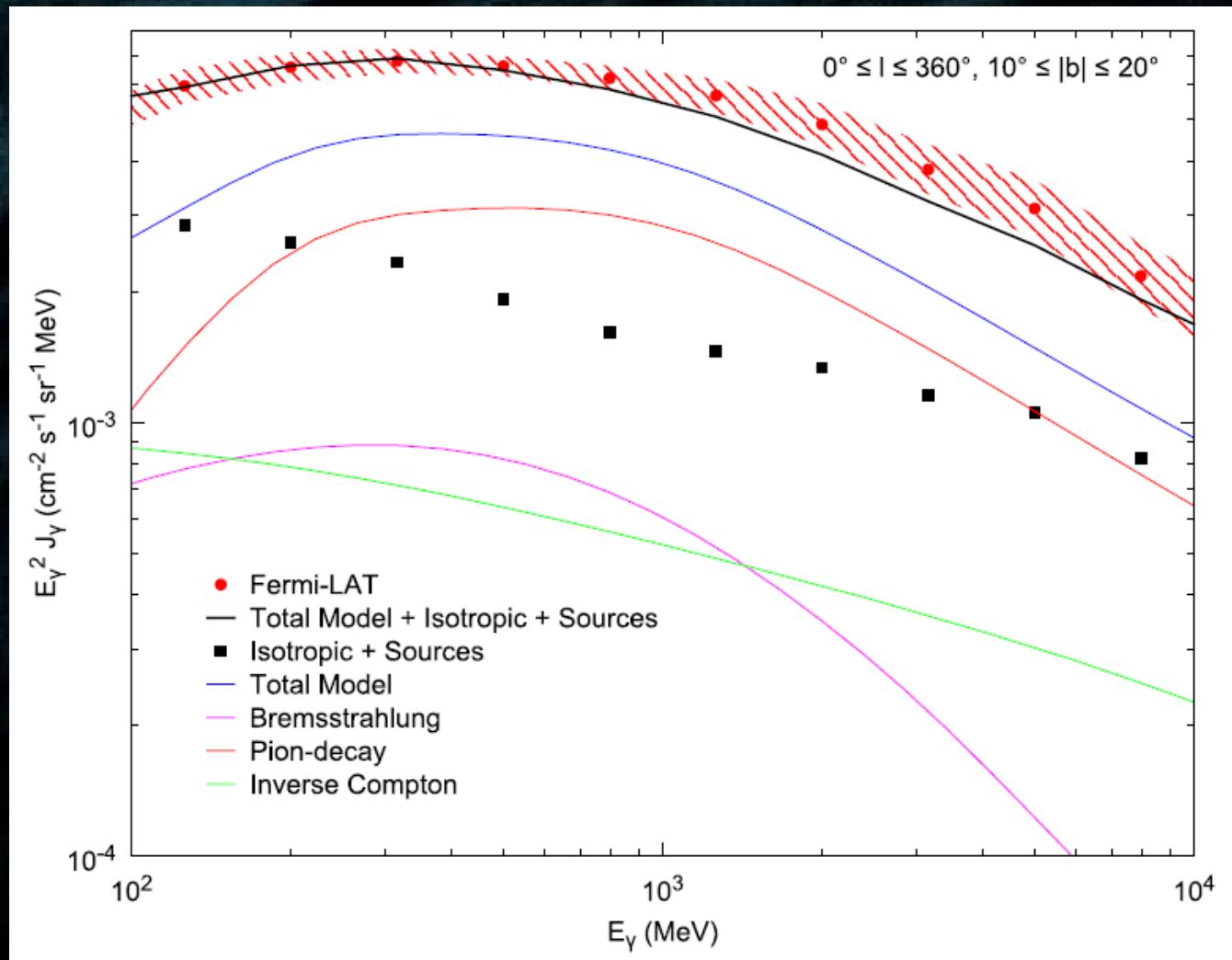


Semi-analytical models provide good fit to the antiproton data.  
Galprop finds the data in excess wrt predictions  
(but fails to fit a reacceleration+convection model to B/C)

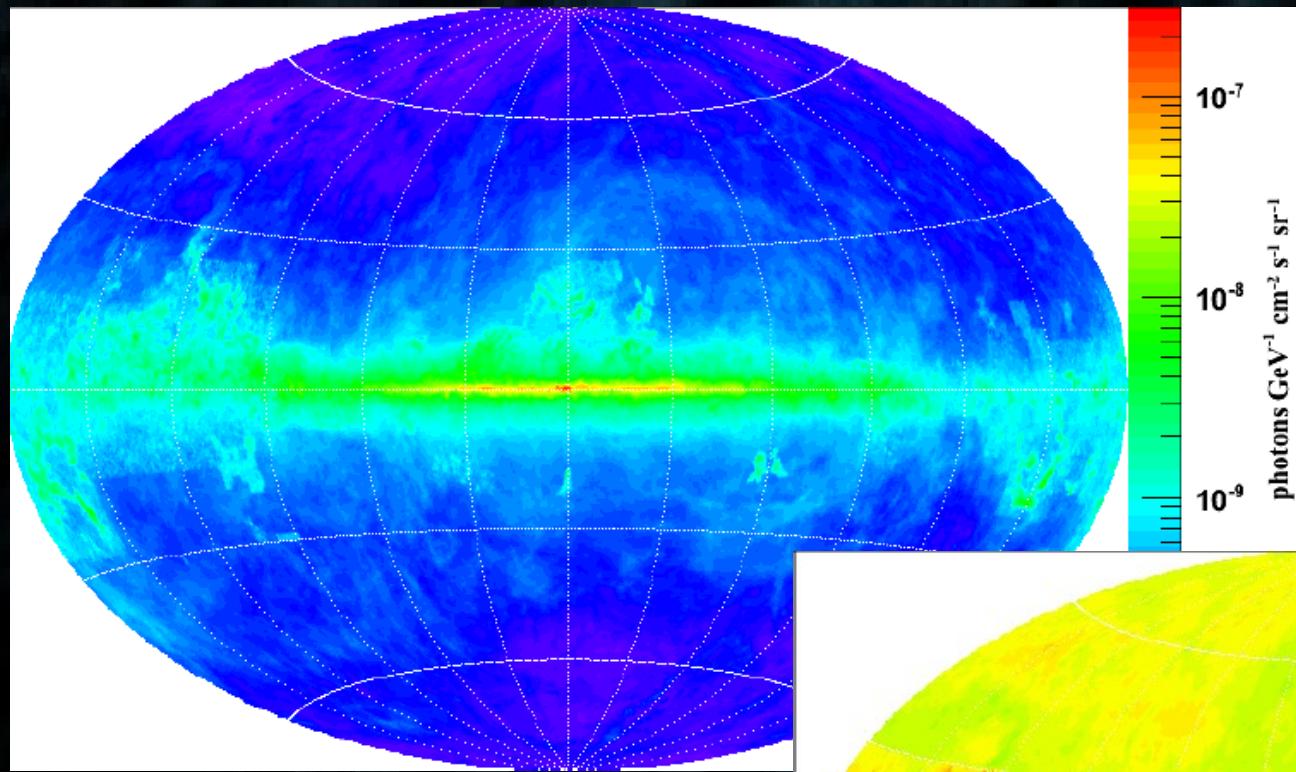
# *CR nuclei transport models: applications*

## *2) Diffuse gamma-rays*

Galprop predictions (Trotta et al 10)



# *CR nuclei transport models: applications**2) Diffuse gamma-rays*

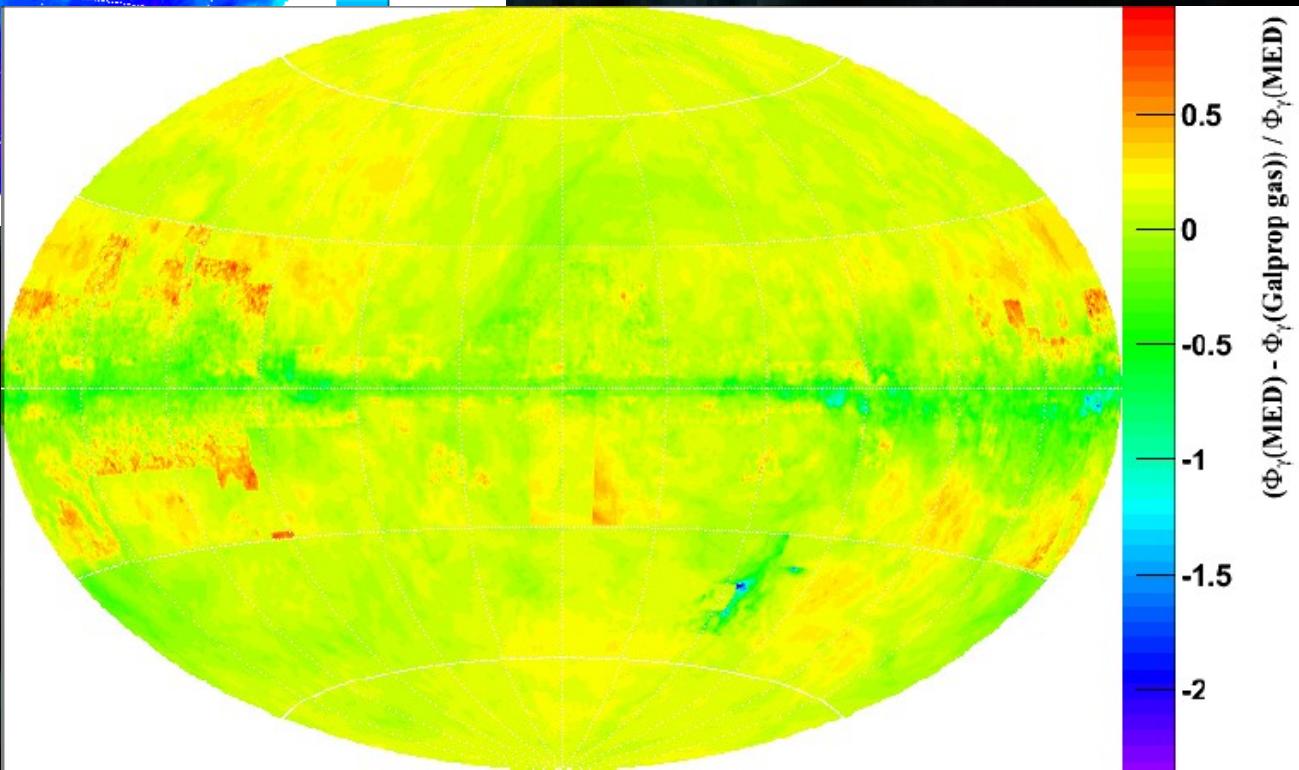


Hadronic component only  
from Delahaye et al (2011)

Hydrogen 3D map from  
Pohl et a (2008).

HI and CO surveys deconvolved with  
an SPH gas-flow model (Bissantz et al  
03)

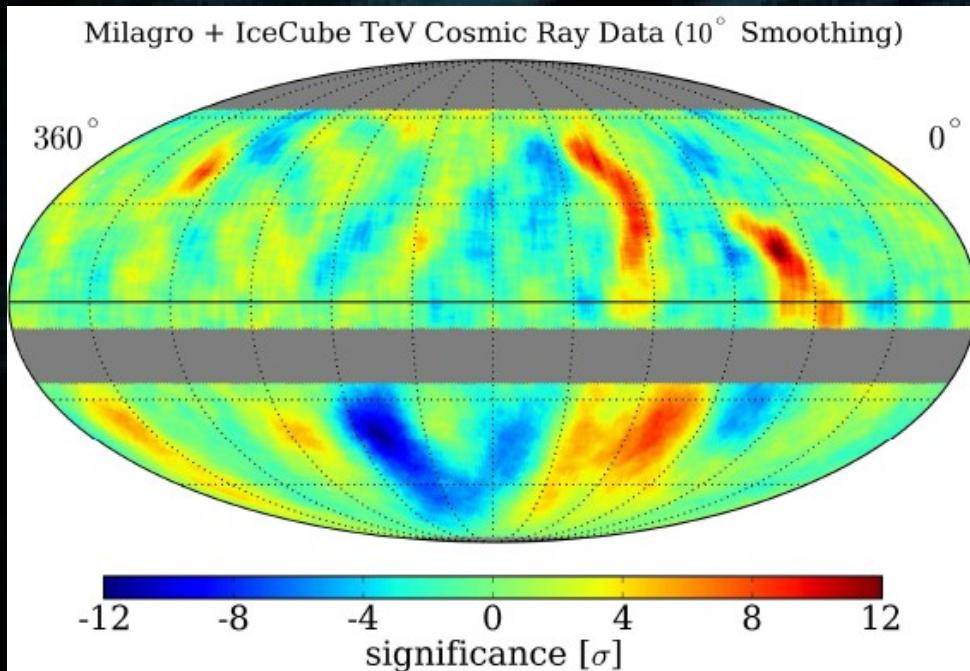
=> large discrepancies wrt Galprop



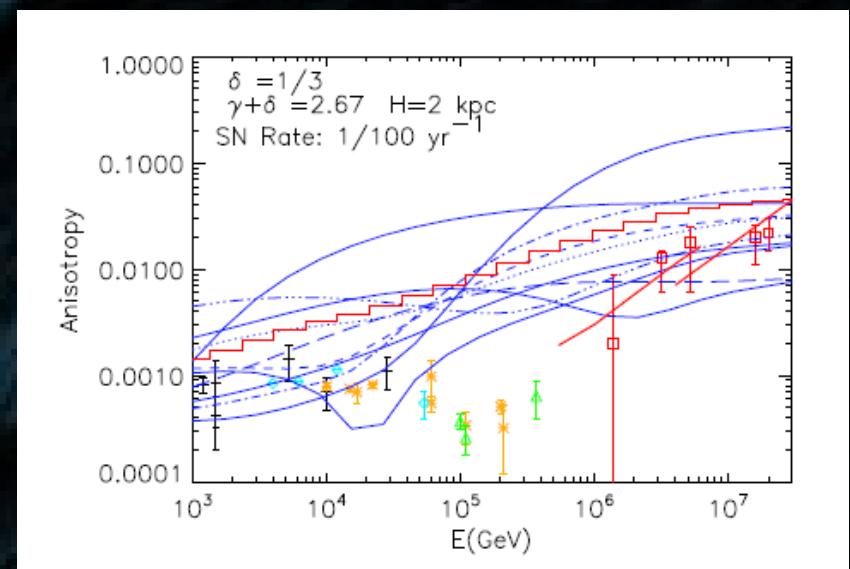
# $\text{CR nuclei transport models: applications}$

## 3) Anisotropies

Icecube: arXiv:1105.2326



MC trials by Blasi & Amato  
arXiv:1105.4529



$$\delta(\theta) = \frac{I_{\max}(\theta) - I_{\min}(\theta)}{I_{\max}(\theta) + I_{\min}(\theta)}$$

$$I(\theta, \phi) = \sum A_{l,m} Y_l^m(\theta, \phi)$$

Phd Thesis Guilhem Bernard  
(LAPTh-Annecy)

$$I_i(\theta) = A_{0,0} + A_{1,0} \cos(\theta) = \bar{I}_i + \delta \bar{I}_i \cos(\theta)$$

$$\phi_i(0) - \phi_i(\pi) = -|\mathcal{J}| = \int d\Omega \cos(\theta) I_i(\theta) = \frac{4\pi}{3} \delta \bar{I}_i$$

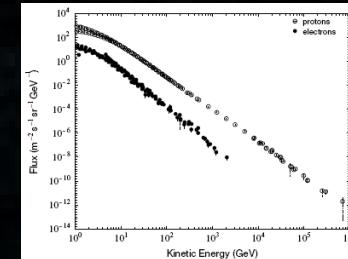
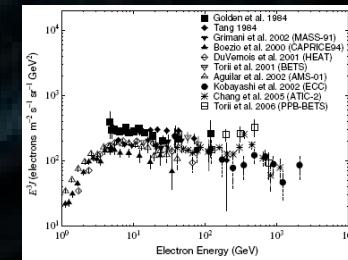
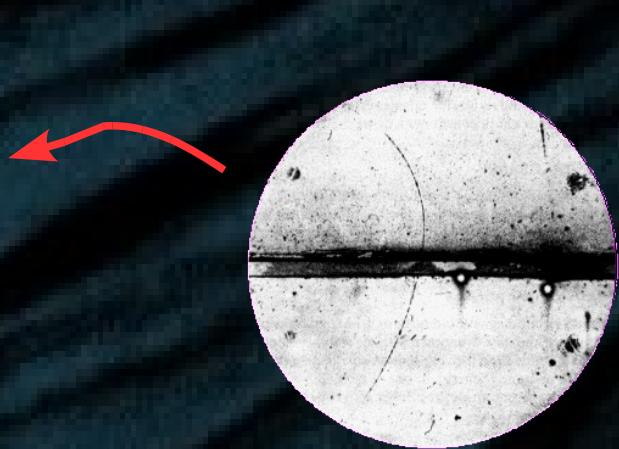
$$\delta_i = \frac{3 K_{xx} |\vec{\nabla} \mathcal{N}_i|}{4 \pi \bar{I}_i} = \frac{3 K_{xx}}{c} \frac{|\vec{\nabla} \mathcal{N}_i|}{\mathcal{N}_i}$$

# *Predictions involving CR nuclei: summary*

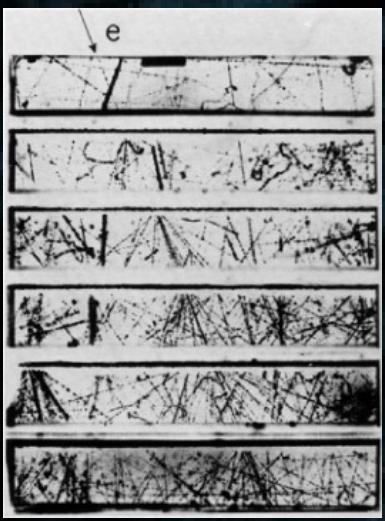
- Rough agreement for predictions relying on large scale averages (eg antiprotons).
- Incredibly successful for diffuse gamma-rays !
- Strongly model-dependent for finer effects (eg gas modeling for diffuse gamma-rays); more reliable but less constrained at high energy (no convection nor reacceleration effects).
- No standard model so far (Galprop is not a “standard model”).

# *Cosmic-ray electrons and positrons*

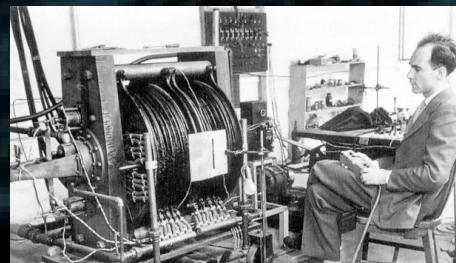
# Brief historical review



Review by Yoshida (2008)



Discovery of the positron  
Anderson, Phys. Rev. (1933)

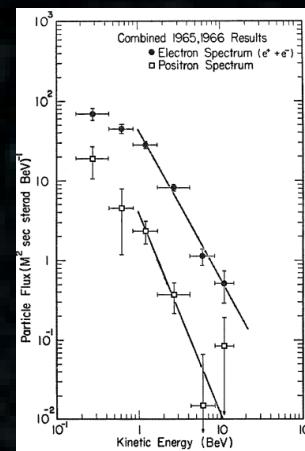
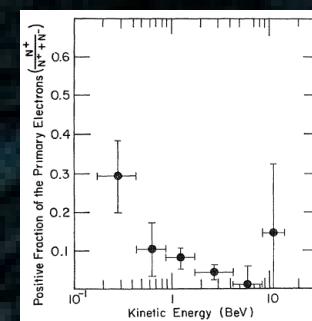


CARL D. ANDERSON, California Institute of Technology, Pasadena, California  
(Received February 28, 1933)



AMS-01 (1998)

Positron fraction  
Fanselow et al (1969)



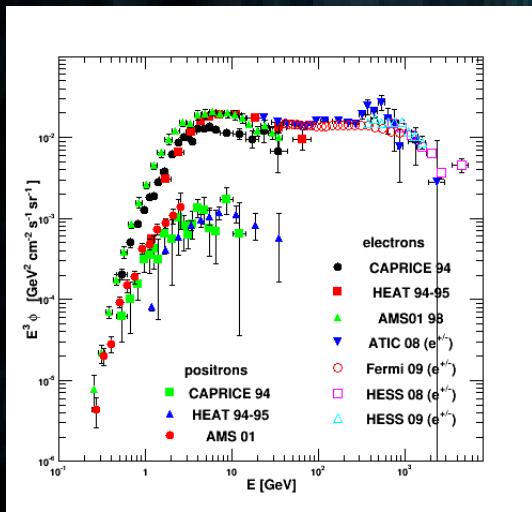
1<sup>st</sup> observation of cosmic ray  
electrons > 0.5 GeV  
Earl (1961): e/p ~ 3%

$$-D\Delta N + \frac{\partial}{\partial r} [b(r)N] = Q(r, t).$$

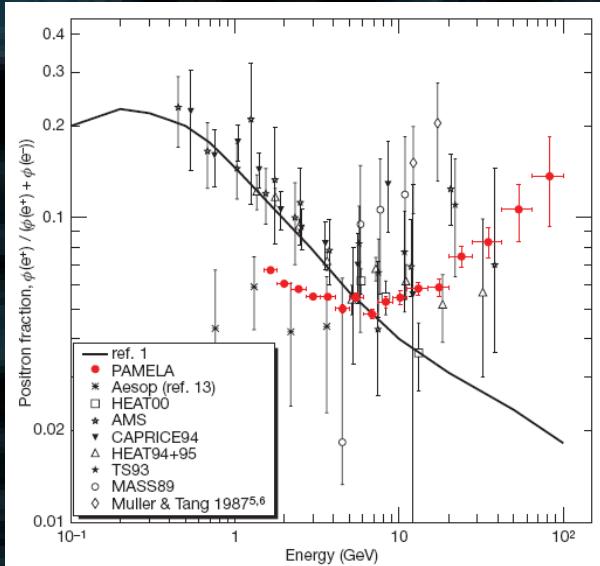
The origin of cosmic rays  
Ginzburg & Sirovatsky (1964)



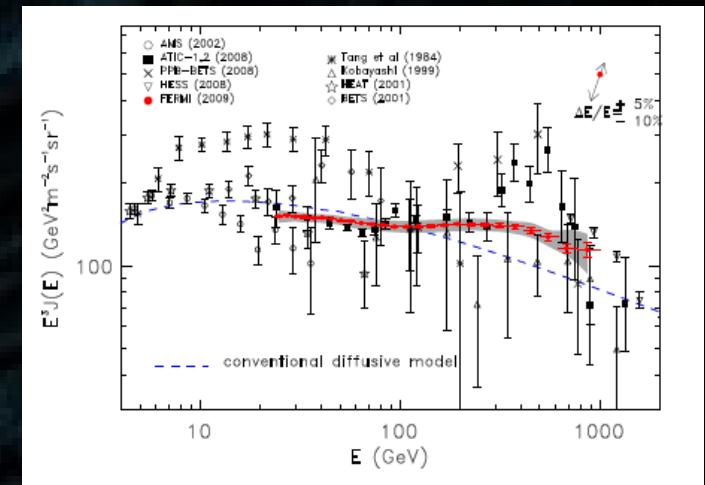
# Current measurements of $e^+$ 's and $e^-$ 's



$e^+$  and  $e^-$   
data compilation



$e^+/(e^+ + e^-)$  PAMELA  
Adriani et al (2009)



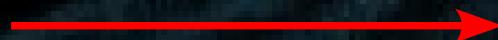
$(e^+ + e^-)$  HESS and Fermi  
Aharonian et al (2009)  
Abdo et al (2009)

Do we understand all of these measurements ?  
(positron excess, spectral features)

# Propagation of Galactic electrons

$$\hat{D}\mathcal{J} = \mathcal{Q}$$

$$D_\mu \mathcal{J}^\mu + D_E \mathcal{J}^E = Q$$



$$\begin{aligned} \partial_t \mathcal{N} &= \mathcal{Q}(\vec{x}, E, t) \\ &+ \vec{\nabla} \left\{ \left( K_x(E) \vec{\nabla} - \vec{V}_c \right) \mathcal{N} \right\} \\ &- \partial_E \left\{ \left( \frac{dE}{dt} - K_E(E) \partial_E \right) \mathcal{N} \right\} \end{aligned}$$

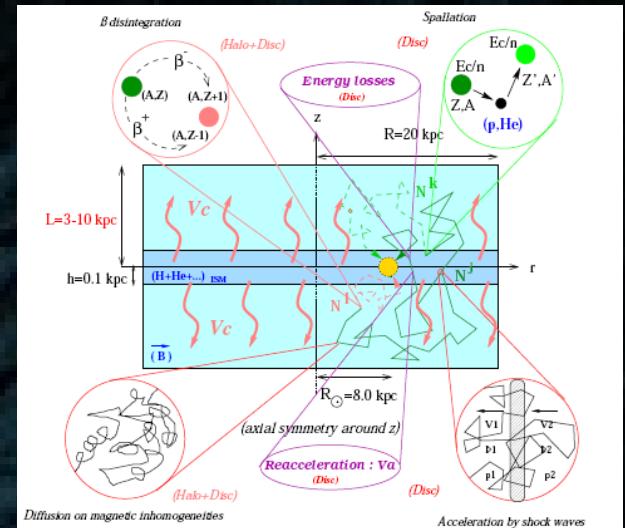
Current conservation  
(continuity equation)

See formalism in:  
Ginzburg & Sirovatskii (1964)  
Berezinskii et al (1990)

Program:

- Solve the equation given boundary conditions
- Constrain the different parameters
- Make predictions, compare with data

Spatial current (diffusion + convection)  
Momentum current (losses + reacceleration)



Credit: Maurin et al (2002)

# *The Green function method*

$$\begin{aligned}\hat{D}\mathcal{J} &= \mathcal{Q} \\ D_\mu \mathcal{J}^\mu + D_E \mathcal{J}^E &= \mathcal{Q}\end{aligned}$$

$$\hat{D}\mathcal{G} = \delta^3(\vec{x} - \vec{x}_s)\delta(E - E_s)\delta(t - t_s)$$

$$\mathcal{J}(\vec{x}, E, t) = \int d^3\vec{x}_s dE_s dt_s \mathcal{G}(\vec{x}, E, t \leftarrow \vec{x}_s, E_s, t_s) \mathcal{Q}(\vec{x}_s, E_s, t_s)$$

Analytical solutions in the following cases for electrons:

- Isotropic diffusion + homogeneous losses + no convection + no reacceleration
- Radial diffusion + convection + homogeneous losses + no reacceleration

# *Solution in an infinite 3D halo (1)*

$$\partial_t \mathcal{N} - K(E) \Delta \mathcal{N} + \partial_E \left\{ \frac{dE}{dt} \mathcal{N} \right\} = \mathcal{Q}$$

**Assumptions: diffusion + energy losses homogeneous and isotropic**

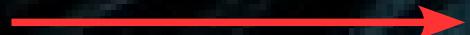
$$\mathcal{N} \equiv dn/dE$$

We are looking for the **particle density** per unit energy at **any place, any energy, any time**.

$$\partial_t \mathcal{N} = 0$$

Assume **steady state** (time fluctuations negligible when averaged over diffusion/energy loss timescales) – reasonable for energies  $\sim 1$ - $100$  GeV, not for  $>100$  GeV.

$$\begin{aligned} K(E) &= K_0 k(E) \\ b(E) &\equiv -dE/dt \\ \psi &\equiv b(E)\mathcal{N} \\ d\tilde{t} &\equiv -\frac{k(E)}{b(E)}dE \end{aligned}$$



$$\frac{\partial \psi}{d\tilde{t}} - K_0 \Delta \psi = \tilde{\mathcal{Q}}$$

**Heat equation !!!!**

# Solution in an infinite 3D halo (2)

$$\frac{\partial \psi}{\partial \tilde{t}} - K_0 \Delta \psi = \tilde{Q}$$

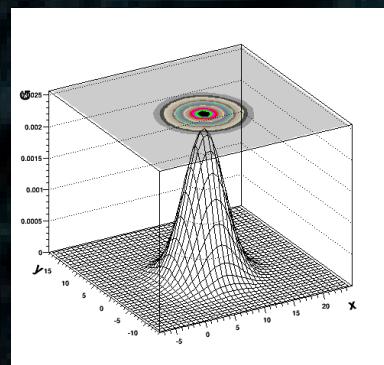
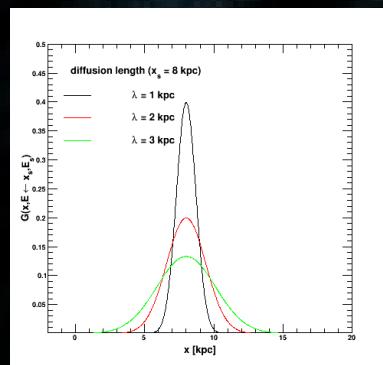


$$\tilde{\mathcal{G}}(\vec{x}, \tilde{t} \leftarrow \vec{x}_s, \tilde{t}_s) = \frac{1}{\pi^{\frac{3}{2}} \lambda^3} \exp \left\{ -\frac{|\vec{x}_s - \vec{x}|^2}{\lambda^2} \right\}$$

**Green function characterized by a propagation scale**

$$\lambda^2 \equiv 4 K_0 (\tilde{t} - \tilde{t}_s) = 4 \int_E^{E_s} dE' \frac{K(E')}{b(E')}$$

**Propagation scale set by pseudo-time (energy)**



**The electron propagator is a Gaussian in space**

$$\begin{aligned} \psi(\vec{x}, \tilde{t}) &= \int_{-\infty}^{t_0} d\tilde{t}_s \int d^3 \vec{x}_s \tilde{\mathcal{G}}(\vec{x}, \tilde{t} \leftarrow \vec{x}_s, \tilde{t}_s) \tilde{Q}(\vec{x}_s, \tilde{t}_s) \\ \Leftrightarrow \mathcal{N}(\vec{x}, E) &= \int_E^\infty dE_s \int d^3 \vec{x}_s \mathcal{G}(\vec{x}, E \leftarrow \vec{x}_s, E_s) Q(\vec{x}_s, E_s) \end{aligned}$$

$$\mathcal{G}(\vec{x}, E \leftarrow \vec{x}_s, E_s) = \frac{1}{\pi^{\frac{3}{2}} \lambda^3 b(E)} \exp \left\{ -\frac{|\vec{x}_s - \vec{x}|^2}{\lambda^2} \right\}$$

$$\frac{d\phi}{dE}(\vec{x}, E) = \frac{\beta c}{4\pi} \mathcal{N}(\vec{x}, E)$$

The flux is the quantity to be compared with the data

# *Boundary conditions*

The diffusion zone has a finite size: flat cylinder of radius  $R \sim 20$  kpc and half-height  $L \sim 1-10$  kpc.

Let us assume that the observer is on Earth, and that  $\mathbf{R} \cdot \mathbf{r} < L$ .

If  $\lambda \ll L$ , the 3D solution is valid.

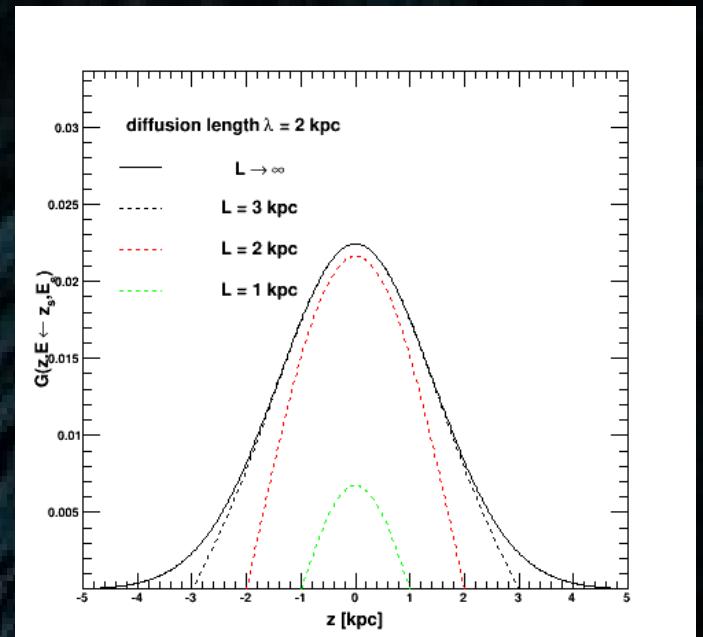
If  $\lambda \sim L$ , then one has to account for the vertical boundary condition:  $N(|z|=L) = 0$ .

Different methods exist: image method, expansion in terms of Helmholtz eigen-functions, etc.

Example of the image method

$$\tilde{V}(z, \tilde{t} \leftarrow z_S, \tilde{t}_S) = \sum_{n=-\infty}^{+\infty} (-1)^n \mathcal{V}_{1D}(z, \tilde{t} \leftarrow z_n, \tilde{t}_S)$$

$$z_n = 2Ln + (-1)^n z_S$$



# Energy losses

Electrons lose their energy through electromagnetic interactions  
(I) with the interstellar medium (ISM)  
(ii) with the interstellar radiation fields (ISRF) and the magnetic fields  
(see Blumenthal & Gould, 1970)

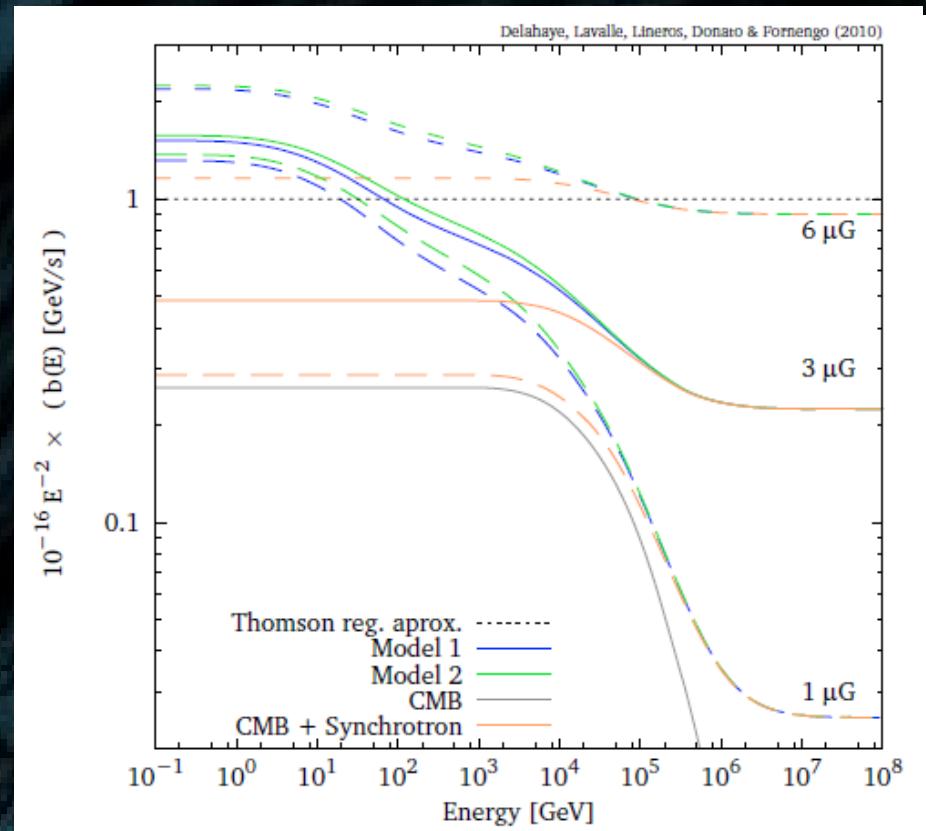
(i) Interactions with the ISM (in the disk):  
Bremsstrahlung (braking radiation),  
ionization

$$\begin{aligned} b_{\text{ion}}(E) &\propto n_{\text{gas}} \ln(E) \\ b_{\text{brem}}(E) &\propto n_{\text{gas}} E \ln(E) \end{aligned}$$

(ii) Interactions with the ISRF (including CMB) and magnetic fields: (inverse) Compton processes

$$b_{\text{sync/ic}} \propto U_{\text{mag/rad}} E^2$$

**Caveats:** .... CMB anywhere, but ISRF concentrated in the disk ... Thomson regime only valid for  $\gamma_e E_{\text{ph}} < m$  ...



# Translate losses into propagation scale

Transport mostly set by **spatial diffusion** and **energy losses**

$$K(E) = K_0 k(E) = K_0 \beta \left( \frac{\mathcal{R}}{1 \text{ GeV}} \right)^{\delta}$$

$$b(E) \equiv -dE/dt \approx \frac{E_0}{\tau_0} \left( \frac{E}{E_0} \right)^{\alpha}$$

**Propagation scale:** a very useful quantity

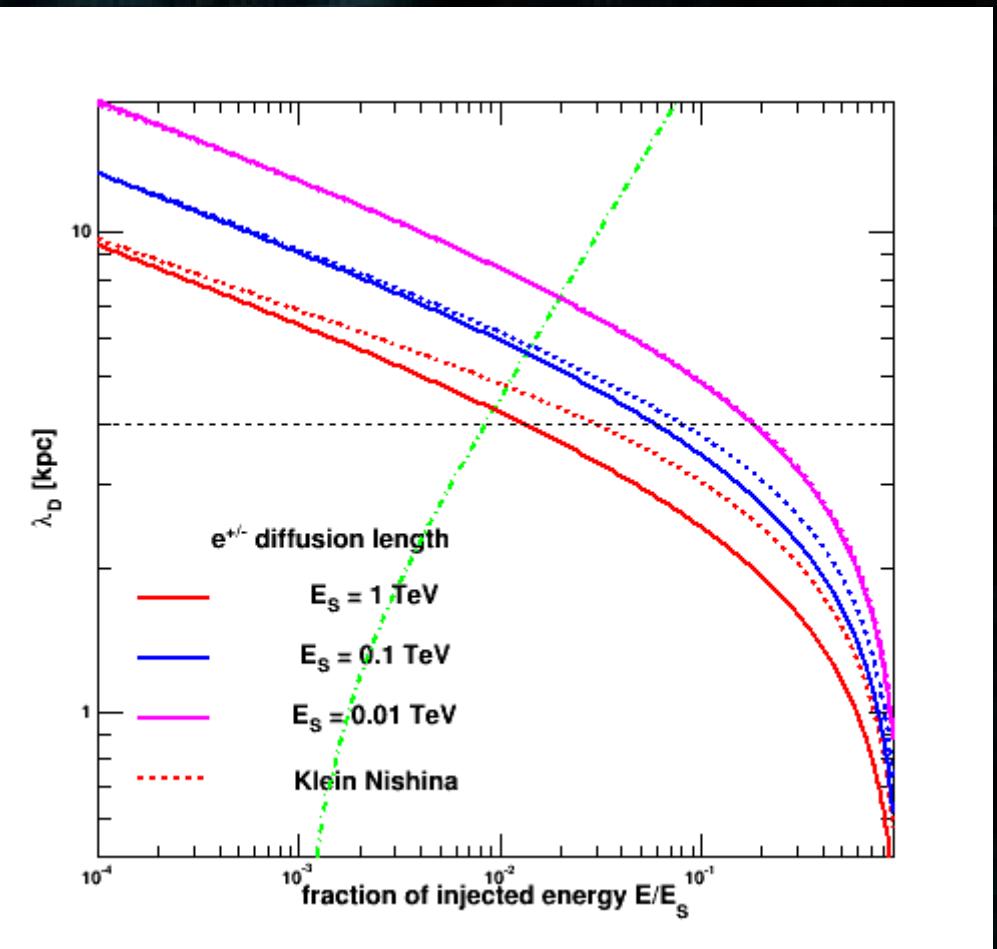
$$\lambda^2 \equiv 4 \int_E^{E_s} dE' \frac{K(E')}{b(E')}$$

$$= \frac{4 K_0 \tau_0}{1 + \delta - \alpha} \left( \frac{\epsilon}{1 \text{ GeV}} \right)^{1 + \delta - \alpha} \Big|_E^{E_s}$$

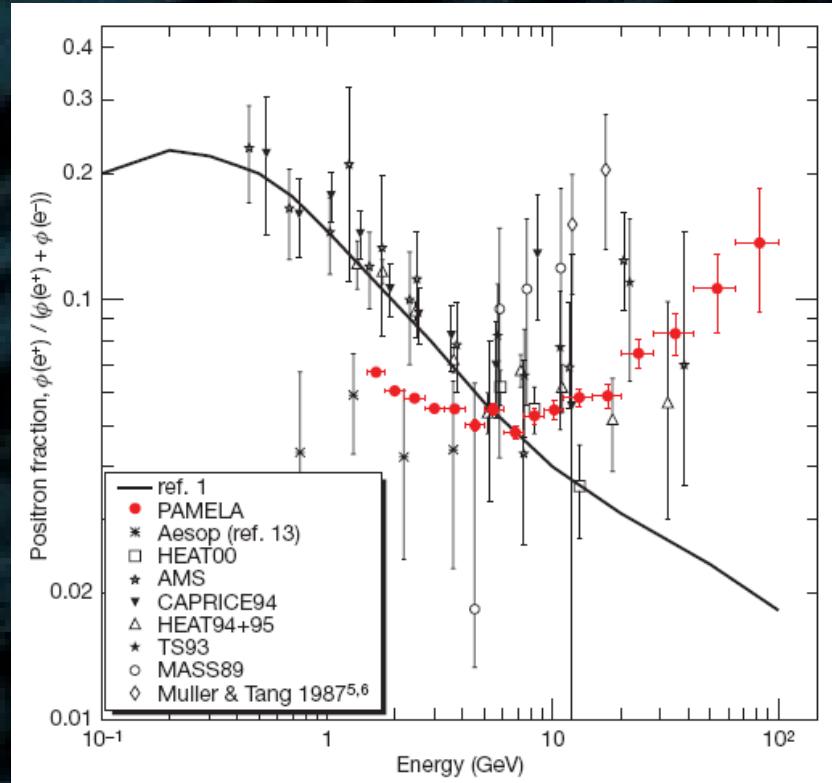
**Electron horizon limited to a few kpc**

$$K_0 = 0.012 \text{ kpc}^2/\text{Myr}; \tau = 10^{16} \text{ s}; \delta = 0.7$$

$$\lambda(E = 1 \text{ GeV} \leftarrow E_s \gg E) \approx 6 \text{ kpc}$$



# Can secondary $e^+$ 's explain the PAMELA data ?



$e^+/(e^+ + e^-)$  PAMELA  
Adriani et al (2009)

Is there a standard model for secondary  $e^+$ 's ?

# *Short recipe for secondaries*

Proton and alpha fluxes

ISM gas distribution

The source term

Inclusive nuclear cross section  
 $p+p \rightarrow e^+ + X$

Propagation  
from  $(x_s, E_s)$  to  $(x, E)$

ANTIMATTER

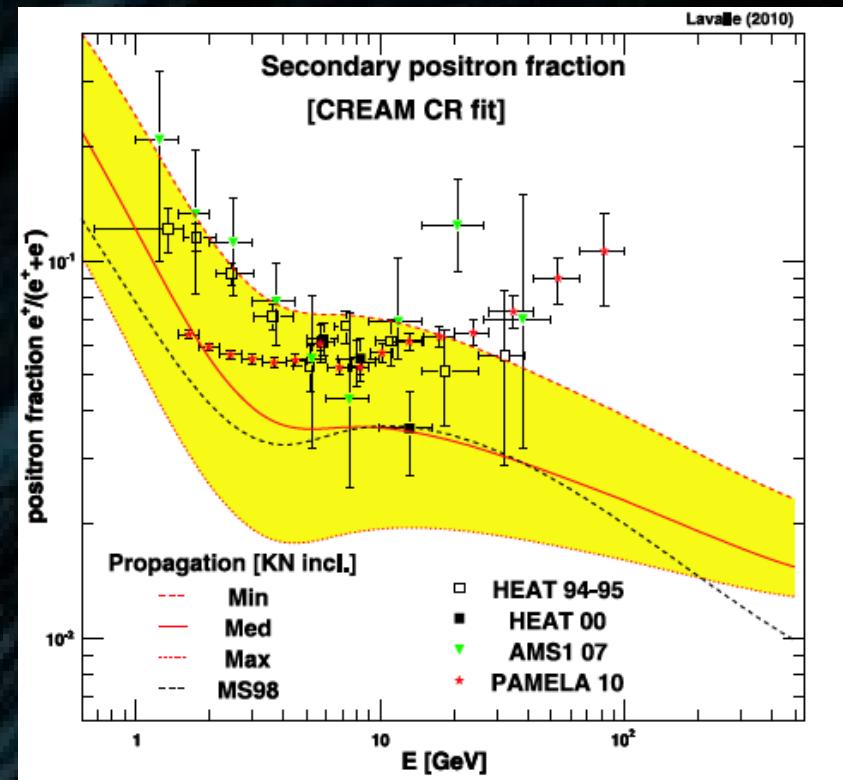
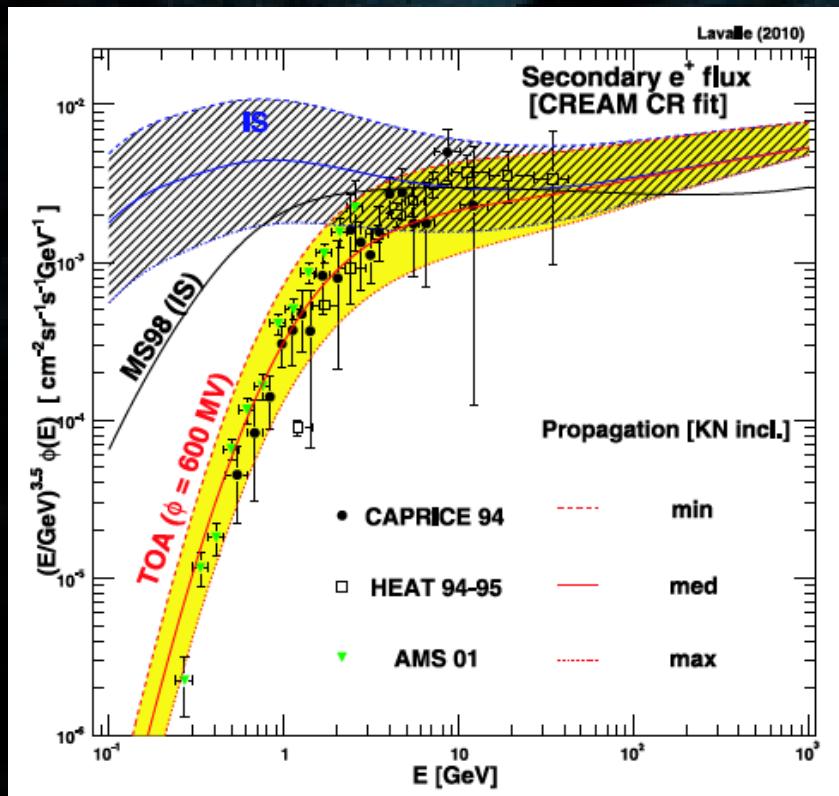
10

Flux at the Earth

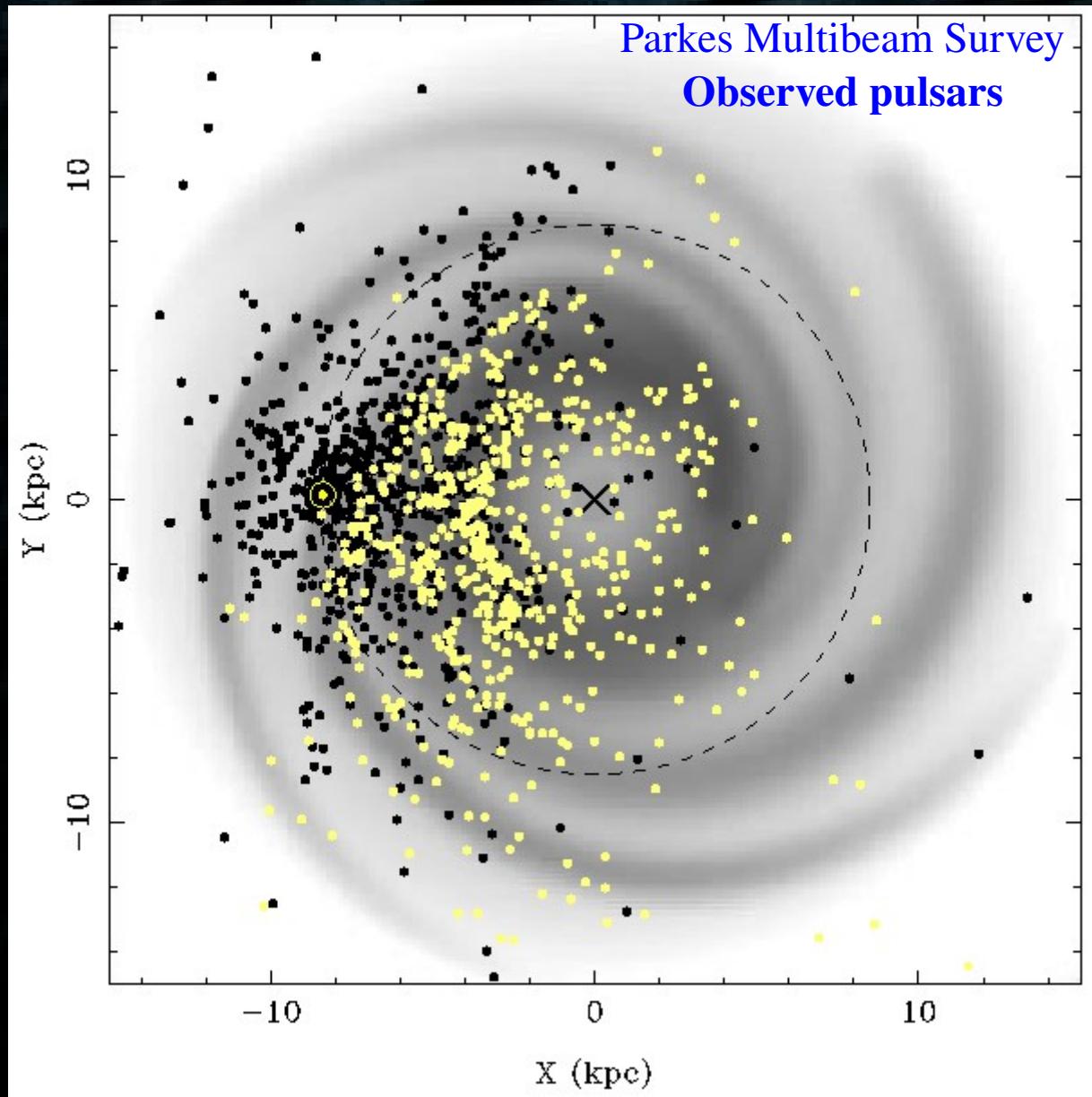
Each box contains  
uncertainties !!!

# *Short recipe for secondaries*

Secondaries with theoretical uncertainties  
Delahaye et al 09, Lavalle 11



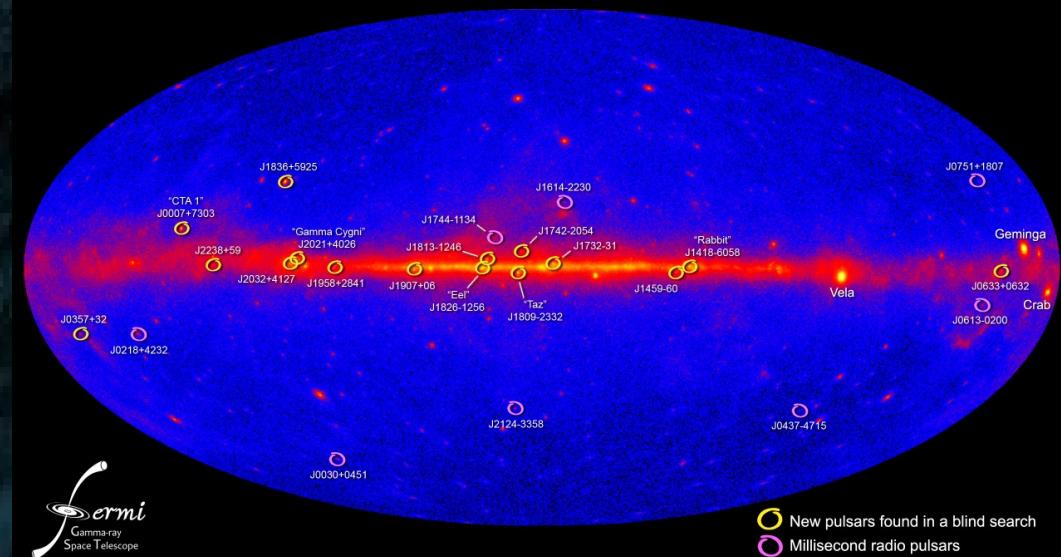
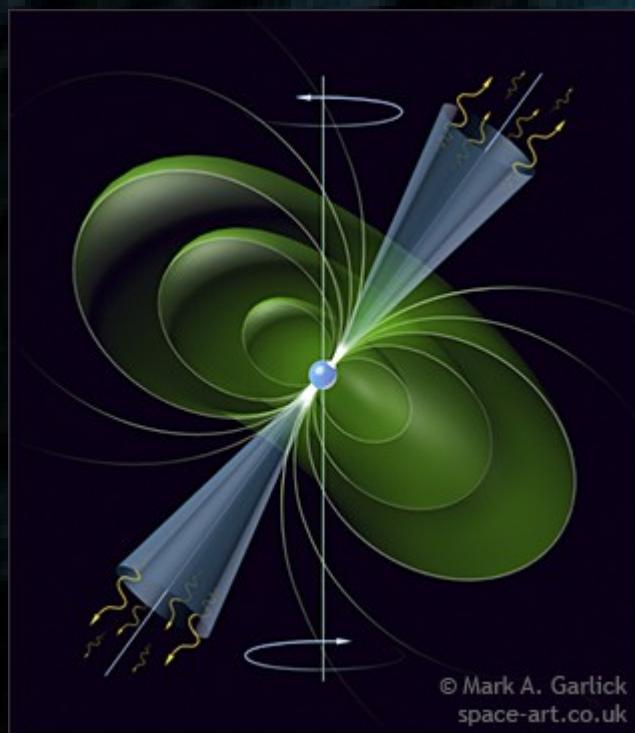
# *Galactic sources of cosmic rays: supernova outcomes*



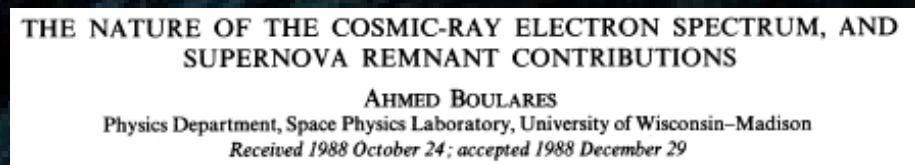
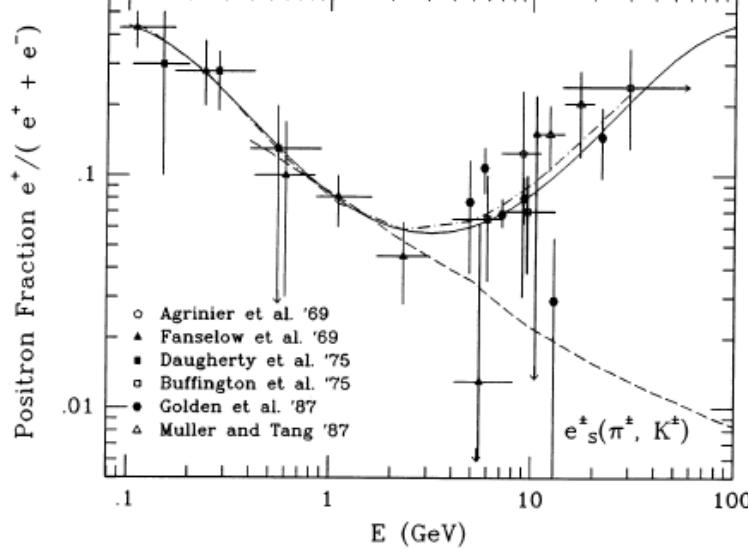
- CRs accelerated by SNR and pulsar shocks (observation + theory)
- SN explosion rate  $\sim 1/\text{century}$
- $\sim 1900$  pulsars and  $\sim 280$  SNRs observed (ATNF and Green catalogs)

Sources of positrons ?

# *“Standard” positron sources ? ... Pulsars !*

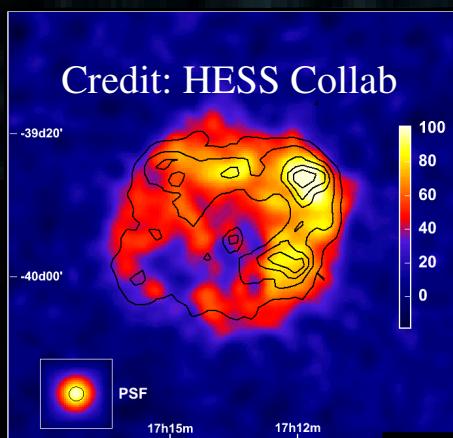
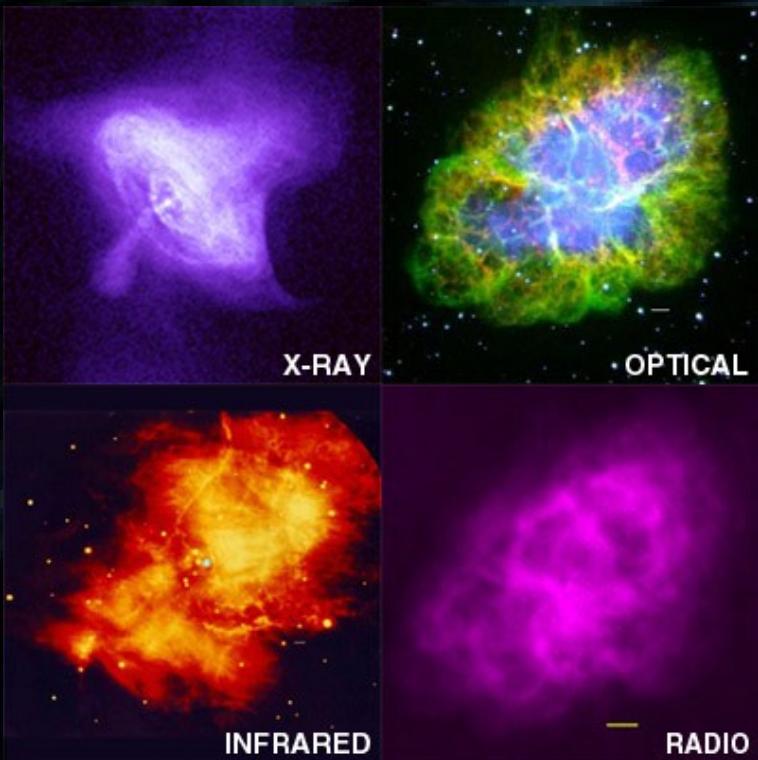


A Population of Gamma-Ray Millisecond Pulsars  
Seen with the Fermi Large Area Telescope  
A. A. Abdo, et al.  
*Science* 325, 848 (2009);  
DOI: 10.1126/science.1176113



radio,  $\gamma$ -rays) suggest this possibility. In fact, if the recent  $e^+/(e^+ + e^-)$  measurements are reliable, this will definitely require a pulsar source, because no other nearby conventional astrophysical sources (within 100–500 pc) can generate both  $e^-$  and  $e^+$  at high energies (of course, dark matter annihilation may be important if it exists).

# *Towards a consistent picture*



## **Include all primaries:**

- SNRs accelerate electrons mostly
- Pulsars accelerate electrons + positrons
- Each pulsar must be paired with a SNR
- Many pulsars are not observable

## **Low energy electrons (< 20 GeV):**

- Contribution of distant sources (collective effects) : average properties

## **High energy electrons (> 20 GeV)**

- Consider local sources: large fluctuations expected
- Use multi-wavelength observational constraints

(see Shen 70, Kobayashi et al 04)

## Issues

- Modeling of local sources (many degeneracies)
- More general: release of CRs in the ISM

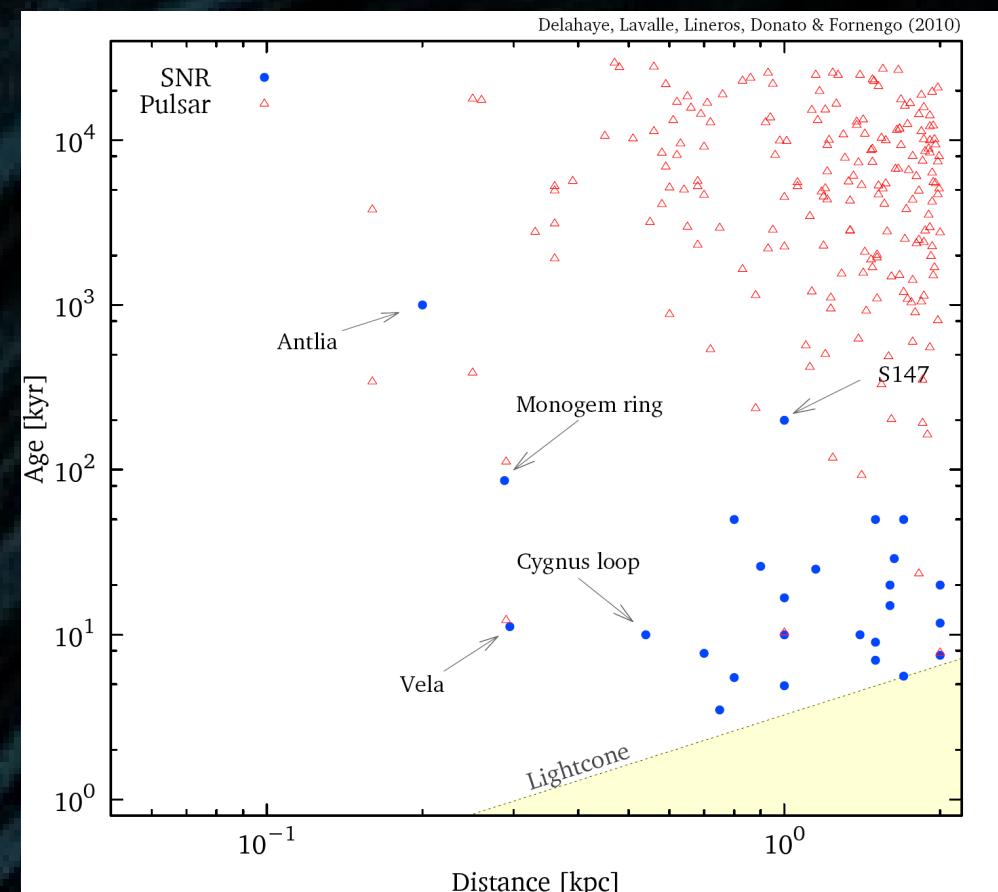
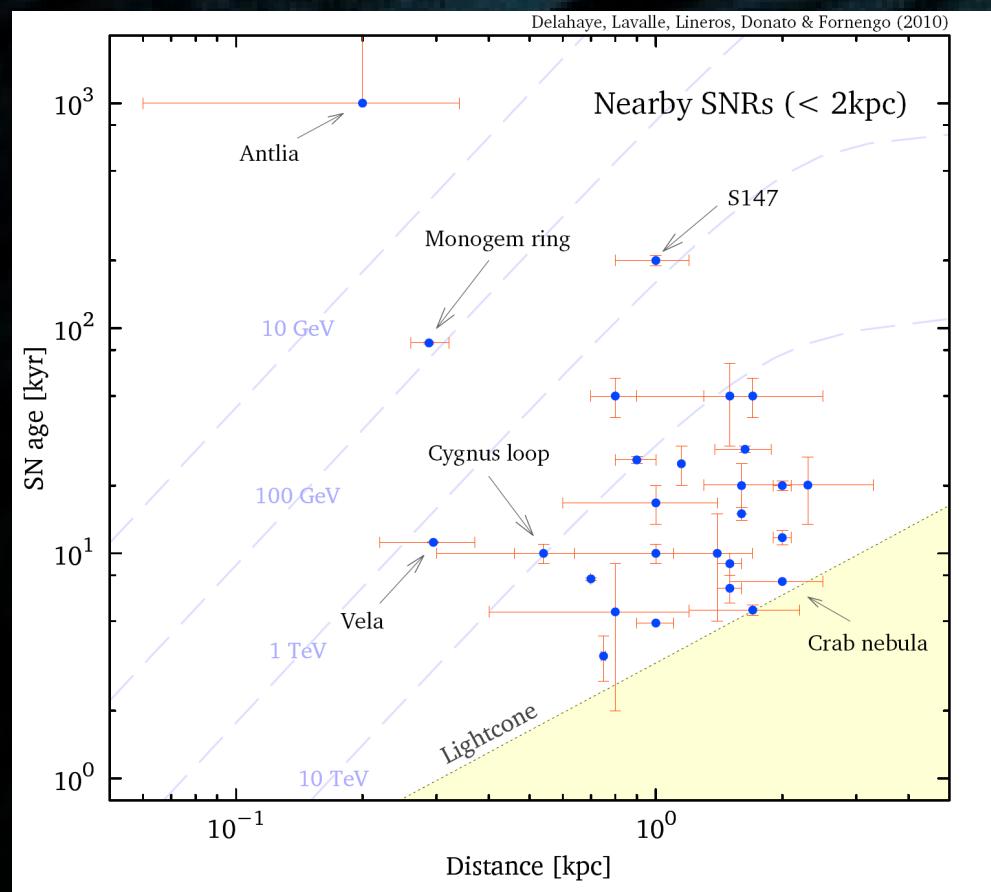
**Standard paradigm, but not standard model!**

# *Deal with the complexity of Nature: Include all known local sources self-consistently*

**27 obs SNRs within 2 kpc**

**Delahaye et al 10  
arXiv:1002.1910**

**~200 obs pulsars within 2 kpc**



SNRs contribute to  $e^-$ , pulsars inject  $e^+e^-$  pairs ...

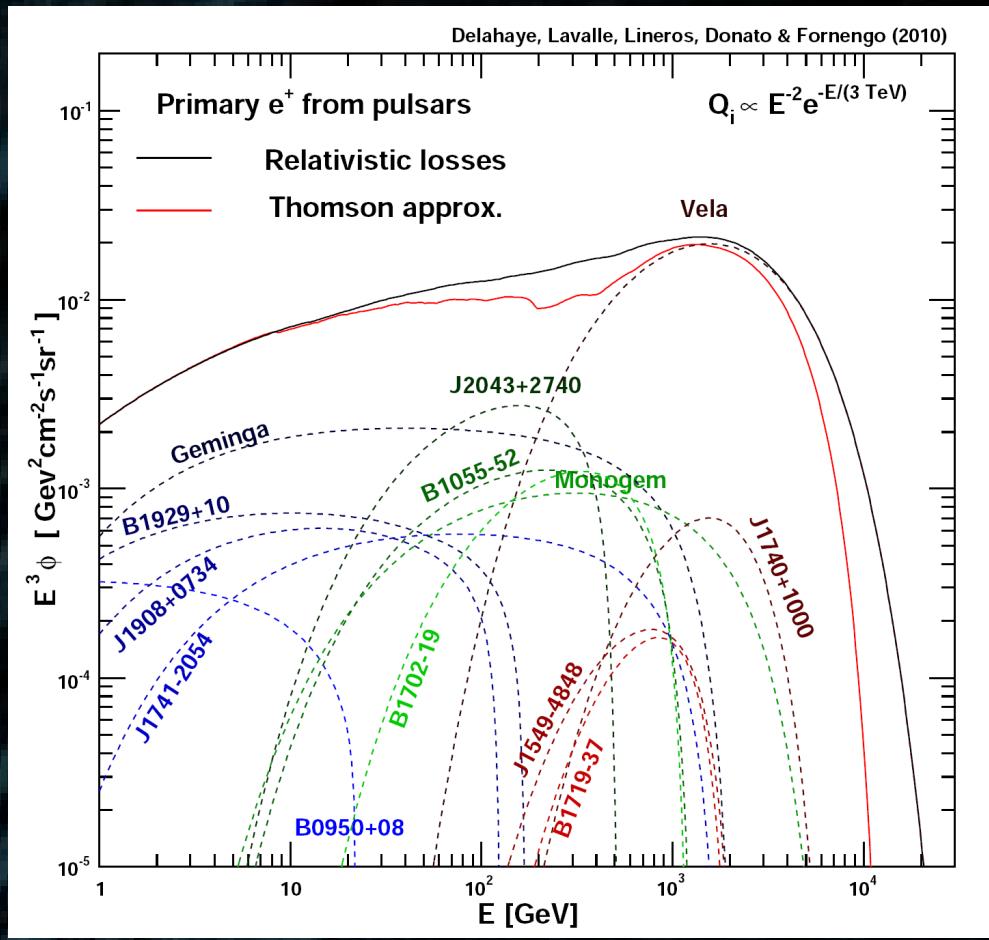
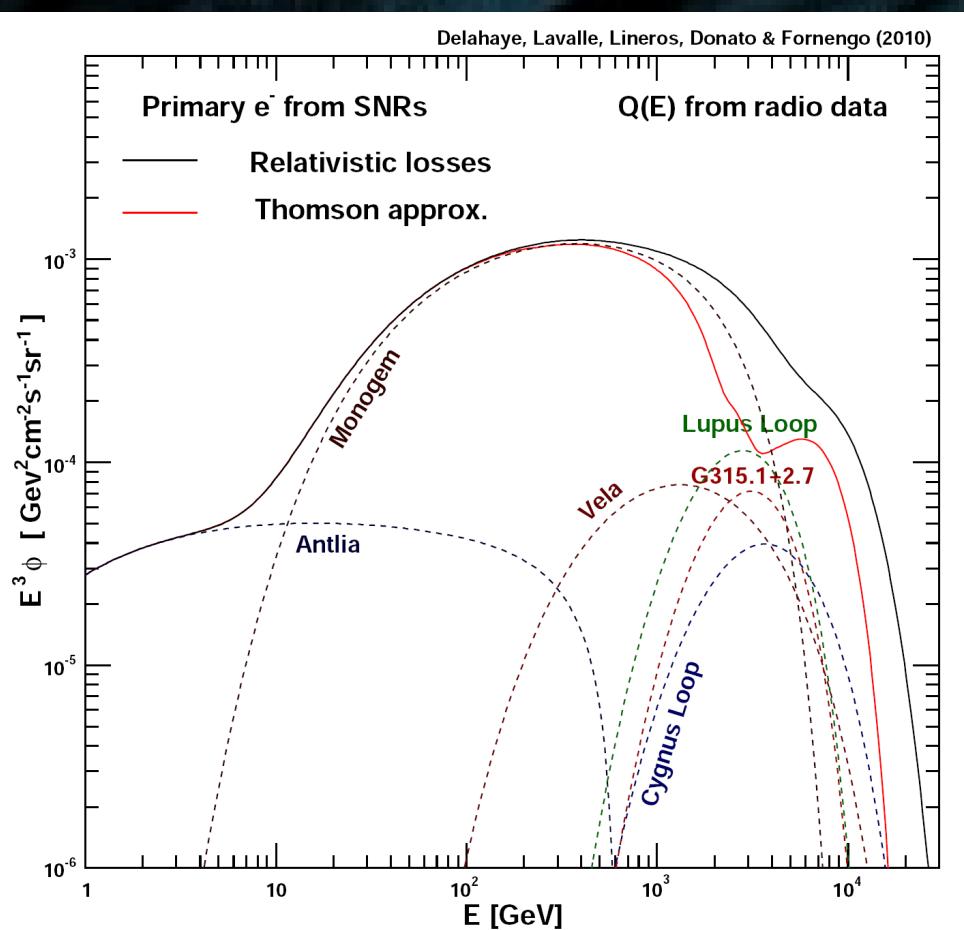
... but each pulsar should be associated with a SNR => Add missing SNRs !

*Deal with the complexity of Nature:  
Include all known local sources self-consistently*

**27 obs SNRs within 2 kpc**

**Delahaye et al 10  
arXiv:1002.1910**

**~200 obs pulsars within 2 kpc**

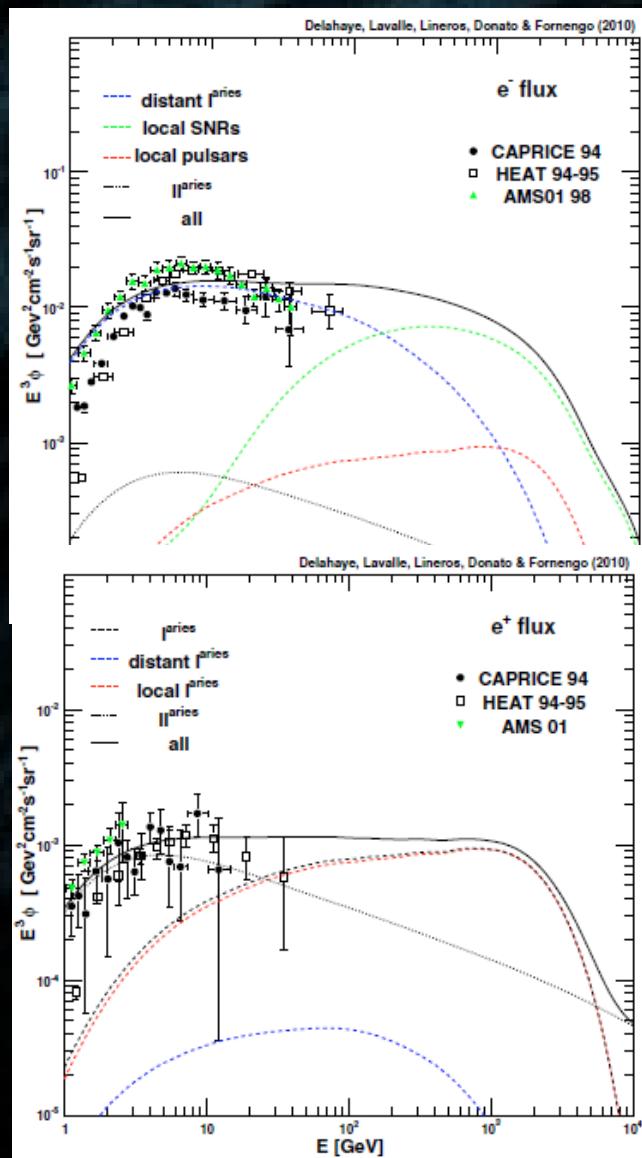


SNRs contribute to  $e^-$ , pulsars inject  $e^+e^-$  pairs ...

... but each pulsar should be associated with a SNR => Add missing SNRs !

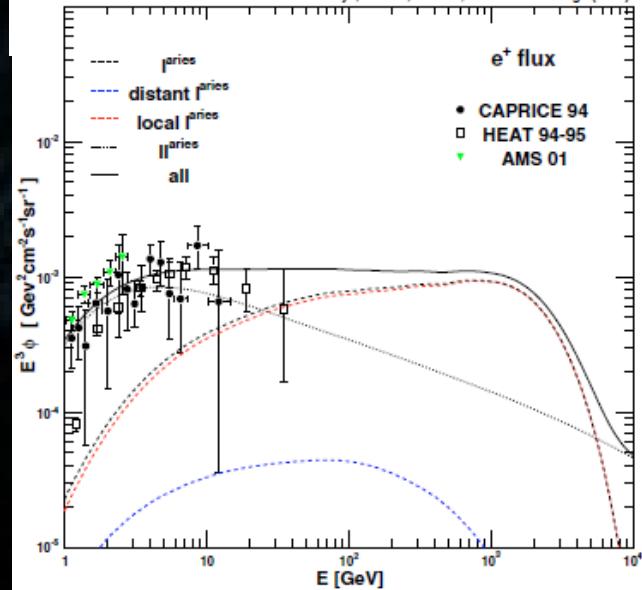
*No choice, Nature is observed to be complex:  
Include all known local sources self-consistently*

electrons

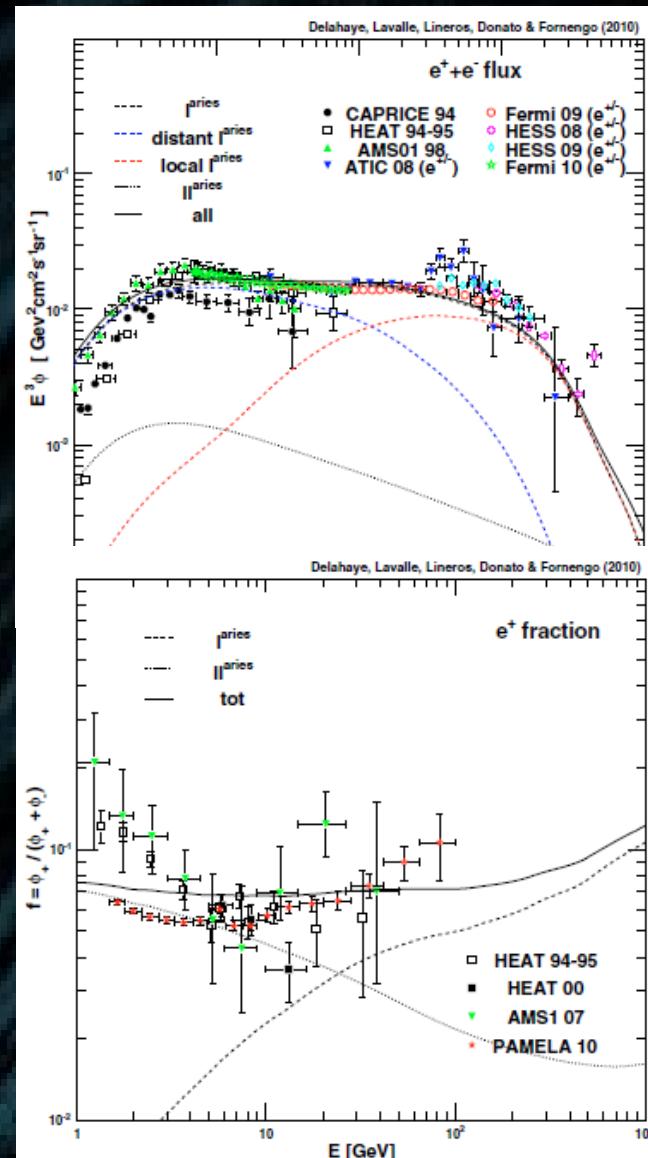


Delahaye et al 2010

positrons



electrons  
+  
positrons



positron  
fraction

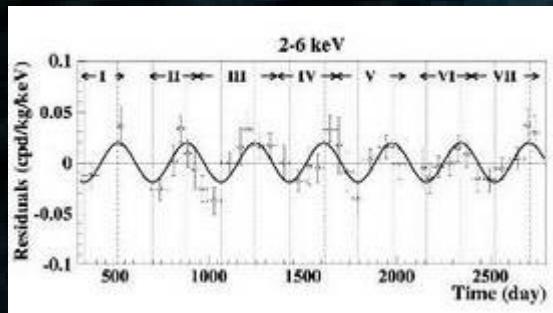
Standard astrophysical sources make it!

# *Cosmic-ray electrons and positrons: summary*

- Electron transport very sensitive to ISRF and magnetic field.
- High-energy predictions require the accurate modeling of local sources, both SNRs and pulsars: some hope to test diffusion locally?
- Large uncertainties for local predictions, but standard astrophysics makes it (no exotic physics needed).
- Much larger uncertainties expected for eg the Galactic center.
- No standard model so far (Galprop is not a “standard model”).
- Multiwavelength analyses useful, though complex (magnetic field, ISRF, source distribution): from Planck to Fermi.

*Dark Matter searches in the sky*

# Hints ?

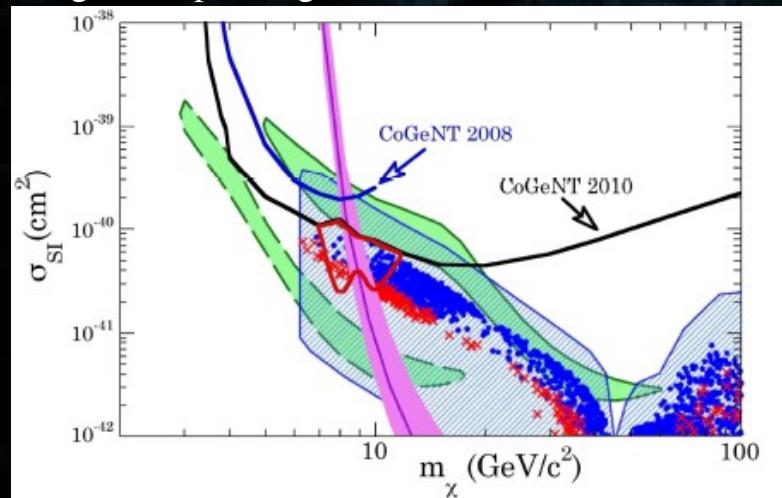


## Direct detection:

DAMA oscillation (Bernabei et al), large significance.

Oscillation not yet detected by others.

Few events in other experiments (CDMS and Cogent), though with poor significance ... lot of excitement ;-)



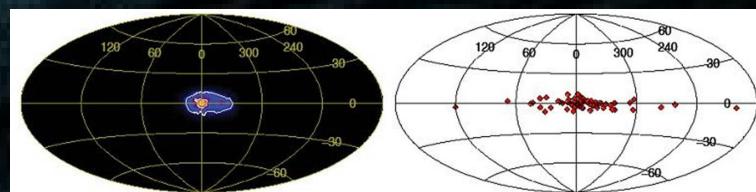
Aaltest et al 10 (Cogent)

see also Ahmed et al 09 (CDMS)

Theoretical prediction: eg Bottino et al 10, Ling et al 10

Interpretation issues: Kopp et al 10

**[~10 GeV mass]**

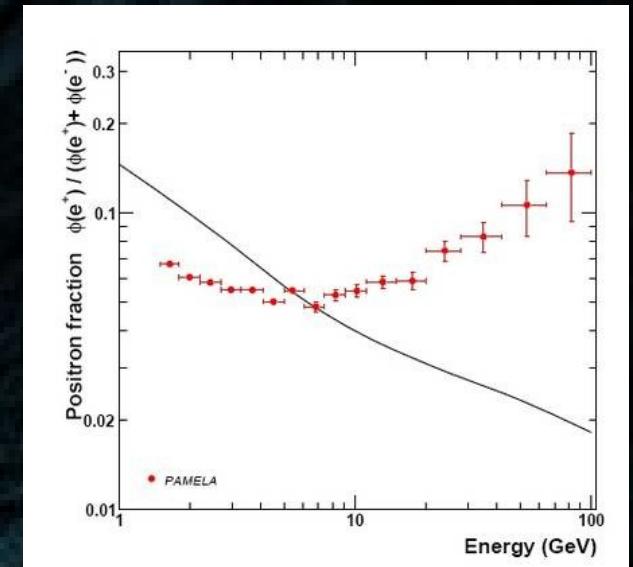


511 keV emission from the GC  
Knodlseder et al 05, Weidenspointner et al 08

Spatial association with X-binaries, but positron production rate and transport issues.

MeV dark matter ? Boehm et al 04

**[~1 MeV mass]**

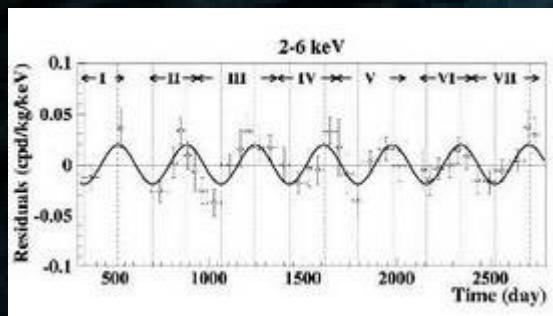


Local positron excess measured by PAMELA  
(Adriani et al 08)

Astrophysical sources or dark matter ???

**[> 100 GeV mass]**

# Hints ?

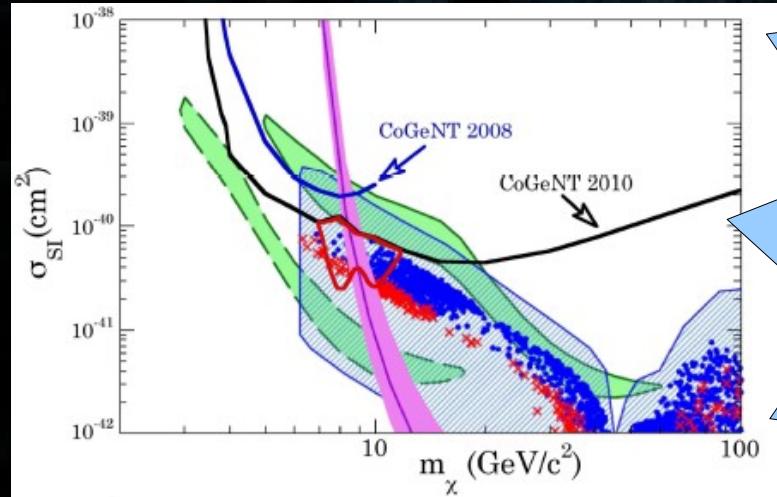


## Direct detection:

DAMA oscillation (Bernabei et al), large significance.

Oscillation not yet detected by others.

Few events in other experiments (CDMS and Cogent), though with poor significance ... lot of excitement ;-)



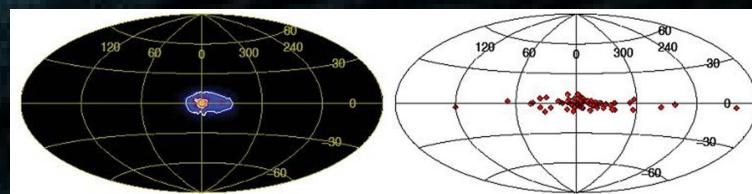
Aaltest et al 10 (Cogent)

see also Ahmed et al 09 (CDMS)

Theoretical prediction: eg Bottino et al 10, Ling et al 10

Interpretation issues: Kopp et al 10

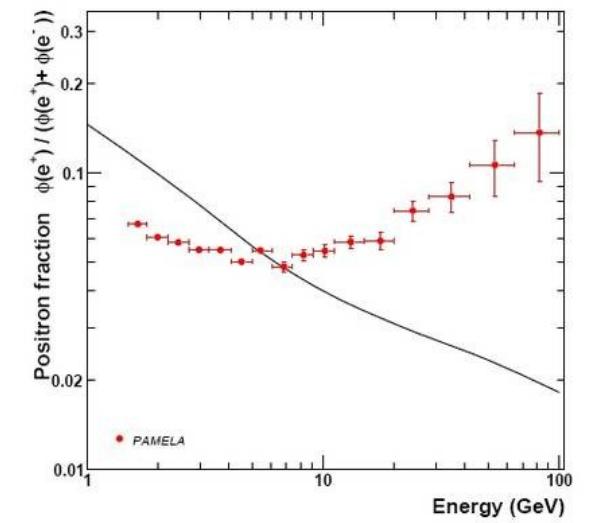
**[~10 GeV mass]**



511 keV emission from the GC  
Knodlseder et al 05, Weidenspointner et al 08

Spatial association with X-binaries, but positron production rate and transport issues.

~1 MeV dark matter ? Boehm et al 04  
**[~1 MeV mass]**



Local positron excess measured by PAMELA  
(Adriani et al 08)

Astrophysical sources or dark matter ???

**[> 100 GeV mass]**

# Antimatter signals

VOLUME 53, NUMBER 6

PHYSICAL REVIEW LETTERS

6 AUGUST 1984

## Cosmic-Ray Antiprotons as a Probe of a Photino-Dominated Universe

Joseph Silk

Astronomy Department, University of California, Berkeley, California 94720, and Institute for Theoretical Physics,  
University of California, Santa Barbara, California 93106

and

Mark Srednicki

Physics Department, University of California, Santa Barbara, California 93106

(Received 8 June 1984)

$\bar{p}, \bar{D} \& e^+$

$$\phi(E) \propto \langle \rho^2 \rangle_{V_{\text{diff}}}$$



$\gamma \& \nu's$

$$\phi(E, \psi) \propto \left\langle \int dl \rho^2 \right\rangle_{\text{res}}$$

Courtesy P. Salati

Main arguments:

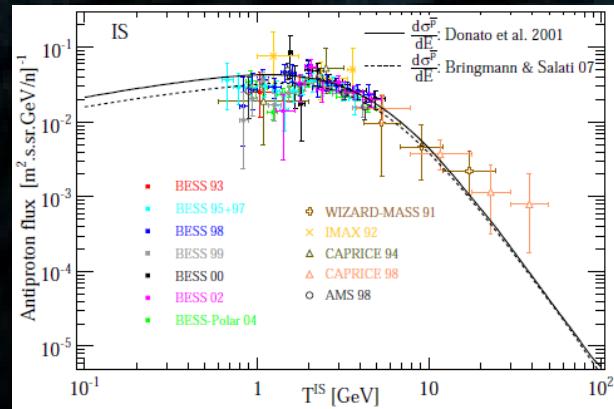
- DM annihilation provides as many particles as antiparticles
- Antimatter cosmic rays are rare because secondary products
- DM-induced antimatter CRs may have specific spectral properties

But:

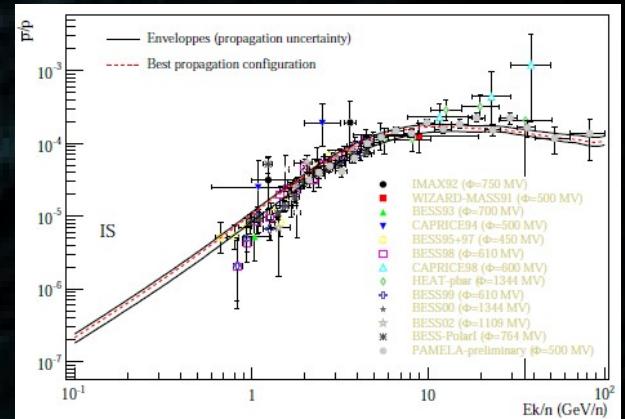
- We must control the backgrounds
- Antiprotons are secondaries, what about positrons ?
- Do the natural DM particle models provide clean signatures?

# Secondary back grounds: CRs interaction with ISM

→ Don't forget theoretical uncertainties!

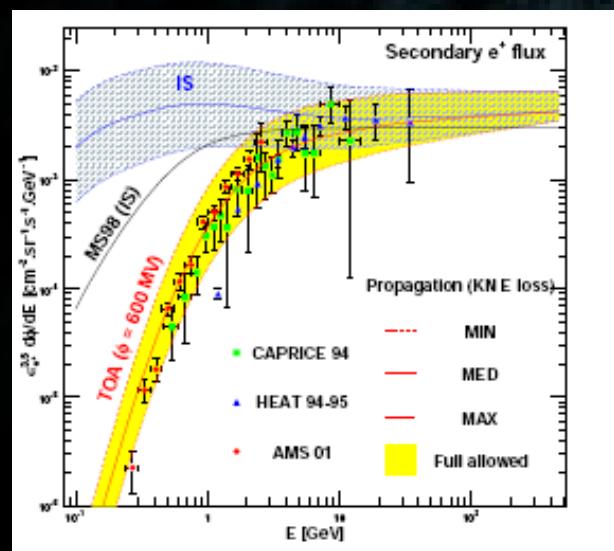


Flux at the Earth

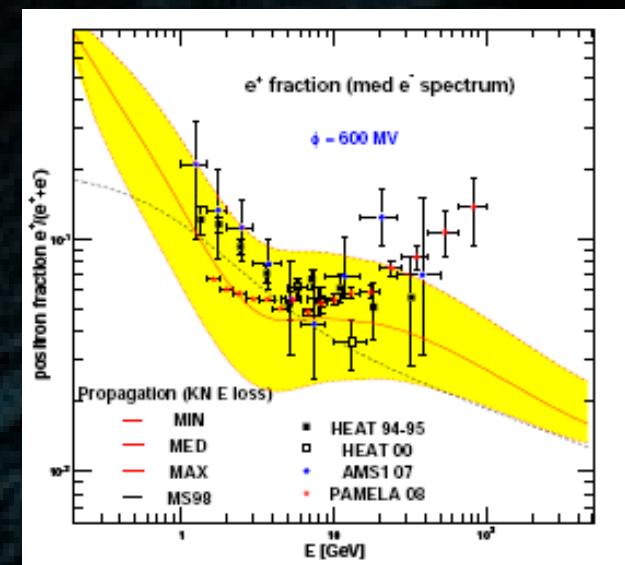


Antiprotons  
Donato et al 01, 09  
Bringmann & Salati 07

Secondary bg:  
antiprotons fit,  
positrons do not

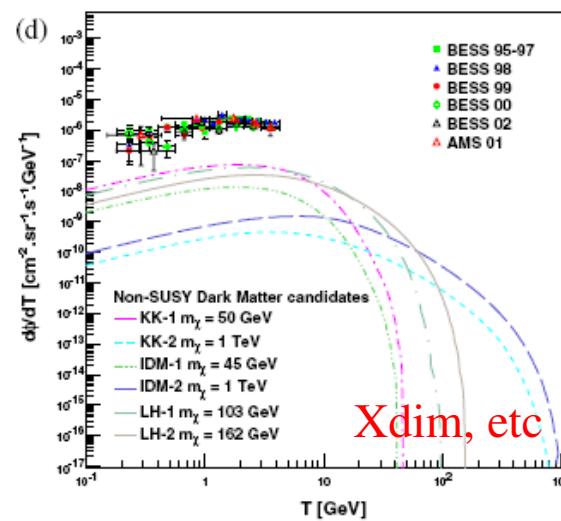
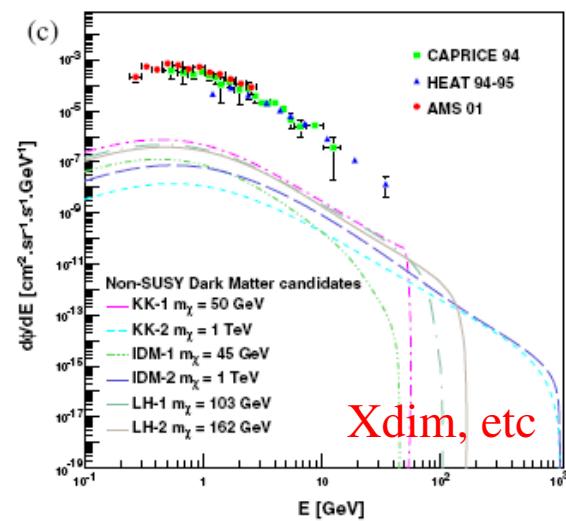
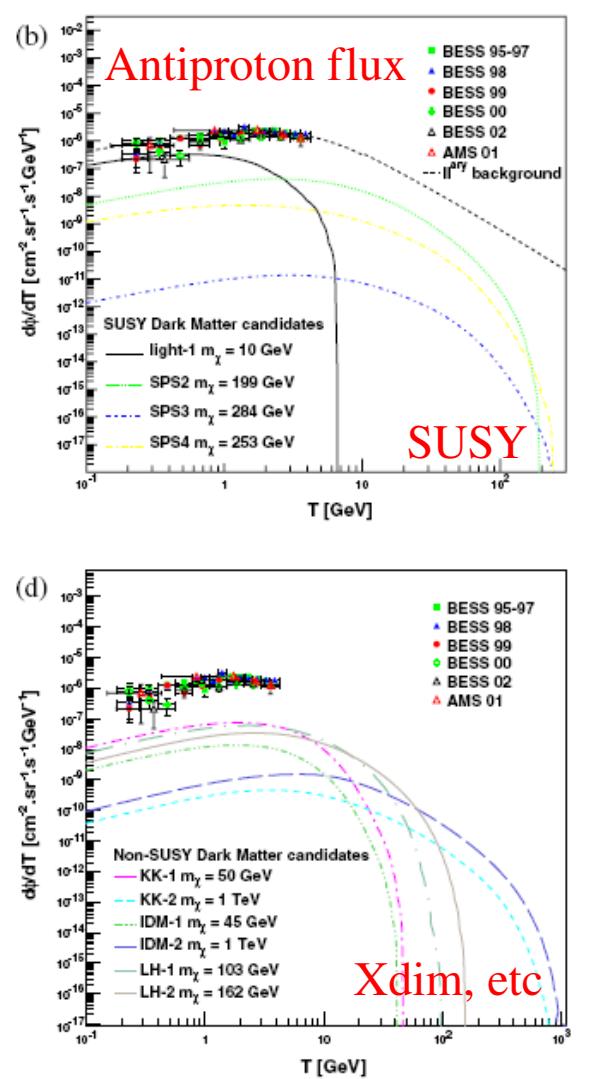
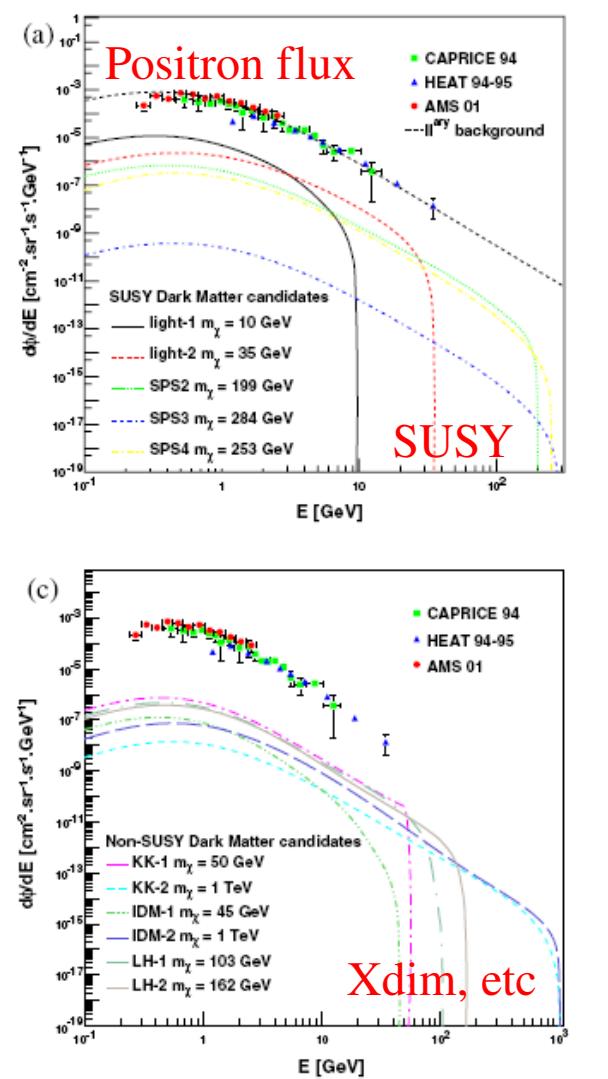


Positrons  
Moskalenko & Strong 98  
Delahaye et al 09  
Lavalle 10



# Dark Matter annihilation: generic predictions for positrons

Lavalle, Nezri, Ling et al (2008) – using a Horizon MW-like Galaxy



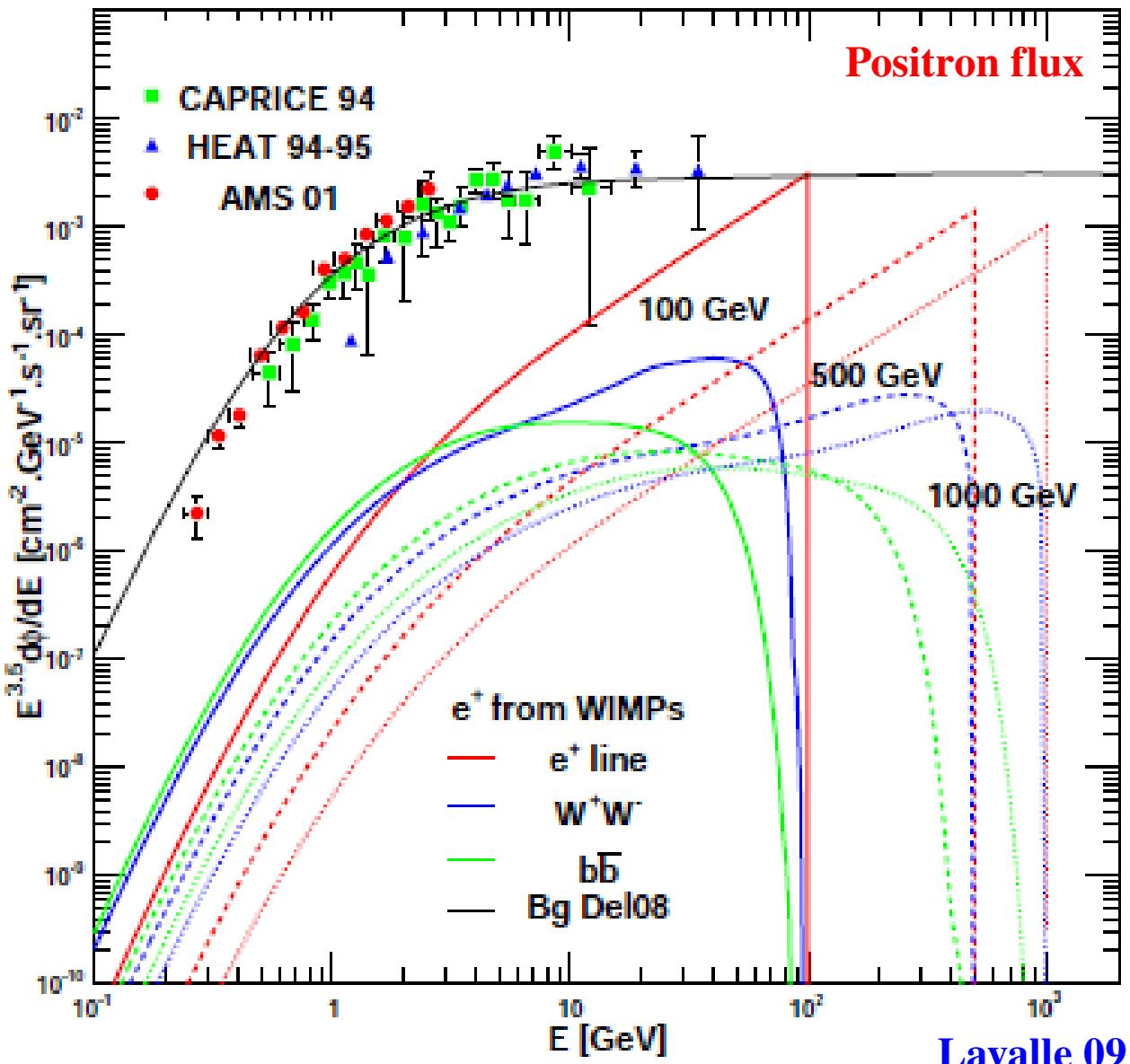
**Susy candidates:**  
**positron (left) – antiproton (right)**

(see  $e^+$  study in eg Baltz & Edsjo 98  
(pbars in eg Chardonnet et al 96,  
Bottino et al 98)

**Non-Susy candidates (KK, etc):**  
**positron (left) – antiproton (right)**

Most motivated thermal models (**SUSY**, X-dim, LH, IDM) are  
**usually not predicted observable** in the antimatter spectrum.

# Dark Matter annihilation: generic predictions for positrons



Boost to get  $\sim 5 \times \phi_{\text{bg}}$  at  $\sim 100 \text{ GeV}$ :

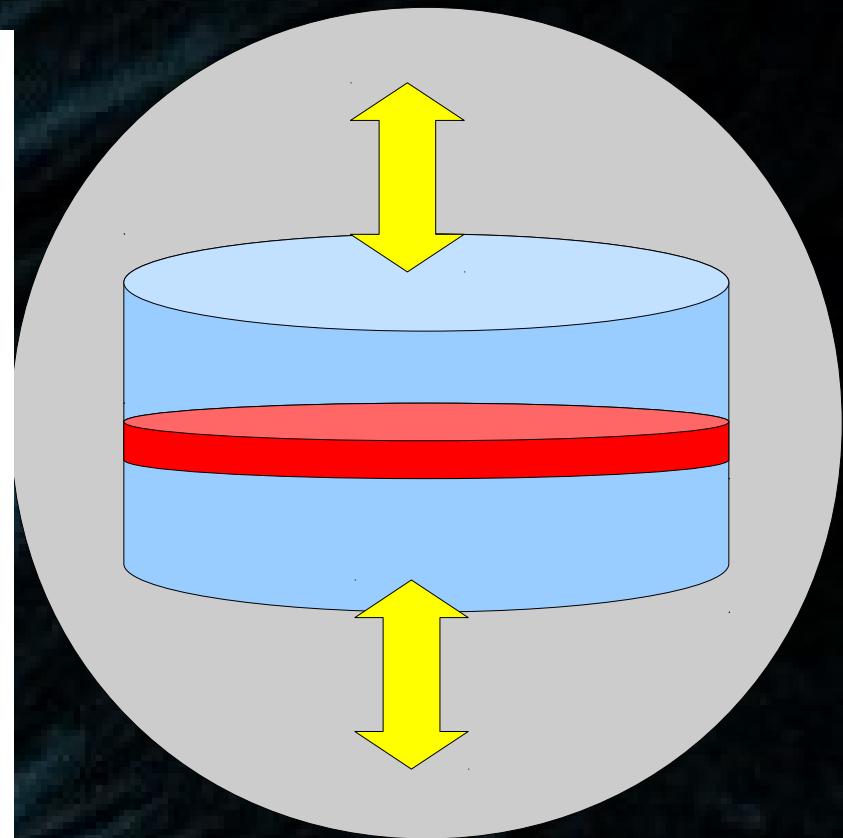
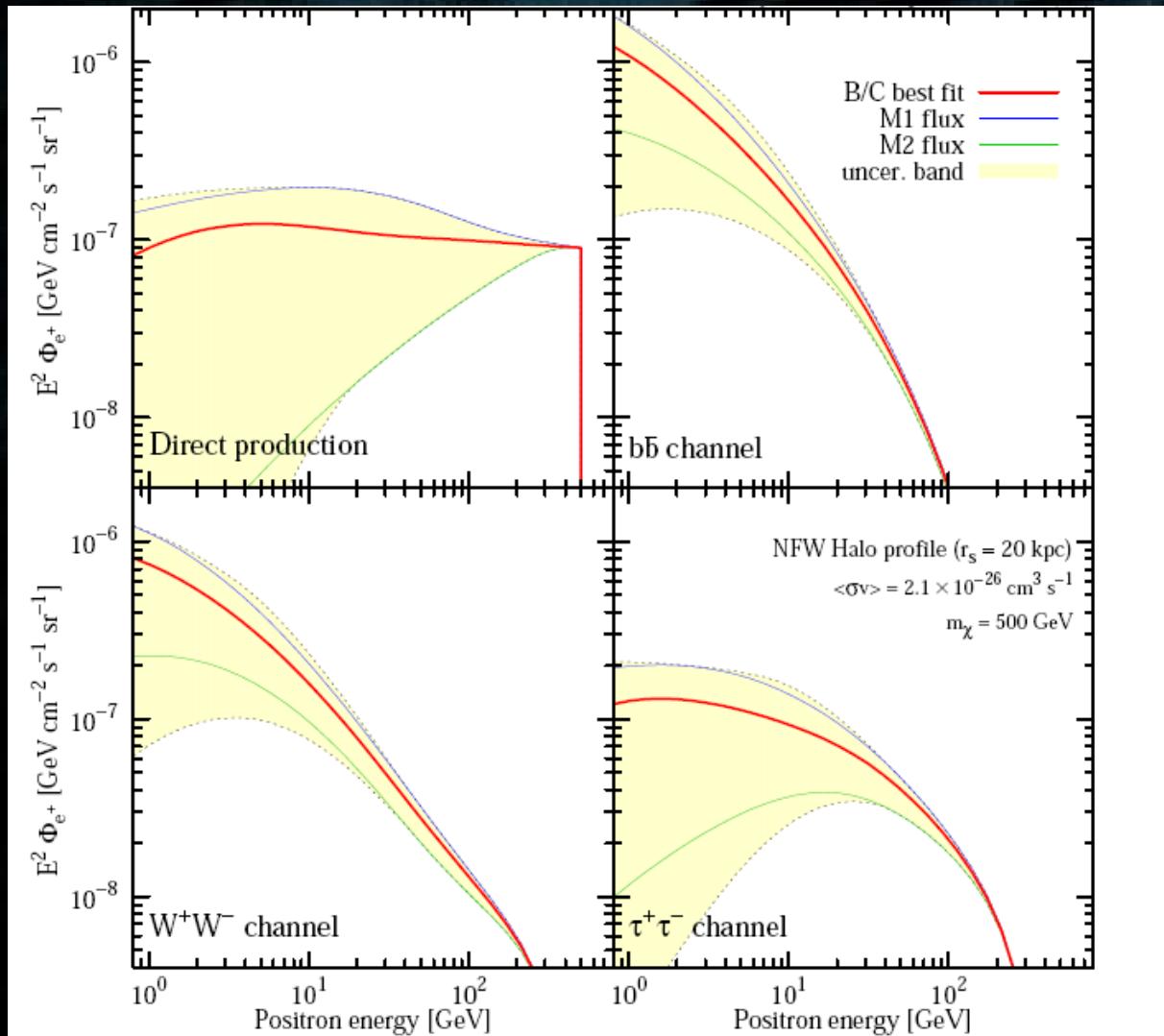
WIMP mass	100 GeV	500 GeV	1 TeV
final state			
e <sup>+</sup> e <sup>-</sup>	10	100	350
W+W <sup>-</sup>	80	500	1000
b <sup>-</sup> b	250	500	1000

The signal must be boosted:

- (i) boost the cross section  
→ contrived scenarios ( $\frac{3}{4}$  of published papers)  $\sim$  excluded by antiprotons  
(see e.g. Cirelli et al 08, Donato et al 09)
- (ii) play with the propagation parameters
- (iii) consider extra-sources  
(subhalos, IMBHs)

# Boost: Play with propagation

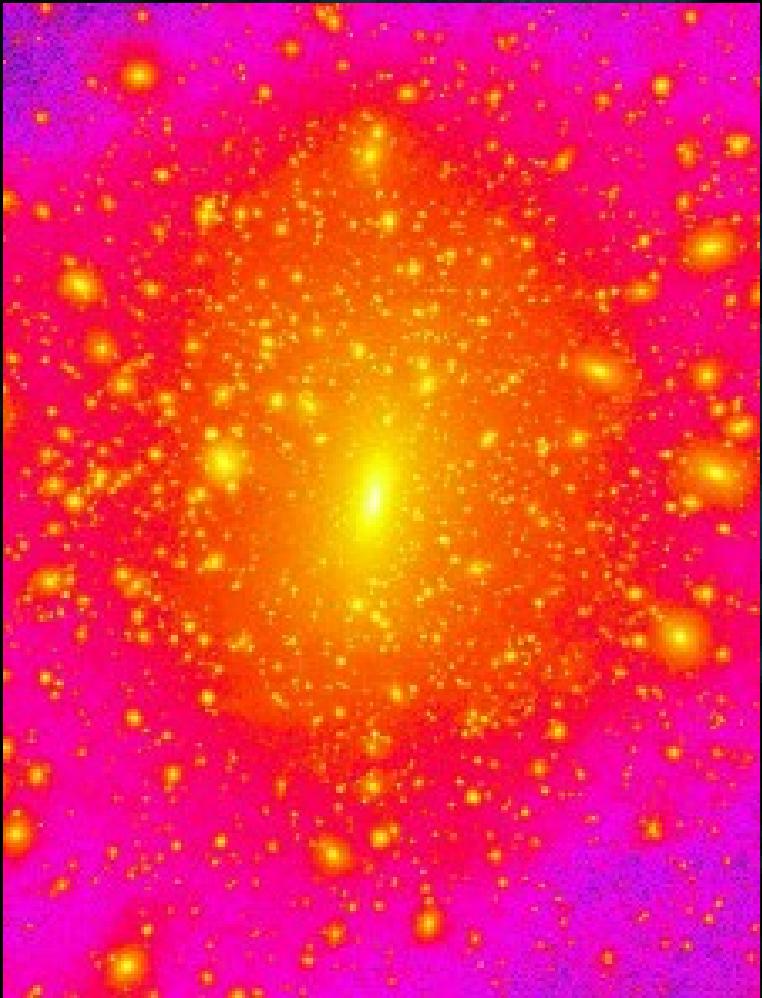
Delahaye et al (2008)



Increasing L implies more DM in the diffusion zone.

Very large effect on antiproton, but not on positrons since energy losses dominate at high energy (short range).

# Collective effect: clumpiness boost factor



Diemand et al 04

- Clumps are predicted by the current theory of structure formation (Peebles and others)
- They are observed in N-body simulations at all resolved scales, as predicted.
- The minimal mass scale is set by the WIMP properties (free streaming)  $\sim$  Earth mass.
- Smallest objects collapse first: they are more DM concentrated !

$$\langle n_{\text{dm}}^2 \rangle \geq \langle n_{\text{dm}} \rangle^2 \quad \longrightarrow \quad B_{\text{ann}} \sim \frac{\langle n_{\text{dm}}^2 \rangle}{\langle n_{\text{dm}} \rangle^2}$$

Clumps are numerous: statistical properties

The flux from an object is a stochastic variable

$$\phi_i(E, \vec{x}_\odot) = S \times \xi_i \times \tilde{g}_i(E, \vec{x}_\odot - \vec{x}_i, E_S)$$



$$\frac{dn_{\text{cl}}}{d\mathcal{L}}(\mathcal{L}, \vec{x}) = \frac{dN_{\text{cl}}}{dV d\mathcal{L}}(\mathcal{L}, \vec{x}) = N_0 \times \frac{dP}{dV}(\vec{x}) \times \frac{dP}{d\mathcal{L}}(\mathcal{L}, \vec{x})$$

*Boost factor ? ... well, in fact, boost factors* **green**

A large light blue circle representing a smooth galaxy.

**Smooth galaxy**

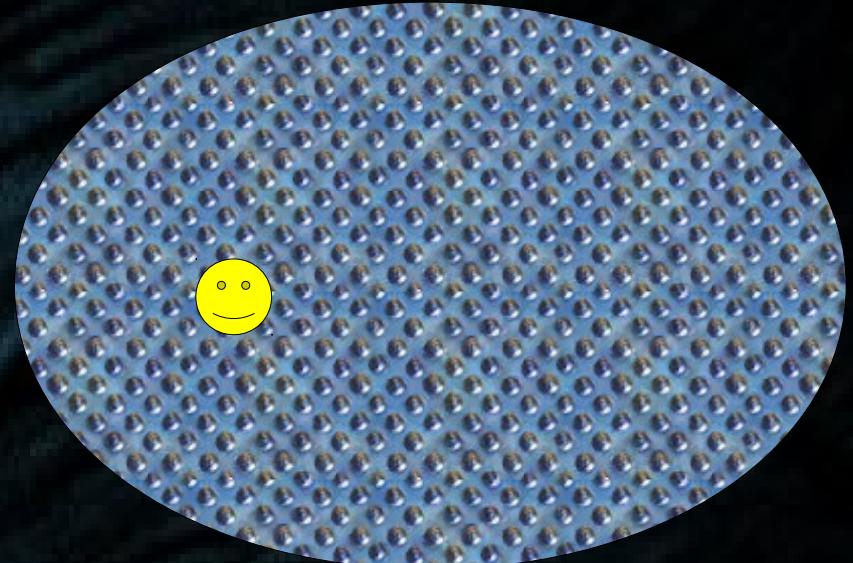
A large dark blue circle with a pattern of small white dots representing a clumpy galaxy.

**Clumpy galaxy**

$$\mathcal{B} = \frac{\langle \rho^2 \rangle}{\langle \rho \rangle^2} \geq 1$$

The volume over which the average is performed depends on the cosmic messenger!

# *Boost factor ? ... well, in fact, boost factors*

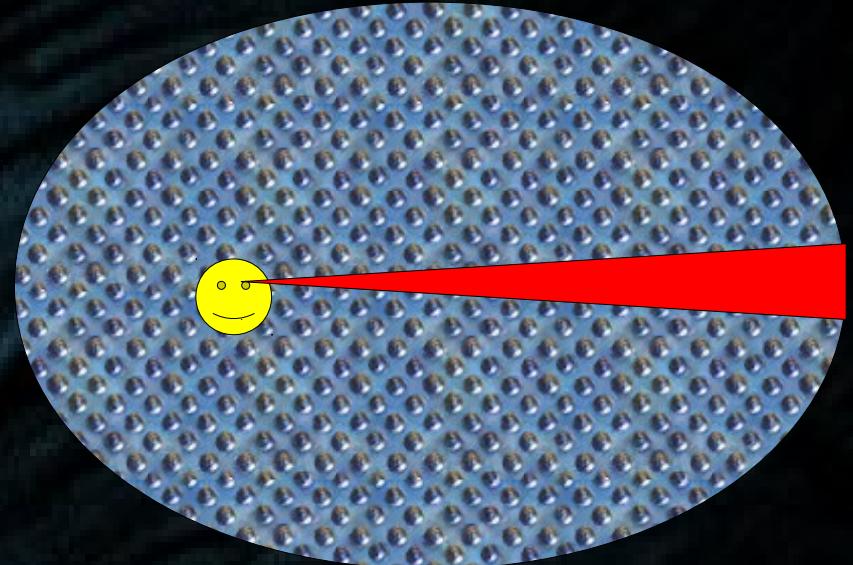
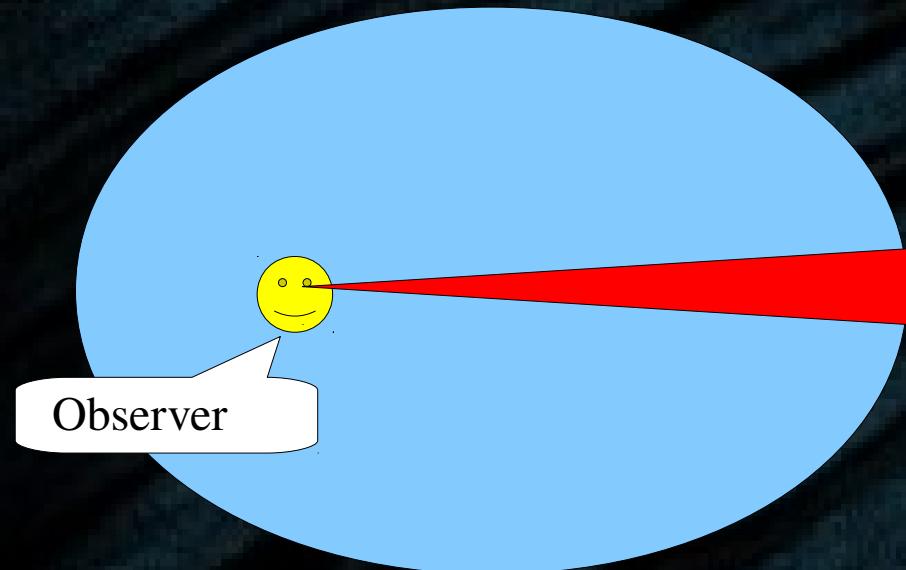


$$\mathcal{B} = \frac{\langle \rho^2 \rangle}{\langle \rho \rangle^2} \geq 1$$

The volume over which the average is performed depends on the cosmic messenger!

- 1) **Prompt gamma-rays:** point a telescope to a certain direction, and average over a volume set by the angular resolution

# *Boost factor ? ... well, in fact, boost factors* green

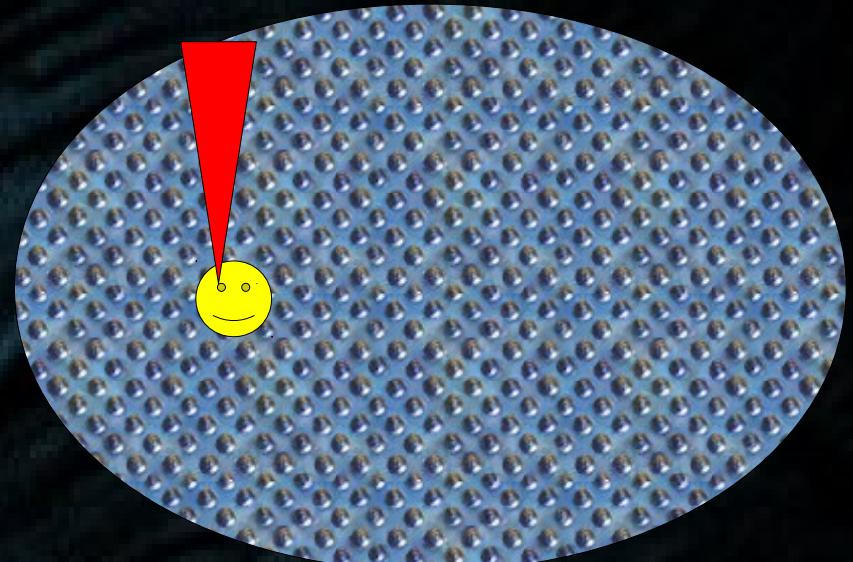
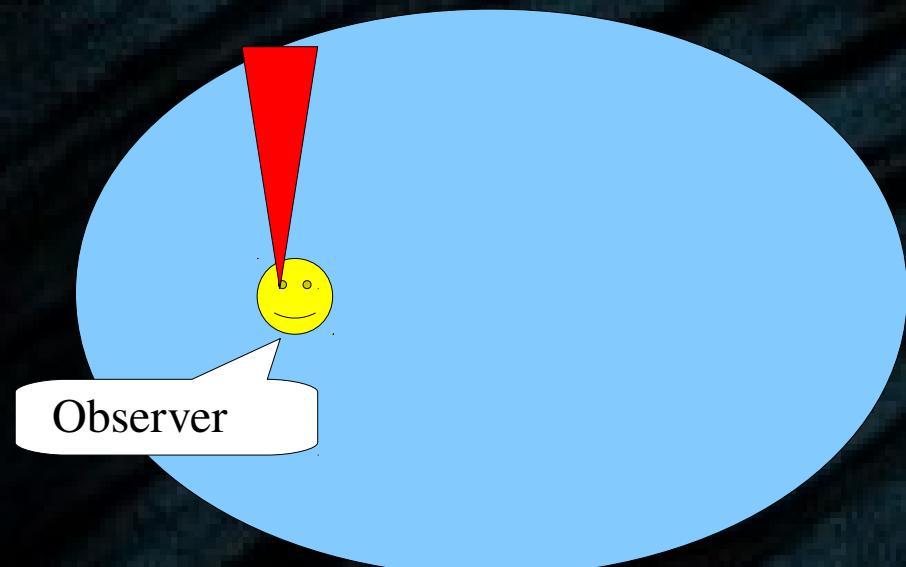


$$\mathcal{B} = \frac{\langle \rho^2 \rangle}{\langle \rho \rangle^2} \geq 1$$

The volume over which the average is performed depends on the cosmic messenger!

- 1) **Prompt gamma-rays:** point a telescope to a certain direction, and average over a volume set by the angular resolution
  - a) To the Galactic center: the smooth halo is singular, clumps have no effect,  $\mathbf{B} \sim 1$

# *Boost factor ? ... well, in fact, boost factors*

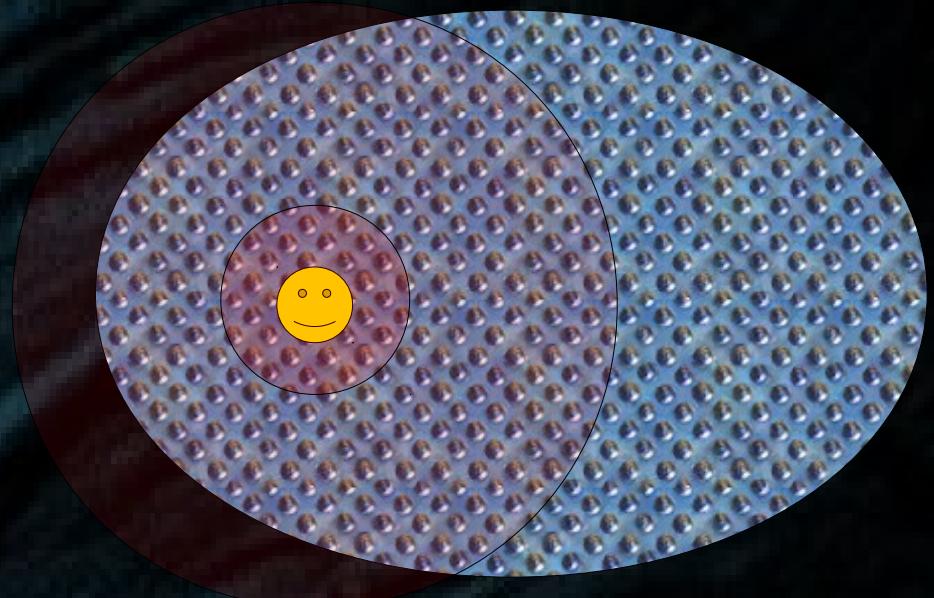
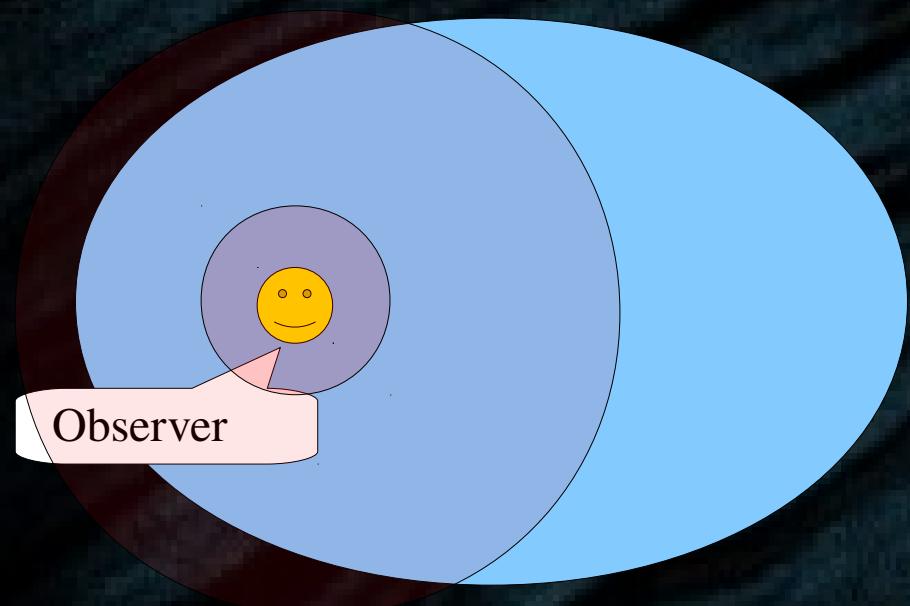


$$\mathcal{B} = \frac{\langle \rho^2 \rangle}{\langle \rho \rangle^2} \geq 1$$

The volume over which the average is performed depends on the cosmic messenger!

- 1) **Prompt gamma-rays:** point a telescope to a certain direction, and average over a volume set by the angular resolution
  - a) To the Galactic center: the smooth halo is singular, clumps have no effect,  $\mathbf{B} \sim 1$
  - b) To high latitudes/longitudes: the smooth halo contributes much less,  $\mathbf{B} \gg 1$

# *Boost factor ? ... well, in fact, boost factors*



$$\mathcal{B} = \frac{\langle \rho^2 \rangle}{\langle \rho \rangle^2} \geq 1$$

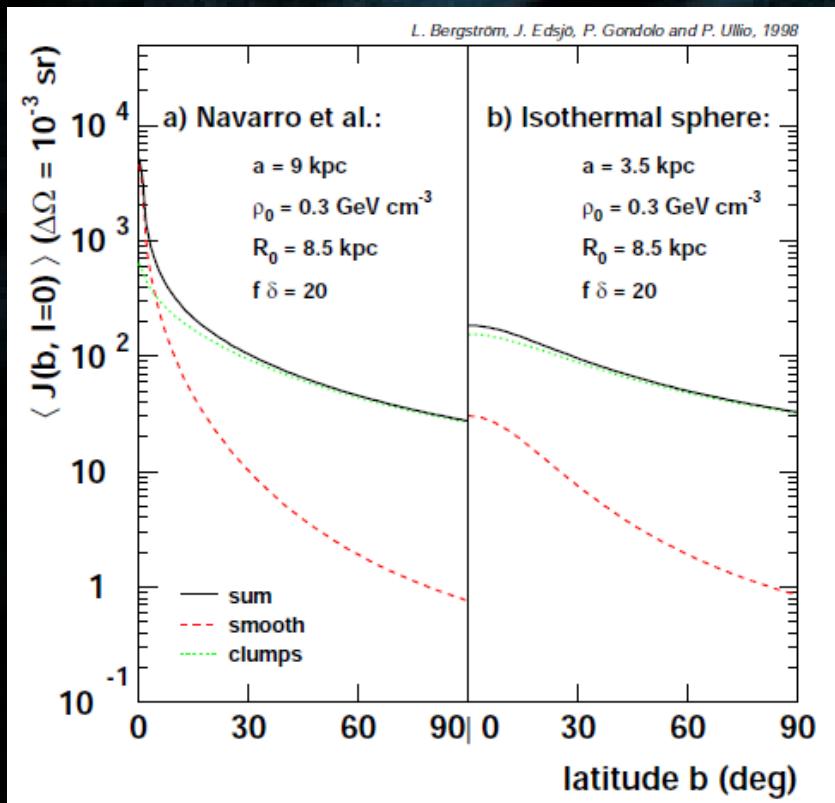
The volume over which the average is performed depends on the cosmic messenger!

- 1) **Prompt gamma-rays:** point a telescope to a certain direction, and average over a volume set by the angular resolution
  - a) To the Galactic center: the smooth halo is singular, clumps have no effect,  $\mathbf{B} \sim 1$
  - b) To high latitudes/longitudes: the smooth halo contributes much less,  $\mathbf{B} \gg 1$
- 2) **Cosmic rays:** stochastic motion, define energy-dependent propagation scale.
  - a) Large propagation scale: if enough to feel regions close to GC, then  $\mathbf{B} \sim 1$
  - b) Small propagation scale: if we are sitting on a clump, then  $\mathbf{B} \gg 1$ , otherwise  $\mathbf{B}$  moderate

# Summary pictures

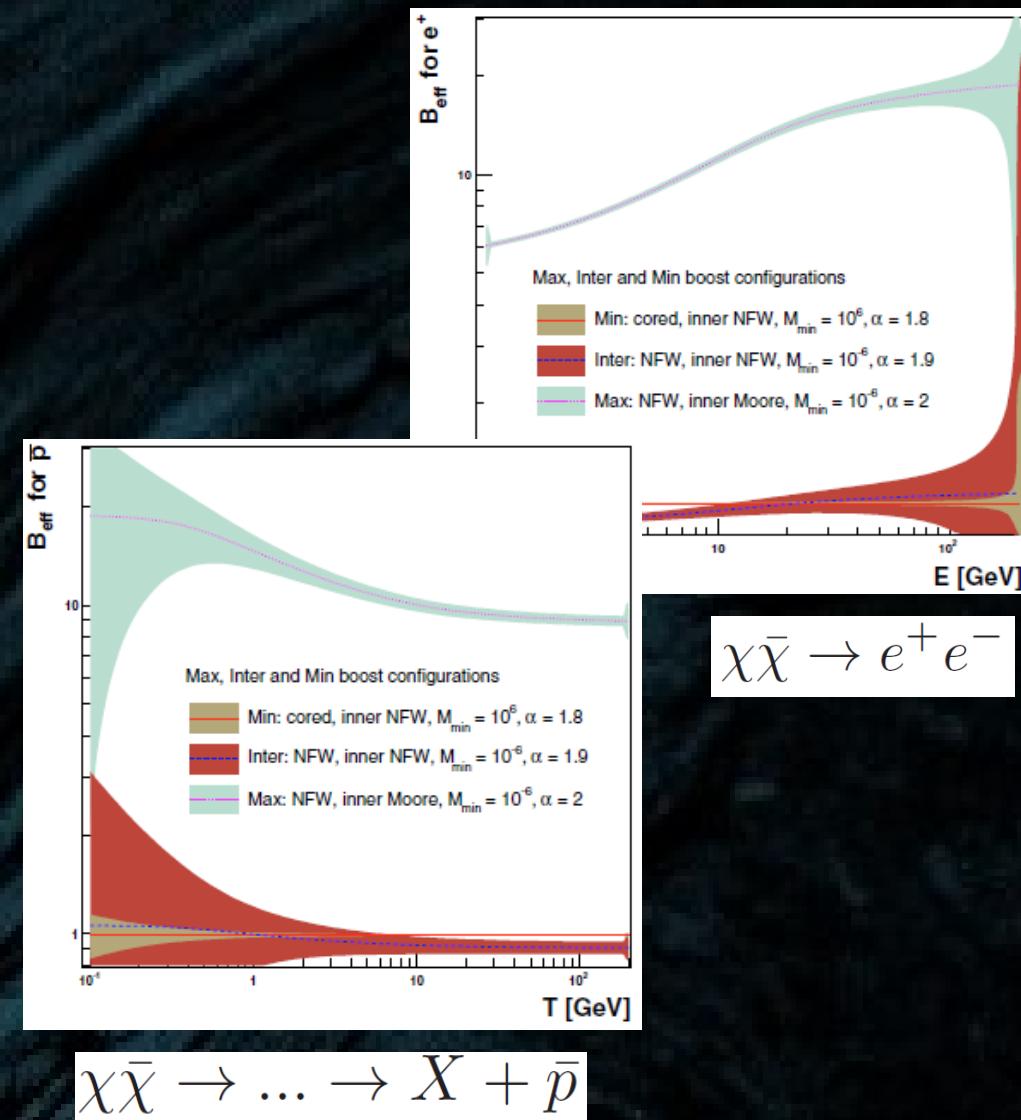
## Gamma rays:

Bergström et al (1999), assuming that clumps spatially track the smooth halo



## Antimatter cosmic rays:

Lavalle et al (2007,2008)

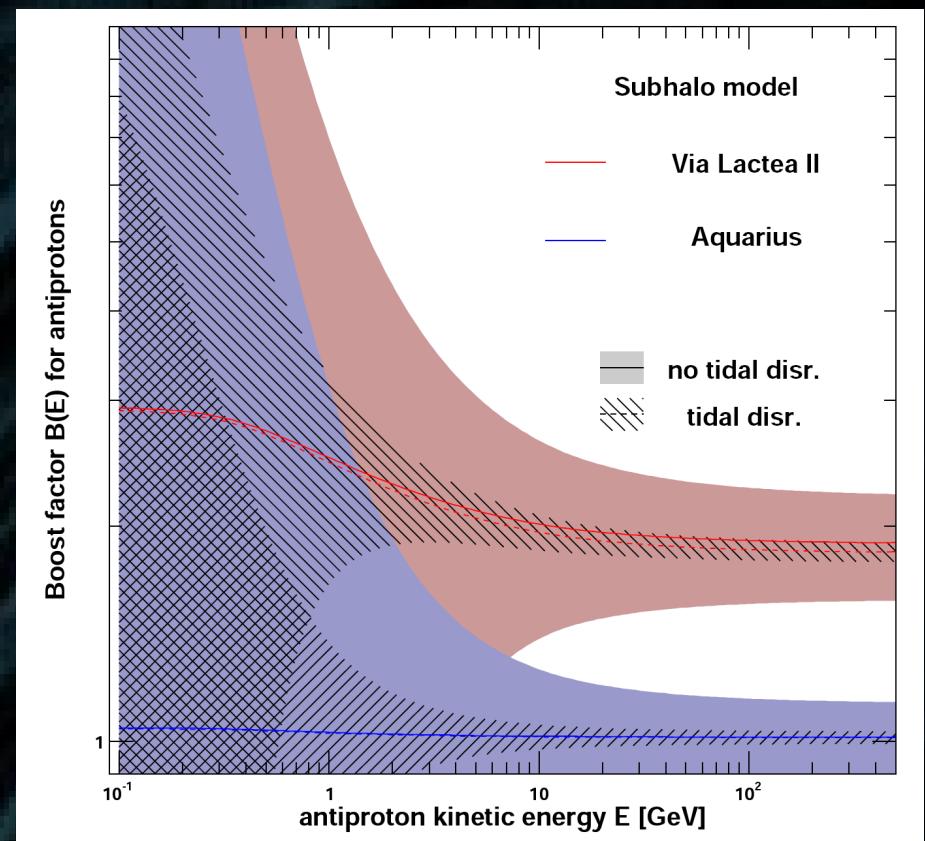
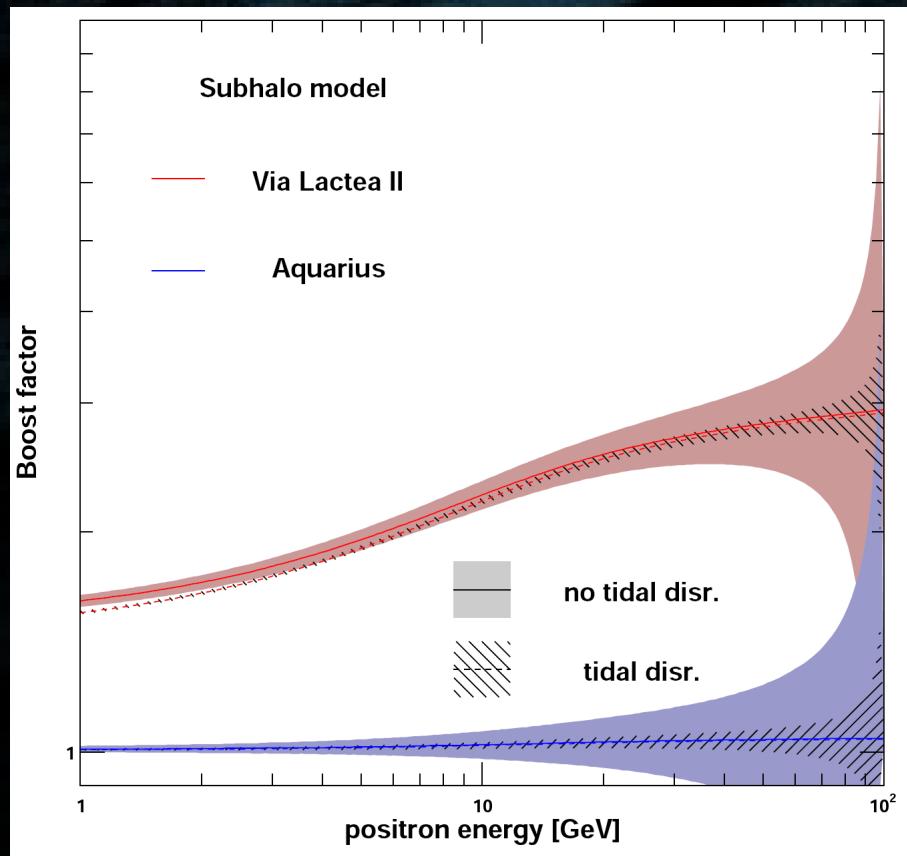


## Caution:

- Statistical meaning only
- Energy dependence of propagation depends on the species (nuclei/electrons)

# *Boost factors for positrons and antiprotons*

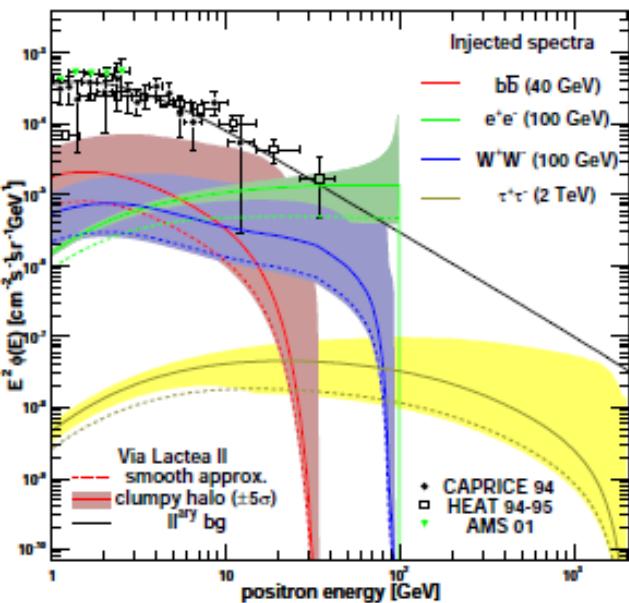
Pieri, JL, Bertone & Branchini (2009)



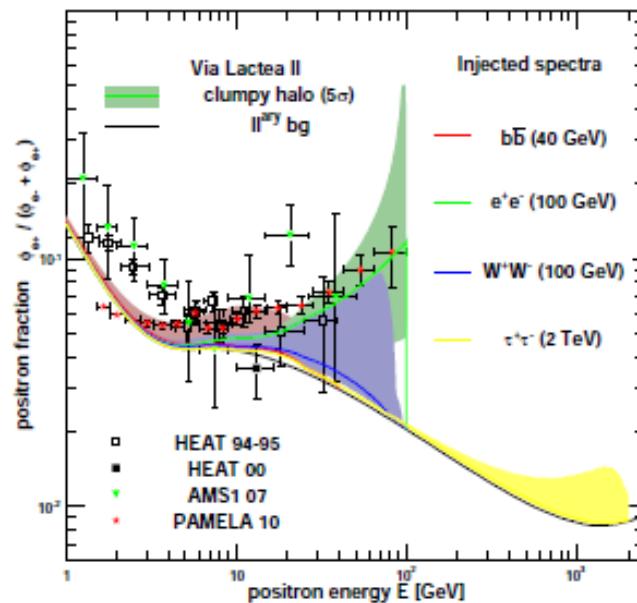
See also Lavalle et al (2007,2008)

# Clumpiness summary: Predictions with VL2 configuration

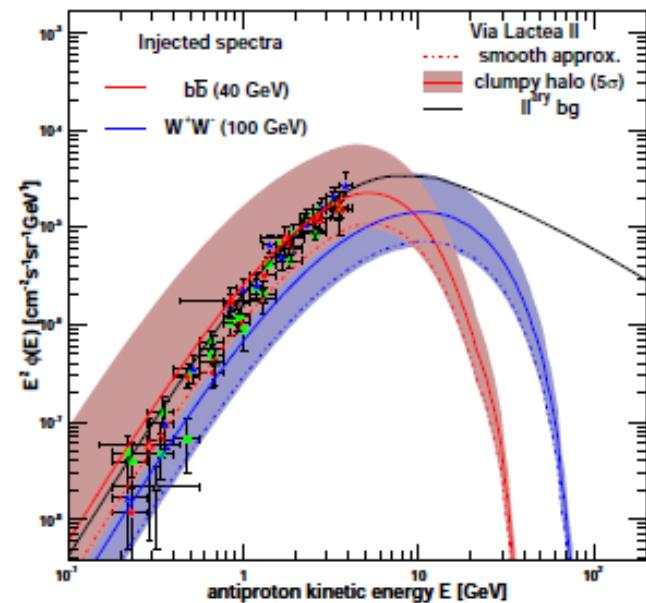
Positron flux



Positron fraction



Antiproton flux



Pieri, JL, Bertone & Branchini (2009)

using results from Via Lactea II (Diemand et al) and Aquarius (Springel et al)  
-- see early calculations in Lavalle et al (2007-2008) --

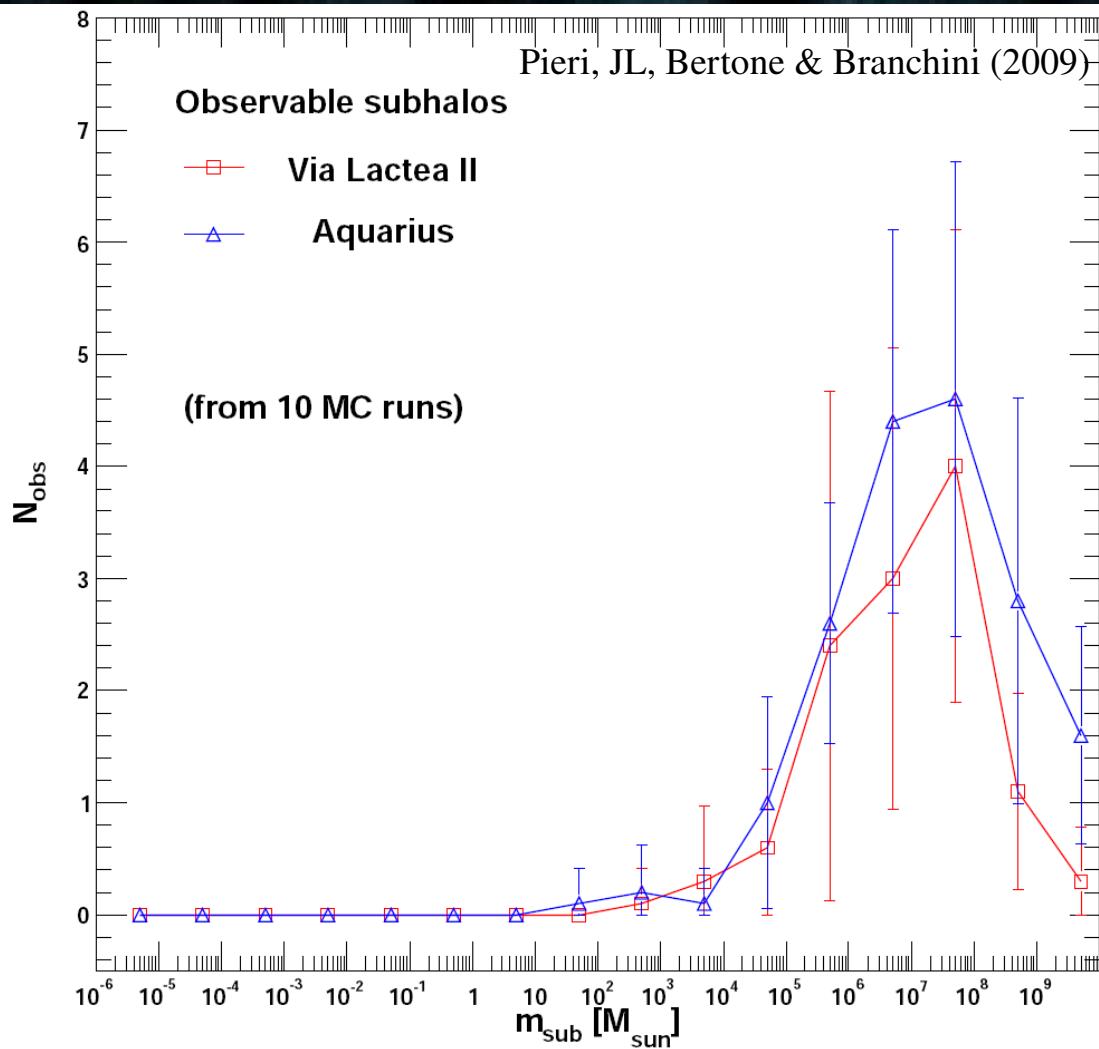
$$\langle \sigma v \rangle = 3 \cdot 10^{-26} \text{ cm}^3/\text{s}$$

model	$m_\chi$ [GeV]	final state
A	40	$b\bar{b}$
B	100	$W^+W^-$
C	100	$e^+e^-$
D	2000	$\tau^+\tau^-$

## Important features:

- 40 GeV WIMP ( $b\bar{b}$ ) excluded by antiproton constraints
- 100 GeV WIMP ( $WW$ ) at the edge of tension with the antiproton data
- 100 GeV WIMP going to  $e^+e^-$  can fit the PAMELA data; but pulsars not included => background must be known before any claim.

# *Sensitivity to individual subhalos*



**Galactic center:**

astrophysical contributions not under control,  
notably cosmic ray electrons.

**Subhalos:**

clean signal if located at high latitude, no  
counterpart at lower energies ... but have to be  
very massive and nearby to be observable.

N < 10 objects detectable with  
Fermi in 5 years.

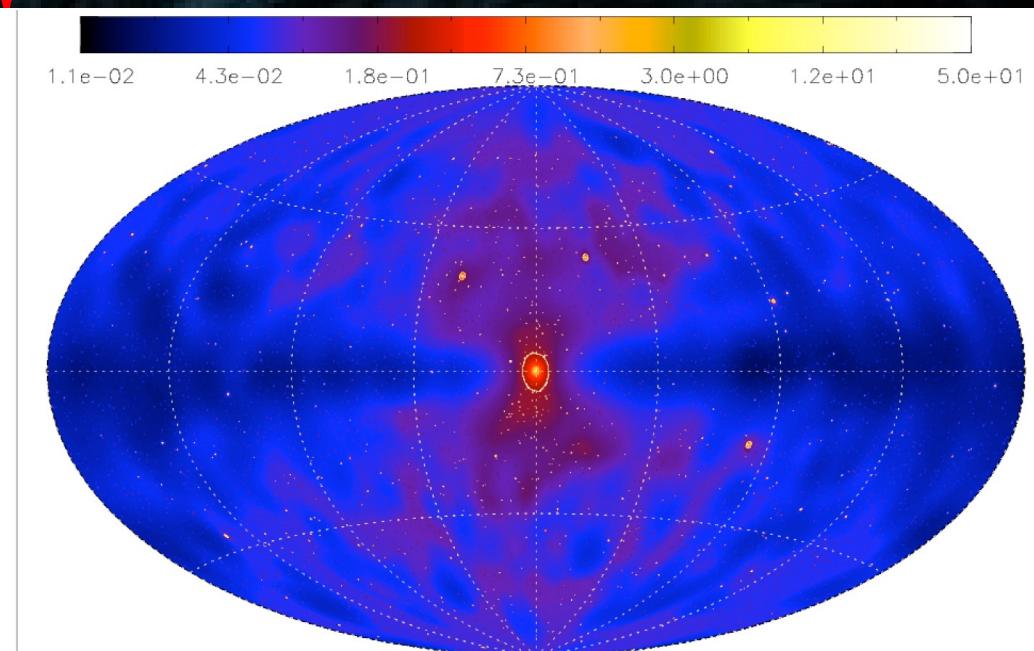
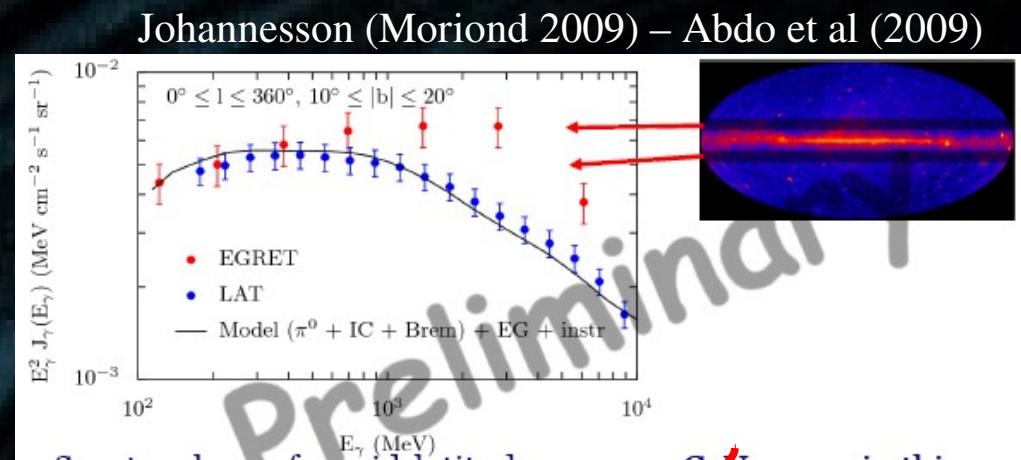
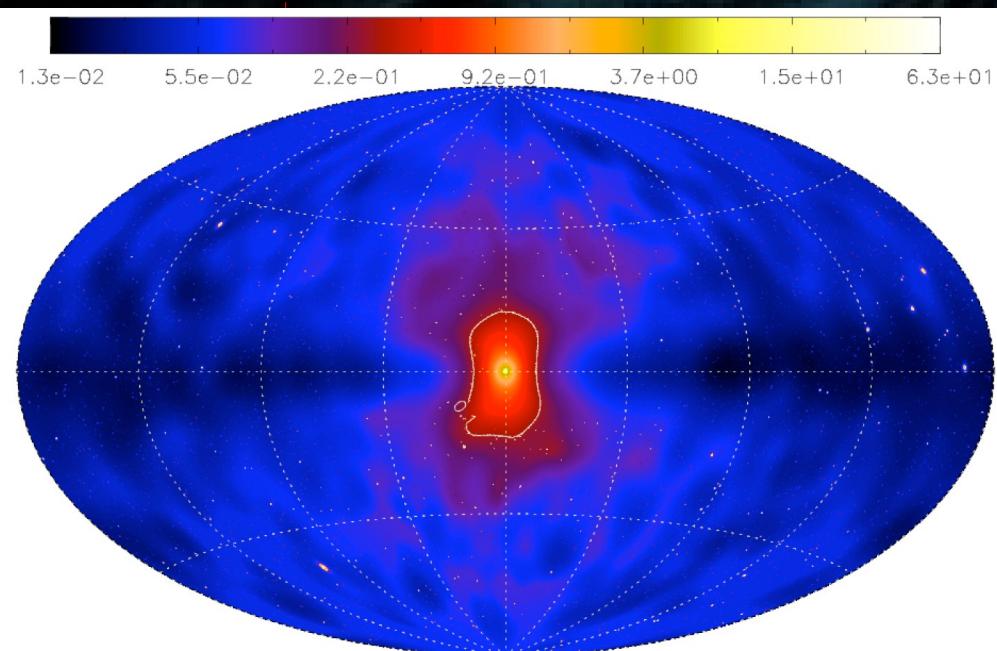
Model A: 40 GeV WIMP going to b-bbar  
 Model B: 100 GeV WIMP going to WW

model	<i>VLLII</i> 3 $\sigma$	<i>VLLII</i> 5 $\sigma$	<i>Aq</i> 3 $\sigma$	<i>Aq</i> 5 $\sigma$
A	$9.2 \pm 2.6$	$4.1 \pm 1.3$	$13.5 \pm 2.5$	$7.3 \pm 2.4$
B	$3.1 \pm 1.1$	$1.4 \pm 0.8$	$6.2 \pm 2.1$	$2.9 \pm 1.4$

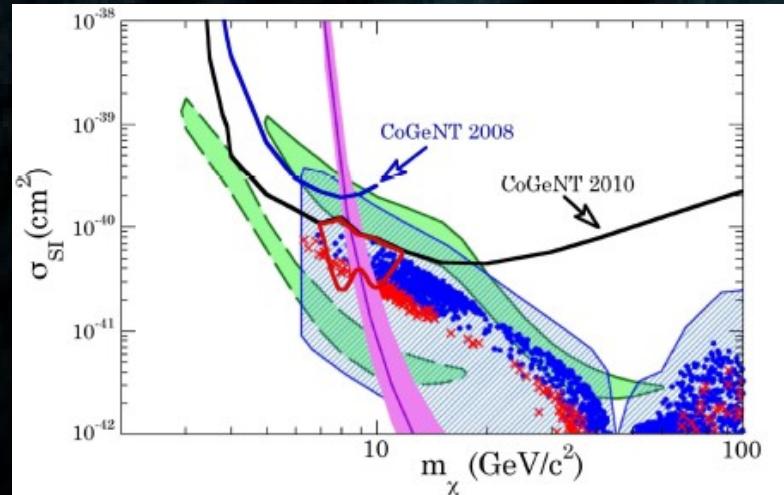
# Gamma-ray skymaps

Empirical diffuse emission model:  
template maps from EGRET  
(Cillis & Hartman 05)

But EGRET is no longer a reference:  
our  $B_g = EGRET - 50\%$



# (Parenthesis: antiprotons versus small WIMP masses)

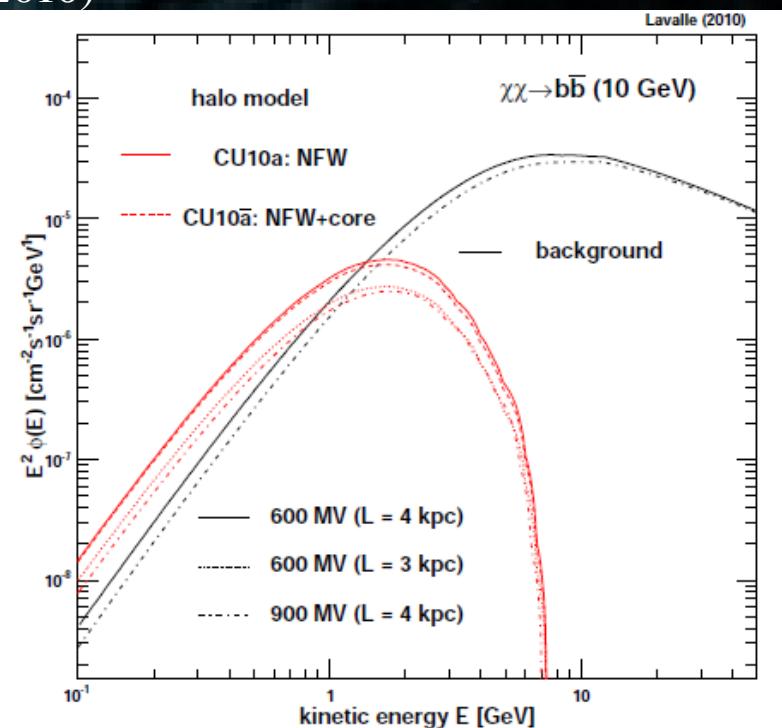
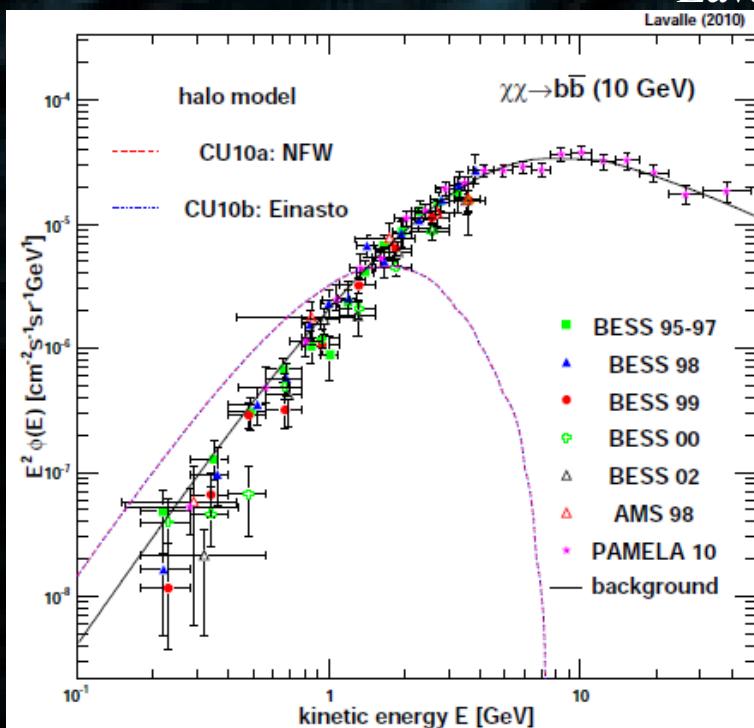


DAMA+CDMS+COGENT mass regions  
=> WIMP mass  $\sim 10$  GeV

If WIMPs couple to quarks, annihilation can produce  
antiprotons if  $m_{\text{wimp}} > m_p$

Large antiproton flux expected (it scales like  $1/m^2$ )  
New constraints on propagation (Putze et al 10) => excess wrt data

Lavalle (2010)



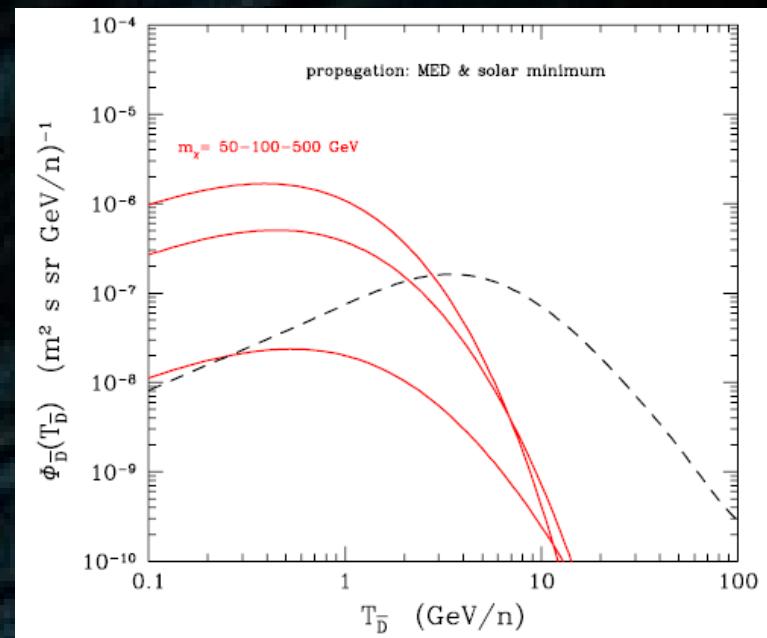
# *An optimistic view about non-discovery (yet): WIMP candidates are not excluded !*

## Status of WIMP searches:

- WIMPs are fairly well motivated from particle physics beyond the Standard Model.
- From generic predictions, they are not expected to show up in current data.
- Interesting constraints from antiprotons: complementarity required!  
(multiwavelength, multimessenger)
- Most promising sources in the future: dwarf spheroidal galaxies and subhalos  
(gamma-rays).
- Cosmic-ray antideuterons below 1 GeV ? (Salati et al, 00)

## Astrophysical issues:

- Backgrounds !
- The impact of baryons on dark matter distribution:
  - Adiabatic contraction in galaxy centers ? Or cores ?  
(see Governato et al 10)
  - Local dark matter density and velocity distribution ?  
(Catena & Ullio 10, Salucci et al 10)
  - Subhalo survival ? Power in small scales vs reionization ?  
(Klypin et al 10)



Donato, Fornengo & Salati 00  
Donato, Fornengo & Maurin 08

# *Conclusions & perspectives*

## *Part I: Cosmic-ray nuclei, propagation models*

- Models incredibly successful despite the very crude assumptions.
- Limits are reached for very accurate predictions.
- Improve Galaxy modeling (ISM, ISRF, magnetic field, convection, etc.).
- More fundamental understanding required: link between turbulence and transport => try top-down approaches.

## *Part II: Cosmic-ray electrons and positrons*

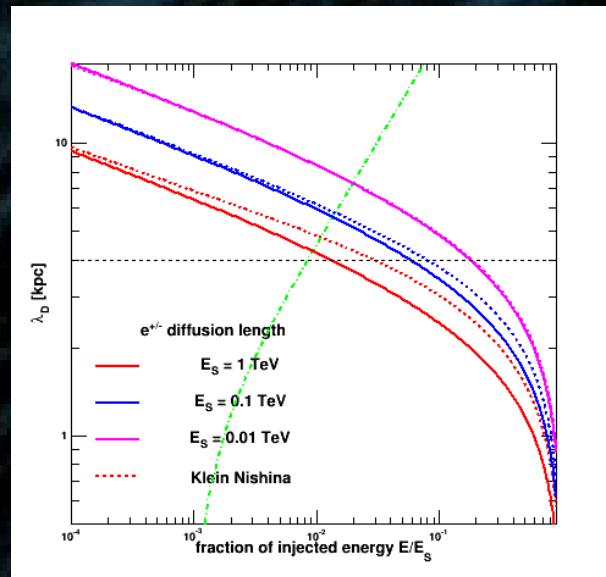
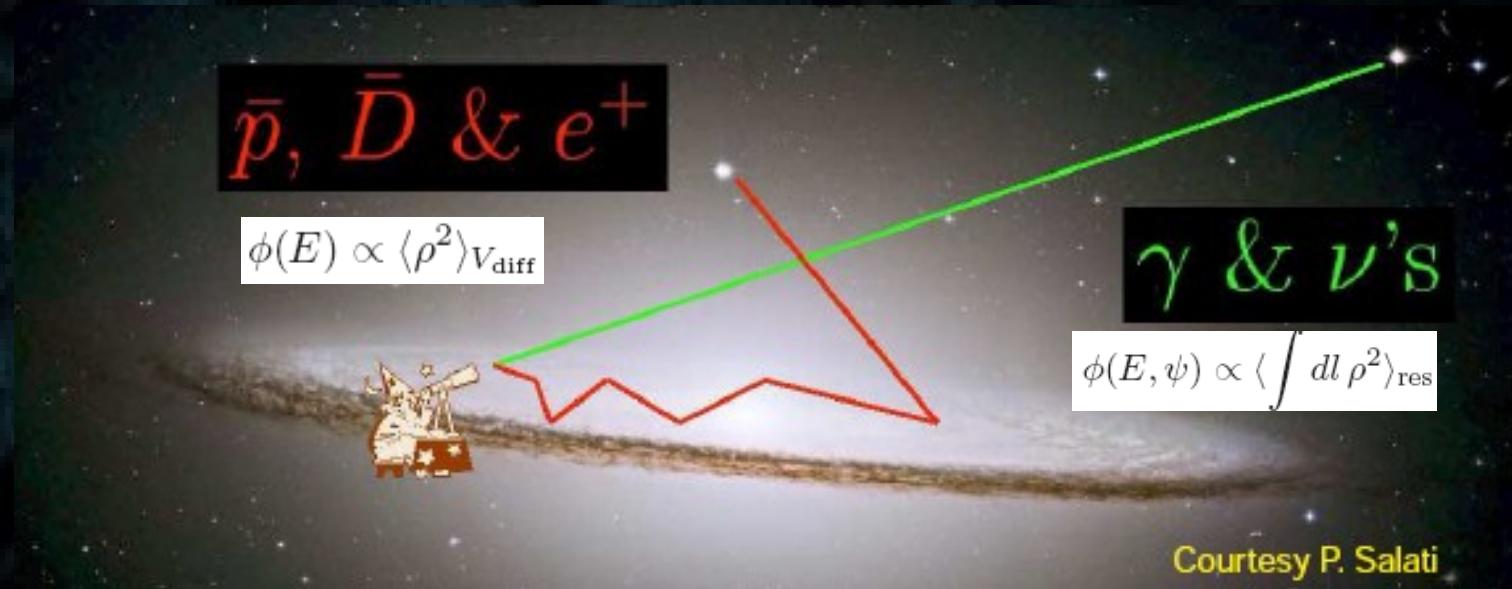
- Local sources give hopes to improve our modeling/understanding.
- Large uncertainties above 50 GeV.
- On going improvements (source modeling, diffuse emissions).

## *Part III: Searches for dark matter annihilation signals*

- Difficult searches: signals are weak and does not show up easily.  
Interesting constraints (antiprotons, diffuse emissions).
- Targets: DSph, Galactic Center, antideuterons ++ complementarity

# *Backup*

# Cosmic messengers: boost related to their spatial origin



# *Why should we take subhalos into account?*

- They are **predicted** by the theory of structure formation, while their features (minimal scale, number density, inner profile) depend on dark matter properties: eg CDM versus WDM.
- They are “**observed**” in N-body simulations of structures on different scales (from the galaxy cluster scale down to the dwarf galaxy scale); but current resolution limit =>  $M_{\text{res}} \sim 10^4 \text{ Msun}$ .
- They might be observed in Nature above scales able to accrete the baryons efficiently enough (dwarf galaxies).
- The small-scale clustering of dark matter can **increase the annihilation rate** quite significantly.

=> **Self-consistency +++; increase discovery / exclusion potential.**

# *Credit to the original idea*

THE ASTROPHYSICAL JOURNAL, 411:439–449, 1993 July 10

© 1993. The American Astronomical Society. All rights reserved. Printed in U.S.A.

## CLUMPY COLD DARK MATTER

JOSEPH SILK

Departments of Astronomy and Physics, and Center for Particle Astrophysics, University of California, Berkeley, CA 94720

AND

ALBERT STEBBINS

NASA/FermiLab Astrophysics Center, Fermi National Accelerator Laboratory, Batavia, IL 60510

*Received 1992 March 25; accepted 1992 December 16*

- WIMPs freeze out (chemically and kinematically) in a radiation-dominated universe before BBN. They feed gravitational perturbations down to their free-streaming scale.
- Perturbations start to grow efficiently after radiation-matter equivalence ( $z \sim 3500$ ): DM seeds have very large densities at that time.  $10^{-6}$  Msun objects enter the non-linear regime around  $z \sim 100$ .
- Galaxies form at  $z \sim 6$  in a much less dense universe, and should contain many of these very dense cores of dark matter, called clumps.
- Some of these clumps may **survive** tidal disruption and **increase the annihilation rate**.

# The small scale issue

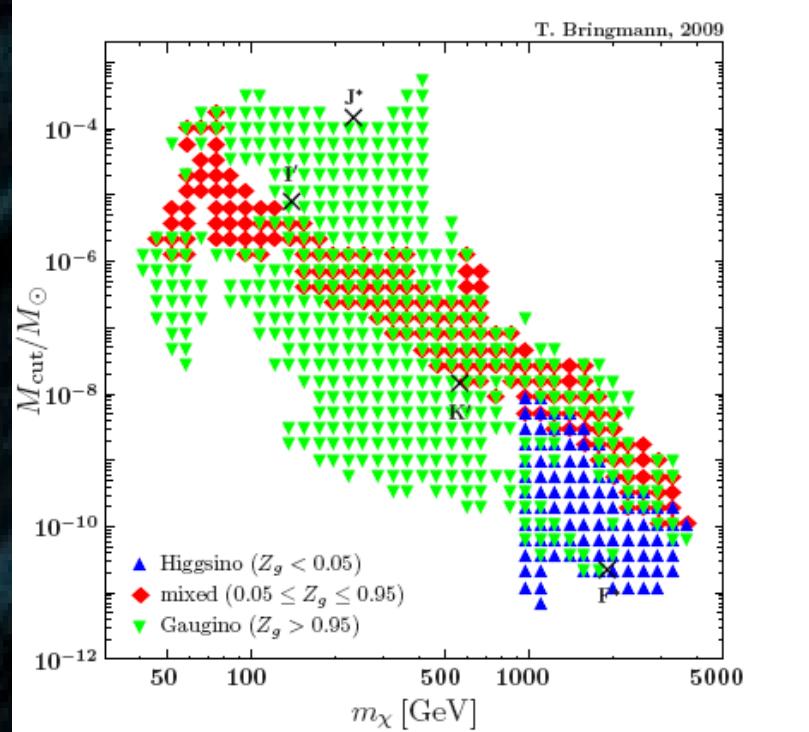
(see review by T. Bringmann (2009))

The free streaming scale depends on the time of kinetic ( $\neq$  chemical) decoupling of WIMPs from the primordial soup.

The weaker the collision rate, the smaller the free streaming scale and the cut-off mass.

Subhalo mass down to  $10^{-11}$ - $10^{-3} M_\odot$  (SUSY). The lighter the denser.

Tidal effects ? Large survival fraction (Berezinsky et al, 2008)



T. Bringmann arXiv:0903.0189

	$M_{\text{sub}}^{\text{res}}$ [ $10^4 M_\odot$ ]	$N_{\text{sub}}^{\text{res}}$ [ $10^4$ ]	Mass slope	$f_{\text{sub}}^{\text{res}}$ [%]
VL2	$\sim 10^2$	5.3	2	10
AQ	3.24	30	1.9	13.2

Extrapolation  
down to  $10^{-6} M_\odot$

	$M_{\text{sub}}^{\text{min}}$ [ $10^{-6} M_\odot$ ]	$N_{\text{sub}}^{\text{tot}}$ [ $10^{15}$ ]	Mass slope	$f_{\text{sub}}^{\text{tot}}$ [%]
VL2	1	28	2	54.2
AQ	1	1.1	1.9	17.1

# Going into more details: a statistical approach (1)

General expression for the flux measured on Earth

$$\phi(E, \vec{x}_{\text{obs}}) = \underbrace{\frac{\delta \langle \sigma v \rangle}{8\pi} \left[ \frac{\rho_0}{m_\chi} \right]^2}_{\mathcal{S}} \int_{(\text{sub})\text{halo}} d^3 \vec{x}_s \underbrace{\int dE_s \mathcal{G}(E, \vec{x}_{\text{obs}} \leftarrow E_s, \vec{x}_s) \frac{dN(E_s)}{dE_s}}_{\tilde{\mathcal{G}}(\vec{x}_{\text{obs}} \leftarrow \vec{x}_s)} \left[ \frac{\rho(\vec{x}_s)}{\rho_0} \right]^2$$

The Green function encodes the propagation properties  
 => trivial for gamma-rays

$$\int_{(\text{sub})\text{halo}} d^3 \vec{x}_s \int dE_s G(E, \vec{x}_{\text{obs}} \leftarrow E_s, \vec{x}_s) \xrightarrow{\gamma-\text{rays}} \int_{\text{l.o.s.}} d\Omega_{\text{res}} dl \int dE_s \delta(E - E_s)$$

Subhalos: point-like sources provided  $G$  does not vary too much over the object

$$\text{if } \lambda_{\text{prop}} \gg r_s \implies \int_{\text{sub}} d^3 \vec{x}_s \tilde{\mathcal{G}}(\vec{x}_{\text{obs}} \leftarrow \vec{x}_s) \left[ \frac{\rho_i(\vec{x}_s)}{\rho_0} \right]^2 \rightarrow \tilde{\mathcal{G}}(\vec{x}_{\text{obs}} \leftarrow \vec{x}_i) \underbrace{4\pi \int dr r^2 \left[ \frac{\rho_i(r)}{\rho_0} \right]^2}_{\xi_i}$$

$$\phi_i = \mathcal{S} \times \tilde{\mathcal{G}}(\vec{x}_{\text{obs}} \leftarrow \vec{x}_i) \times \xi_i \quad \phi_{\text{tot}} = \phi_{\text{sm}} + \sum_{i \in \text{sub}} \phi_i = \phi_{\text{sm}} + N_{\text{tot}} \langle \phi_{\text{sub}} \rangle$$

$$\mathcal{B} = \frac{\phi_{\text{tot}}}{\phi_{\text{smooth}}} = \left\{ \frac{\phi_{\text{sm}}}{\phi_{\text{smooth}}} \approx 1 \right\} + N_{\text{tot}} \frac{\langle \phi_{\text{sub}} \rangle}{\phi_{\text{smooth}}}$$

# Going into more details: a statistical approach (2)

Define the flux pdf for subhalos

$$\langle \phi_{\text{sub}} \rangle = \int d\phi \phi \frac{d\mathcal{P}_\phi(\phi)}{d\phi}$$

The flux pdf is completely set by:

$$\frac{d\mathcal{P}_\phi(\phi)}{d\phi} \propto \underbrace{\frac{d\mathcal{P}_V(\vec{x})}{dV}}_{\text{spatial distrib.}} \times \underbrace{\frac{d\mathcal{P}_M(M, \vec{x})}{dM}}_{\text{mass distrib.}} \times \underbrace{\frac{d\mathcal{P}_c(c, M, \vec{x})}{dc}}_{\text{concentration distrib.}}$$

The average subhalo flux is entirely defined (same way for variance)

$$\begin{aligned} \langle \phi_{\text{sub}} \rangle &= \mathcal{S} \int d^3 \vec{x}_s \tilde{\mathcal{G}}(\vec{x}_{\text{obs}} \leftarrow \vec{x}_s) \frac{d\mathcal{P}_V(\vec{x}_s)}{dV} \int dM \frac{d\mathcal{P}_M(M, \vec{x}_s)}{dM} \int dc \frac{d\mathcal{P}_c(c, M, \vec{x})}{dc} \xi(\vec{x}_s, M, c) \\ &= \mathcal{S} \times \langle \tilde{\mathcal{G}} \langle \xi \rangle_{c,M} \rangle_V \approx \mathcal{S} \times \langle \tilde{\mathcal{G}} \rangle_V \times \langle \xi \rangle_{c,M} \end{aligned}$$

Remind: the subhalo properties are fully set by its mass and its concentration  
(and position in the Galaxy)

$$M_{\text{vir}} = \frac{4\pi}{3} (\delta \rho_c) r_{\text{vir}}^3$$

$$\begin{aligned} M_{200} &= M_{\text{vir}}(\delta = 200) \\ M_{\text{vir}} &= M_{\text{vir}}(\delta = \Delta(z) \Omega_m(z)) \end{aligned}$$

$$\begin{aligned} c_{200} &= \frac{r_{200}}{r_{-2}} \\ c_{\text{vir}} &= \frac{r_{\text{vir}}}{r_{-2}} \end{aligned}$$

# Use $\mathcal{N}$ -body info: Via Lactea II versus Aquarius

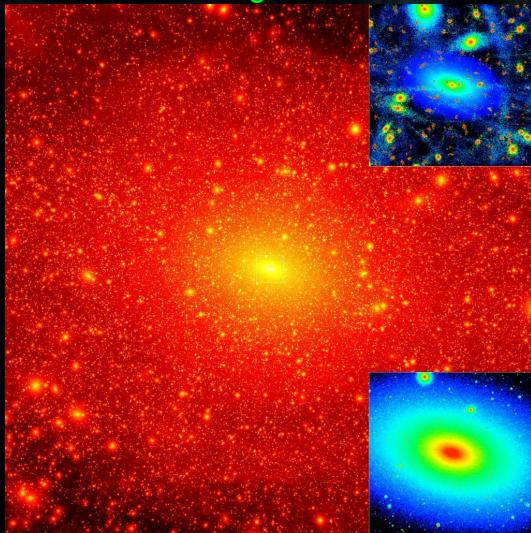
Via Lactea II: Diemand et al (2008)

Aquarius: Springel et al (2008)

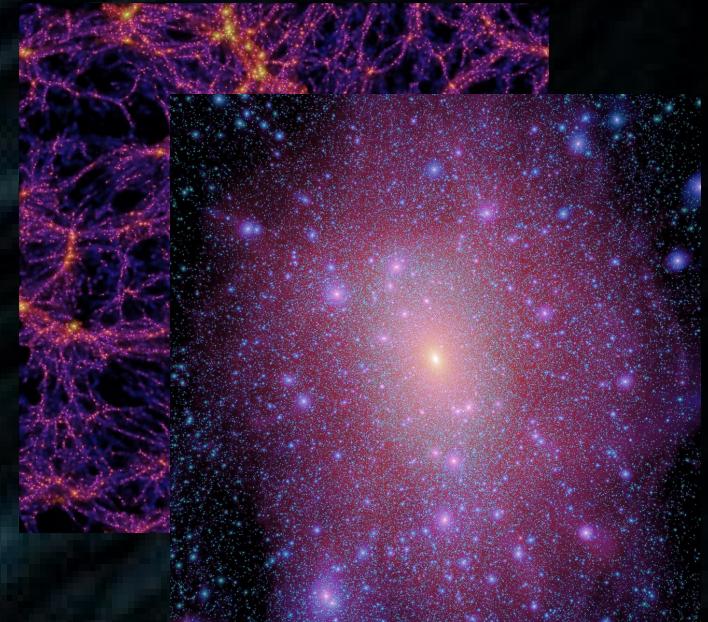
MW-like halos with  $\sim 1$  billion particles of  $\sim 10^3 M_{\odot}$   
 $> 50,000\text{-}300,000$  subhalos with masses  $> 10^6 \text{--} 10^{4.5} M_{\odot}$

Slightly different cosmologies: WMAP3 vs WMAP5  
 $(\sigma_8 = 0.74 \text{ vs } 0.9)$

<http://www.ucolick.org/~diemand/vl/index.html>



<http://www.mpa-garching.mpg.de/aquarius/>



Gamma-ray studies in:

Kuhlen et al (2008) – VL2

Springel et al (2008) – AQ

## Overall DM

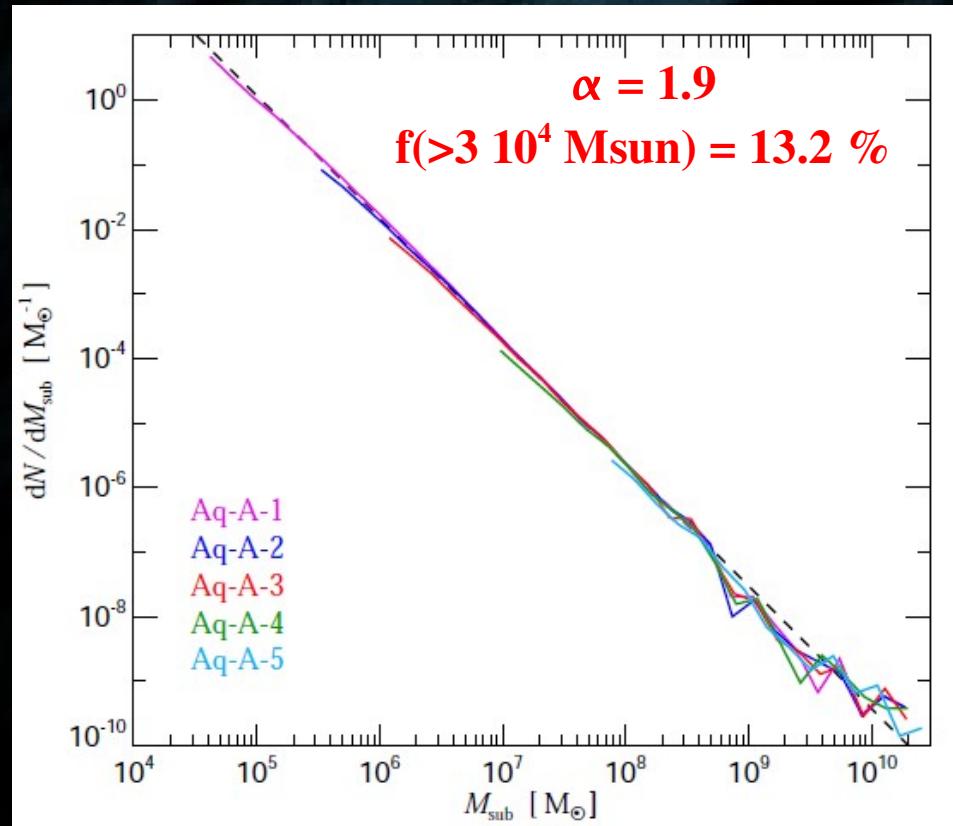
	$M_{\text{part}}$ $[10^3 M_{\odot}]$	$N_{\text{part}}$ $[10^8]$	$M_{50}$ $[10^{12} M_{\odot}]$	$R_{50}$ [kpc]	Density profile	$\rho_{\odot}$ [GeV/cm $^3$ ]
VL2	4.1	4.7	1.9	402	NFW	0.42
AQ	1.7	14.7	2.52	433	Einasto	0.57

## Subhalos

	$M_{\text{sub}}^{\text{res}}$ $[10^4 M_{\odot}]$	$N_{\text{sub}}^{\text{res}}$ $[10^4]$	Mass slope	$f_{\text{sub}}^{\text{res}}$ [%]
VL2	$\sim 10^2$	5.3	2	10
AQ	3.24	30	1.9	13.2

# Mass function

Subhalo mass function from Aquarius  
(Springel et al, 2008)



Power law mass function

$$\frac{d\mathcal{P}_M(M)}{dM} = K_M \left[ \frac{M}{M_\odot} \right]^{-\alpha}$$

Press & Schechter (1974):  $\alpha = 2$  (theory)

Aquarius (Springel et al):  $\alpha \sim 1.9$

Via Lactea (Diemand et al):  $\alpha \sim 2.0$

NB: resolution limit => **assume scale invariance**

Calibrate subhalo mass content from simulations:

$$f_{\text{tot}} = f_{\text{res}} \times \frac{(M_{\text{max}}^{2-\alpha} - M_{\text{min}}^{2-\alpha})}{(M_{\text{max}}^{2-\alpha} - M_{\text{res}}^{2-\alpha})}$$

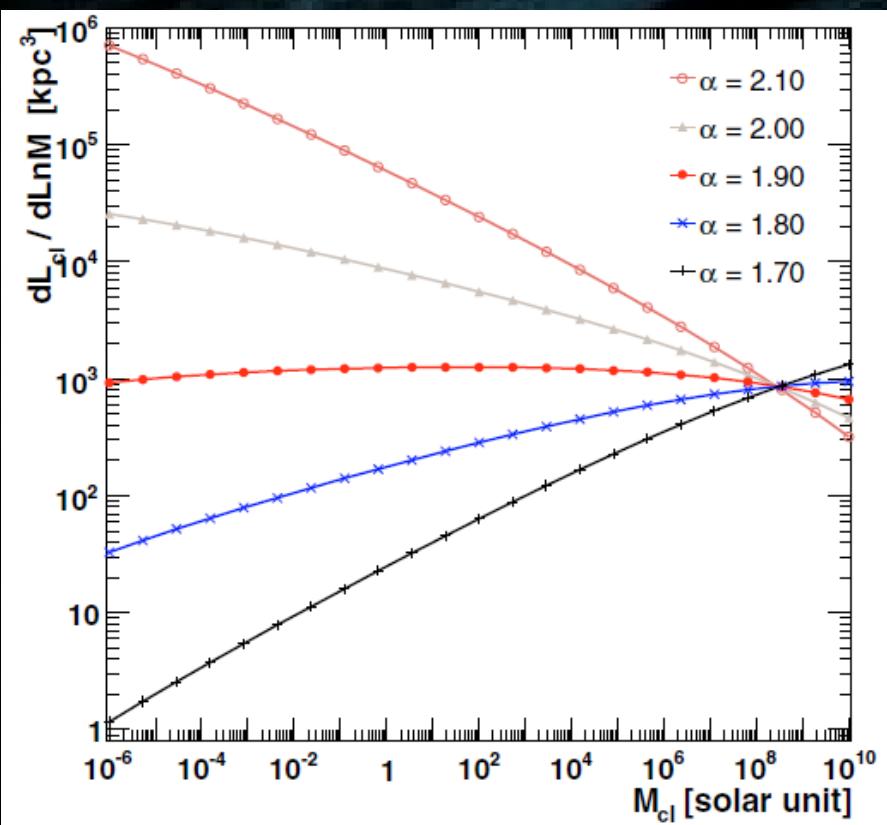
=> Get total number of subhalos:

$$N_{\text{tot}} = \frac{f_{\text{tot}} M_{MW}}{\langle M \rangle} \propto M_{\text{min}}^{1-\alpha}$$

The subhalo mass content is determined by the minimal mass  $M_{\text{min}}$  and the slope  $\alpha$ , and is calibrated from the mass fraction resolved in N-body simulations => **Extrapolation down over > 10 OM !!!**

# Luminosity function

Analytical luminosity function  
 (NFW, concentration from Bullock et al 2001)  
 (Lavalle et al, 2008)



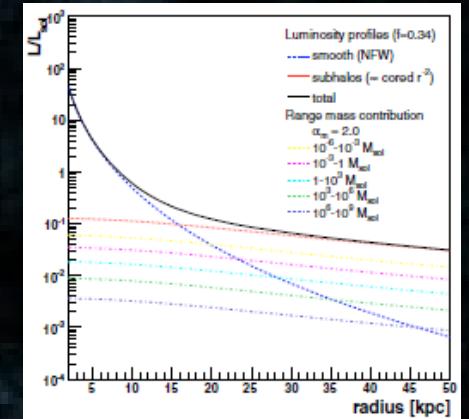
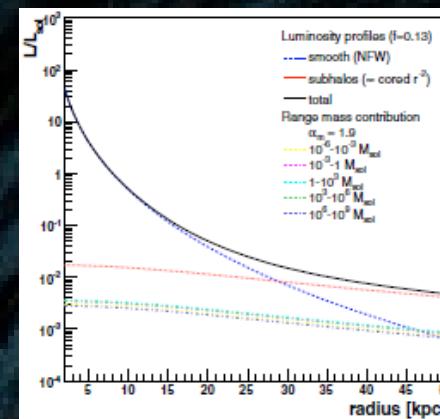
Luminosity per mass decade

$$\frac{d\mathcal{L}}{d \ln M} \propto N_{\text{tot}} \times M \times \frac{d\mathcal{P}_M(M)}{dM} \times \xi(M)$$

$\Leftarrow$  Impact of  $M_{\min}$  depends on  $\alpha$  :  
 $\alpha \sim 1.9$ : constant luminosity per mass decade  
 $\alpha \sim 2.0$ : luminosity dominated by small objects

Similar dependence

$$\xi_{\text{NFW}}(M) \approx M^{0.9} \implies \langle \xi_{\text{NFW}} \rangle \approx M_{\min}^{1.9-\alpha}$$



# Spatial distribution: a self-consistent method

Trivial cases:

- 1) given from N-body analysis (still to check consistency)
- 2) subhalos track the host halo:  $dP/dV = \rho(r)/M_{\text{MW}}$

(i) Global fit to the N-body simulation (eg NFW)

$$\rho_{\text{MW}}(r) \text{ such that } 4\pi \int dr r^2 \rho_{\text{MW}}(r) = M_{\text{MW}}$$

(ii) Adding subhalos means splitting the global fit into a smooth + clumpy components

$$\text{Adding subhalos} \Rightarrow \rho_{\text{MW}}(r) = \rho_{\text{sm}}(r) + \rho_{\text{sub}}(r)$$

**Warning !!!**

$$\rho_{\text{sm}}(r) \neq (1 - f_{\text{sub}})\rho_{\text{MW}}(r)$$

often assumed = in the past

$$\rho_{\text{sm}}(r) \text{ such that } 4\pi \int dr r^2 \rho_{\text{sm}}(r) = (1 - f_{\text{sub}}) M_{\text{MW}}$$

$$\rho_{\text{sub}}(r) \text{ such that } 4\pi \int dr r^2 \rho_{\text{sub}}(r) = f_{\text{sub}} M_{\text{MW}}$$

(iii) Use N-body prescriptions: subhalo distribution cored in the center.

in Via Lactea, **antibiased** relation: subhalo distrib  $\propto r \times$  global ~~smooth~~ **smooth** distrib

$$\left\{ \begin{array}{l} \rho_{\text{sm}}(r) = \frac{\rho_{\text{MW}}(r)}{(1 - r/r_b)} \propto \begin{cases} r^{-1} & \text{for } r \lesssim r_b \sim r_s \\ r^{-4} & \text{for } r \gtrsim r_b \sim r_s \end{cases} \\ \rho_{\text{sub}}(r) = \frac{\rho_{\text{MW}}(r)(r/r_b)}{(1 - r/r_b)} \propto \begin{cases} \text{cst} & \text{for } r \lesssim r_b \sim r_s \\ r^{-3} & \text{for } r \gtrsim r_b \sim r_s \end{cases} \end{array} \right.$$

# Spatial distribution: a self-consistent method

Trivial cases:

- 1) given from N-body analysis (still to check consistency)
- 2) subhalos track the host halo:  $dP/dV = \rho(r)/M_{\text{MW}}$

(i) Global fit to the N

$\rho_{\text{MW}}(r)$  such that  $4\pi$

(ii) Adding subhalos means splitting the global fit into a smooth + clumpy components

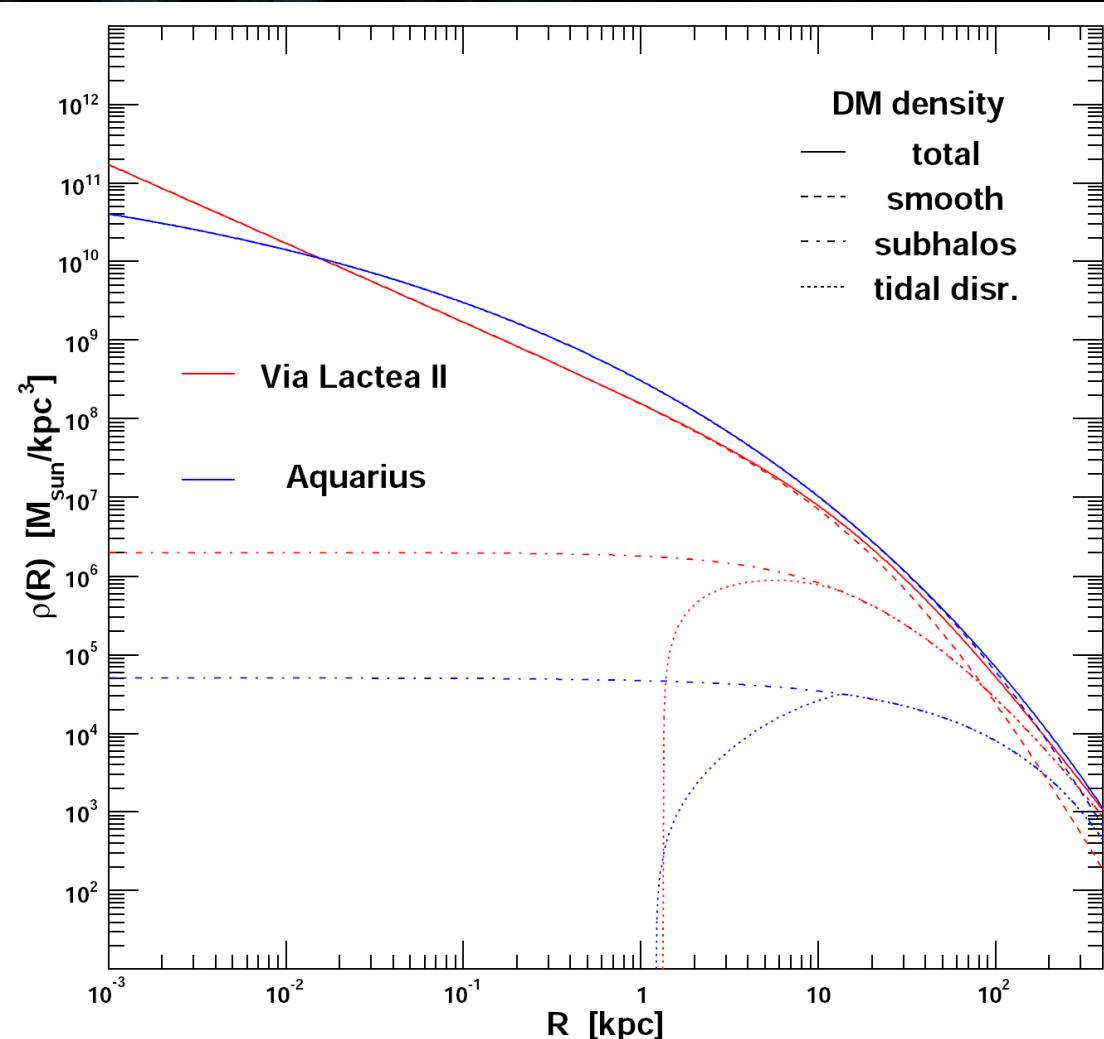
$$\text{Adding subhalos} \Rightarrow \rho_{\text{MW}}(r) = \rho_{\text{sm}}(r) +$$

$$\rho_{\text{sm}}(r) \text{ such that } 4\pi \int dr r^2 \rho_{\text{sm}}(r) = (1 - f_s)$$

$$\rho_{\text{sub}}(r) \text{ such that } 4\pi \int dr r^2 \rho_{\text{sub}}(r) = f_{\text{sub}} M$$

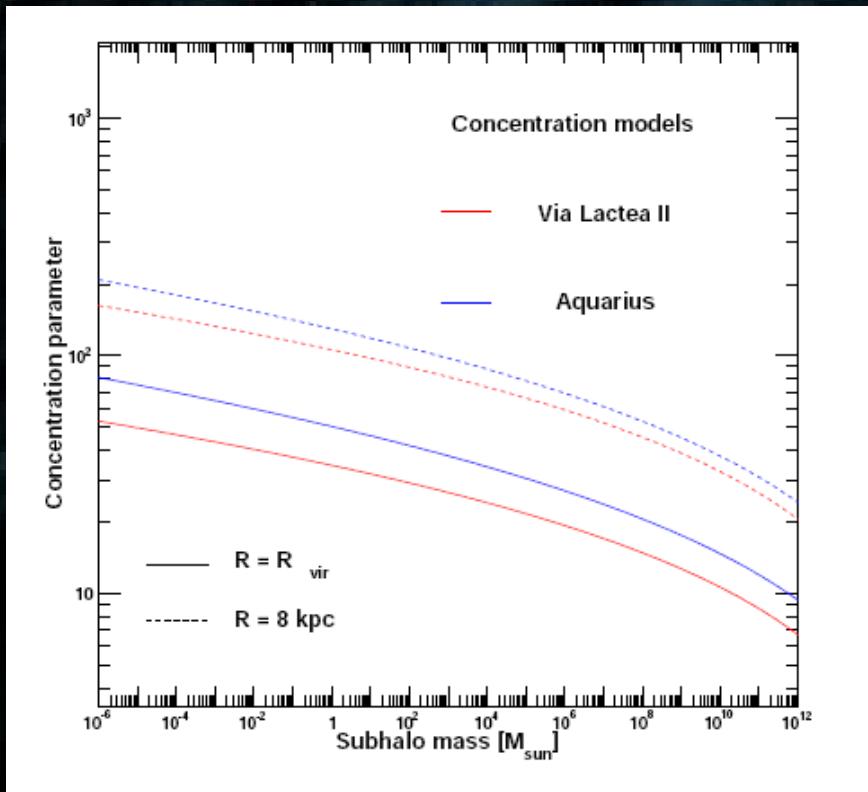
(iii) Use N-body prescriptions: subhalos in Via Lactea, **antibiased** relation

$$\left\{ \begin{array}{l} \rho_{\text{sm}}(r) = \frac{\rho_{\text{MW}}(r)}{(1 - r/r_b)} \\ \rho_{\text{sub}}(r) = \frac{\rho_{\text{MW}}(r)(r_s - r)}{(1 - r/r_b)} \propto \begin{cases} r^{-3} & \text{for } r \gtrsim r_b \sim r_s \end{cases} \end{array} \right.$$

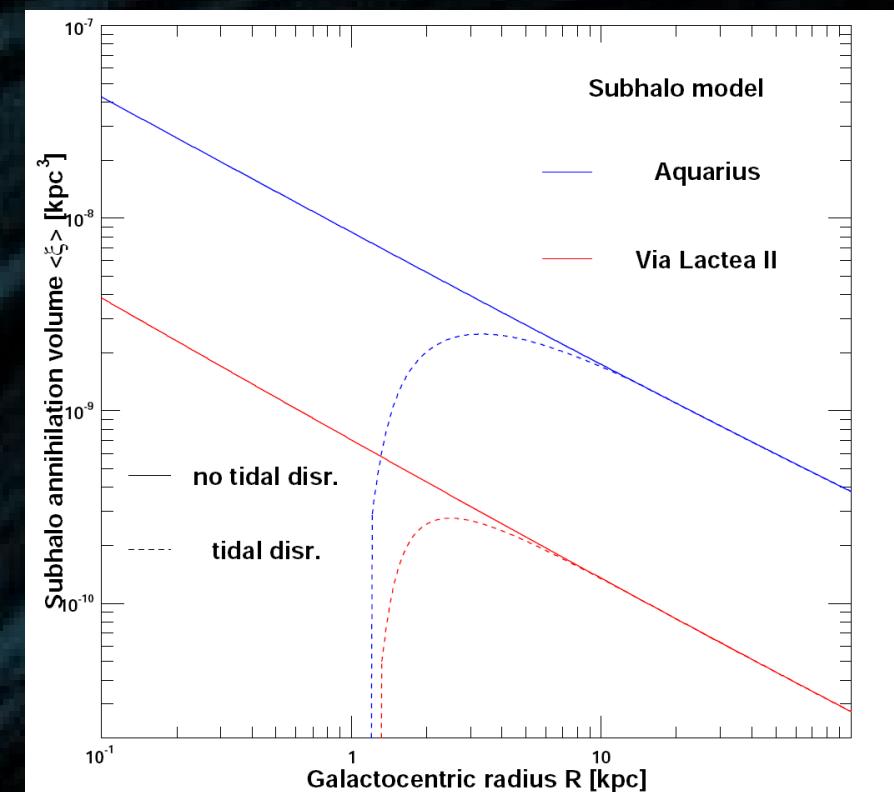


# Concentration function

Concentration vs mass and location in the MW



Average subhalo luminosity vs distance to GC



## Concentrations:

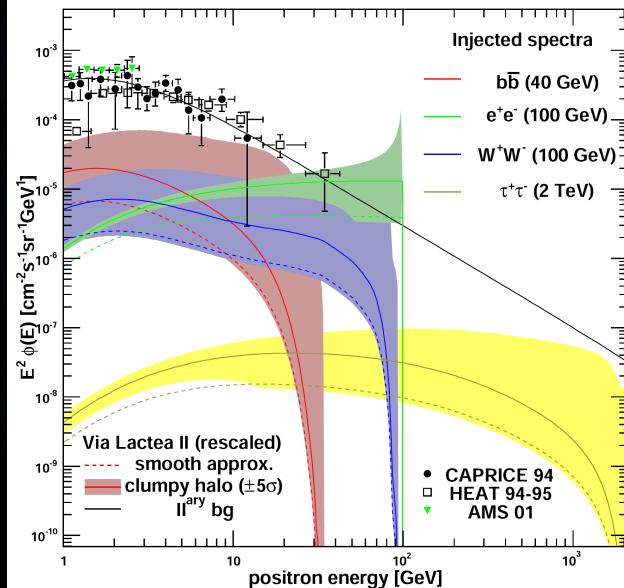
- 1) Large theoretical uncertainties (impact of cosmological inputs).
- 2) Tidal effects: concentrations get larger when closer to the GC (demonstrated in VL2 and Aquarius).

$$\xi \propto c_{\text{vir}}^3$$

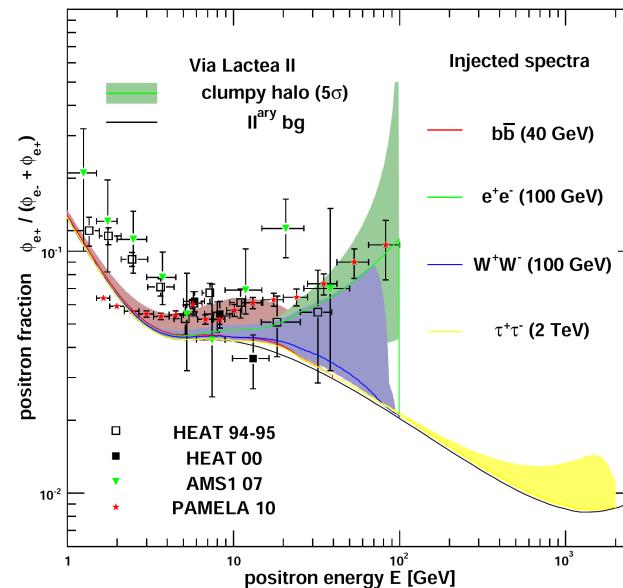
Average luminosity strongly affected!

# Dark Matter subhalos: energy-dependent boost factor < 5 (modulo variance)

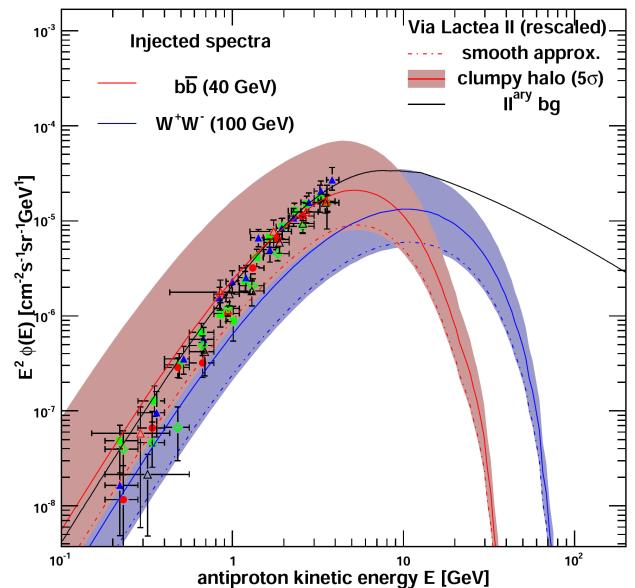
Positron flux



Positron fraction



Antiproton flux



Pieri, JL, Bertone & Branchini (2009)

using results from Via Lactea II (Diemand et al) and Aquarius (Springel et al)  
-- see early calculations in Lavalle et al (2007-2008) --

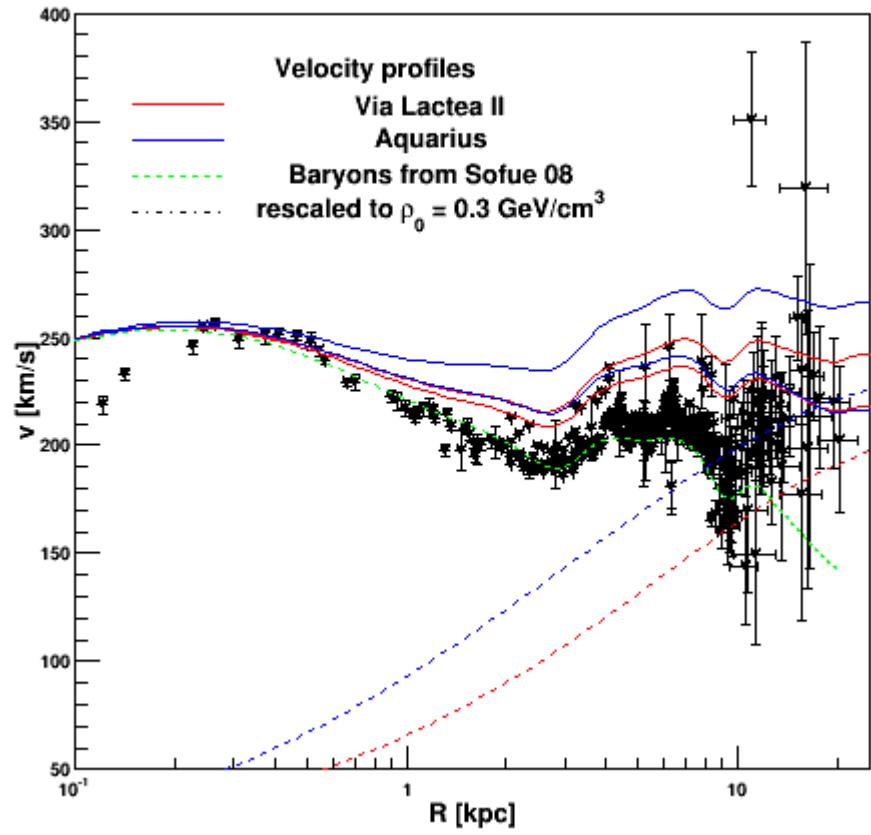
## Important features:

- 40 GeV WIMP ( $b\bar{b}$ ) excluded by antiproton constraints
- 100 GeV WIMP ( $WW$ ) at the edge of tension with the antiproton data
- 100 GeV WIMP going to  $e^+e^-$  can fit the PAMELA data; but pulsars not included => background must be known before any claim.

model	$m_\chi$ [GeV]	final state
A	40	$bb$
B	100	$W^+W^-$
C	100	$e^+e^-$
D	2000	$\tau^+\tau^-$

# *High-resolution is not the end of the story: what about baryons?*

VL2/Aquarius + baryons from Sofue et al 09



Kinematics data are available for the MW:  
→ try to use them to improve predictions

## **Subhalos:**

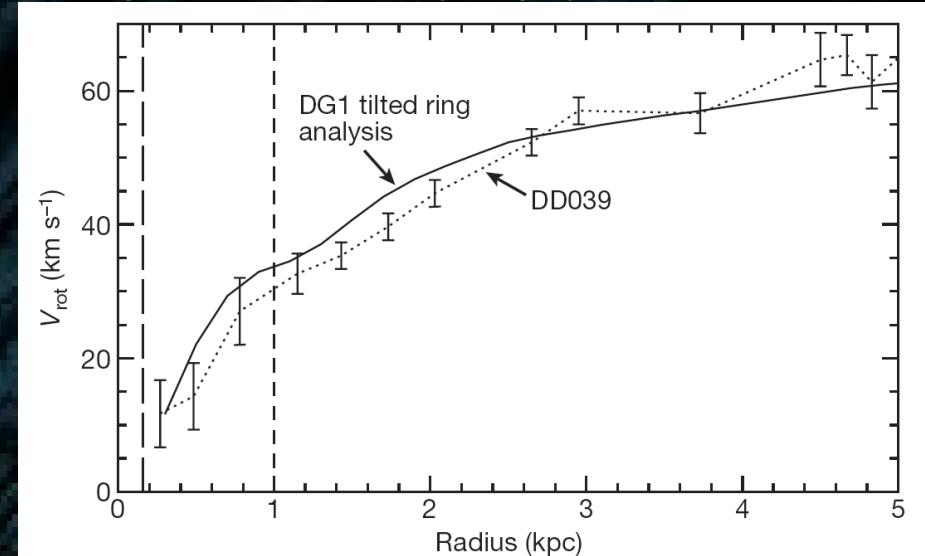
Small scale issue + more efficient tidal stripping in the disk and the bulge leading to a dark disk (cf Read et al)

## **Galactic center:**

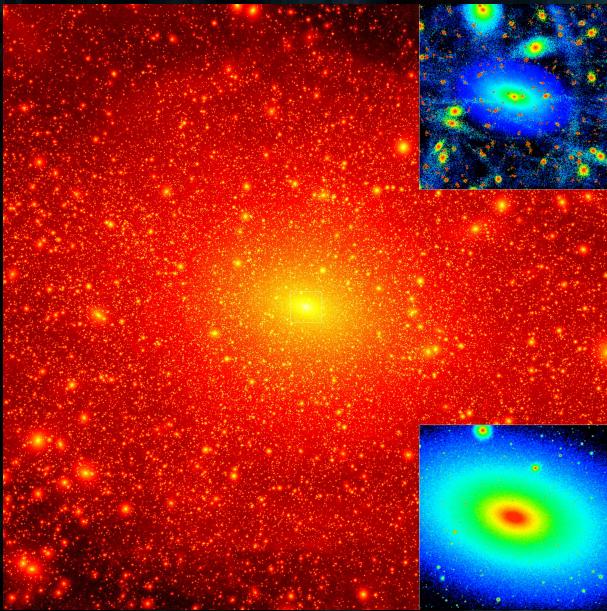
Adiabatic compression might increase the DM density, but competition with dynamical friction from SF feedback re-heating the gas.

=> **Still large uncertainties**

Governato et al 10:  
CDM + high-resolution baryon physics can lead to cores



# *Dark matter inhomogeneities wandering around ?*



Via Lactea (Diemand et al)

## Mini-dark halos with intermediate mass black holes

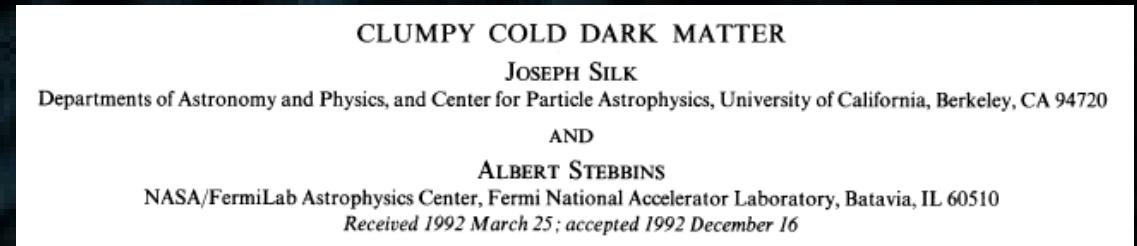
HongSheng Zhao and Joseph Silk  
(Dated: 1 June 2005 on Phys. Rev. Letters 95, 011301)

Further developed by Bertone et al

Vol 460 | 2 July 2009 | doi:10.1038/nature08083

## An intermediate-mass black hole of over 500 solar masses in the galaxy ESO 243-49

Sean A. Farrell<sup>1,2†</sup>, Natalie A. Webb<sup>1,2</sup>, Didier Barret<sup>1,2</sup>, Olivier Godet<sup>3</sup> & Joana M. Rodrigues<sup>1,2</sup>

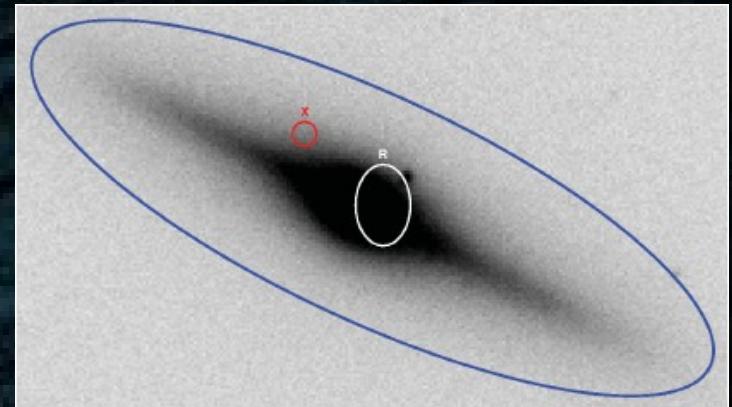


cores in globular clusters, and in galactic nuclei. The enhanced annihilation rate in clumps can lead to a significant contribution to the diffuse  $\gamma$ -ray background, as well as emission from the Galactic center. Results from terrestrial dark matter detection experiments might be significantly affected by clumpiness in the Galactic halo.



### Two main cases:

- Collective effect.
- A very bright single objects
- (excluded from gamma-ray data,  
•Bringmann, Lavalle & Salati 09)

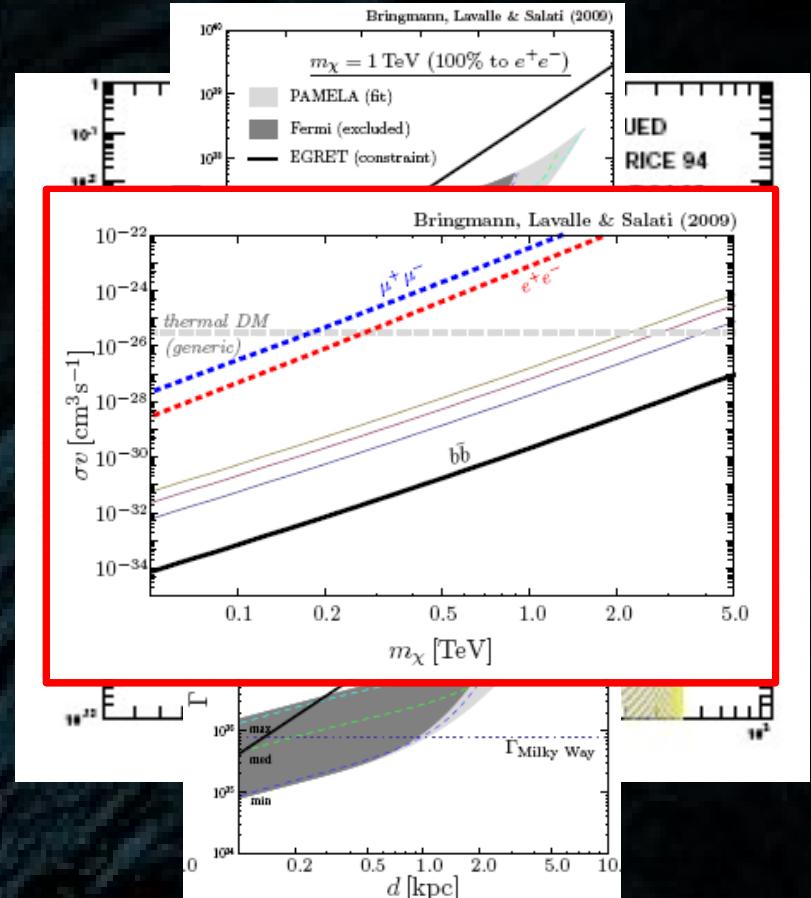
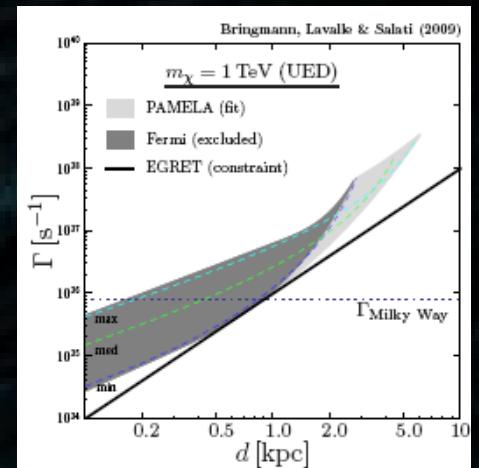
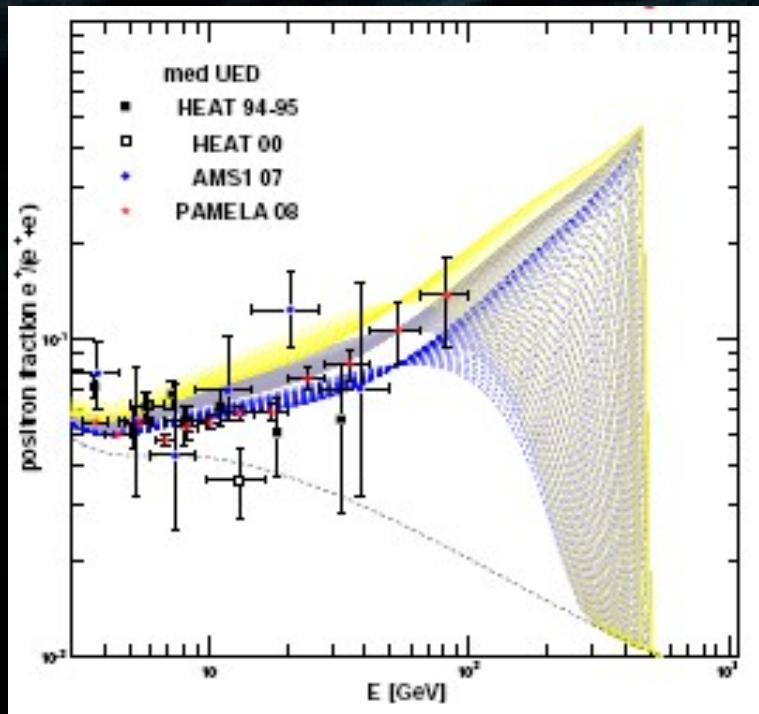


# Single object wandering around

## The game one can play:

- Assume a single DM source at any distance  $d$  to the Earth.
- Assume a WIMP mass and its annihilation final states.
- Search for the brightness necessary to fit PAMELA.
- Check against other data (gamma, antiprotons, etc.)

Bringmann, Lavalle & Salati (2009)



# *Boost factor: a simplistic view*

A large blue circle representing a smooth galaxy.

Smooth galaxy

A blue circle with a dense pattern of small, dark dots representing a clumpy galaxy.

Clumpy galaxy

$$\langle \rho(\vec{x}) \rangle \stackrel{\text{assumption}}{=} \rho(\vec{x})$$

**Usual assumption:** simulations provide us with the net density profile function  $\rho(r)$   
=> keep in mind that it comes from a fit of  $\langle \rho \rangle$

$$\Gamma_{\text{ann}}^{\text{smooth}}(\vec{x}) \propto \langle \sigma v \rangle \rho^2(\vec{x}) = \langle \sigma v \rangle \langle \rho(\vec{x}) \rangle^2$$

**If clumps are considered:**  $\Gamma_{\text{ann}}^{\text{clumpy}}(\vec{x}) \propto \langle \sigma v \rangle \rho^2(\vec{x}) = \langle \sigma v \rangle \langle \rho^2(\vec{x}) \rangle$

**This allows to define the so-called boost factor:**

$$\mathcal{B} = \frac{\langle \rho^2 \rangle}{\langle \rho \rangle^2} \geq 1$$