

Black holes as particle detectors



∞ Vítor Cardoso ∞
(CENTRA/Técnico & Perimeter)

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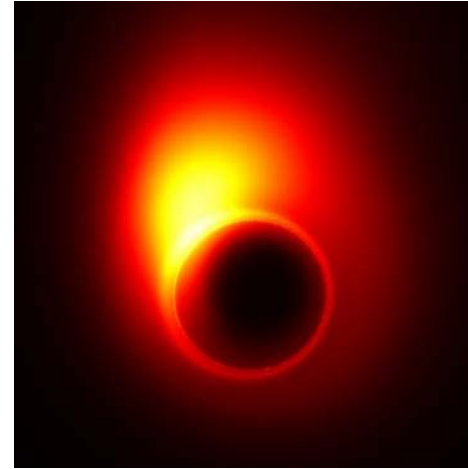
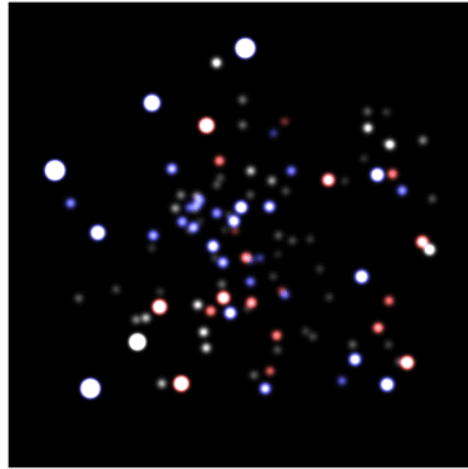
Quy Nhon, Vietnam

Cardoso, Gualtieri, Herdeiro & Sperhake
Exploring New Physics Frontiers Through Numerical Relativity,
Liv. Rev. Relativity; arXiv:1409.0014

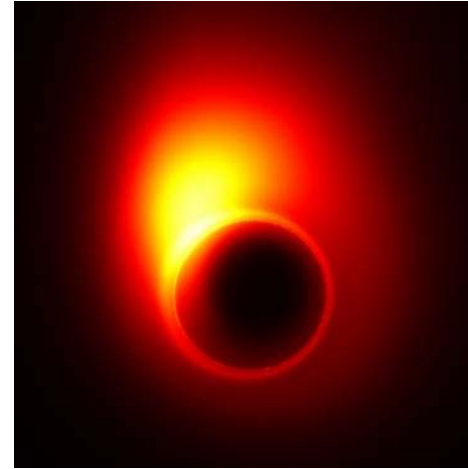
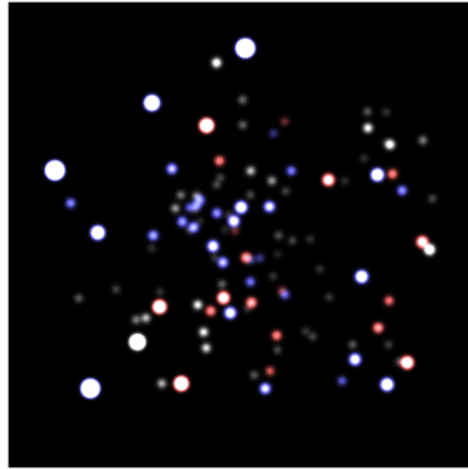
Brito, Cardoso & Pani,
Superradiance,
Springer-Verlag (2015); arXiv:1501.06570

Berti et al,
Testing General Relativity with Present and Future Observations,
arXiv:1501.07274

Black holes exist



Black holes exist

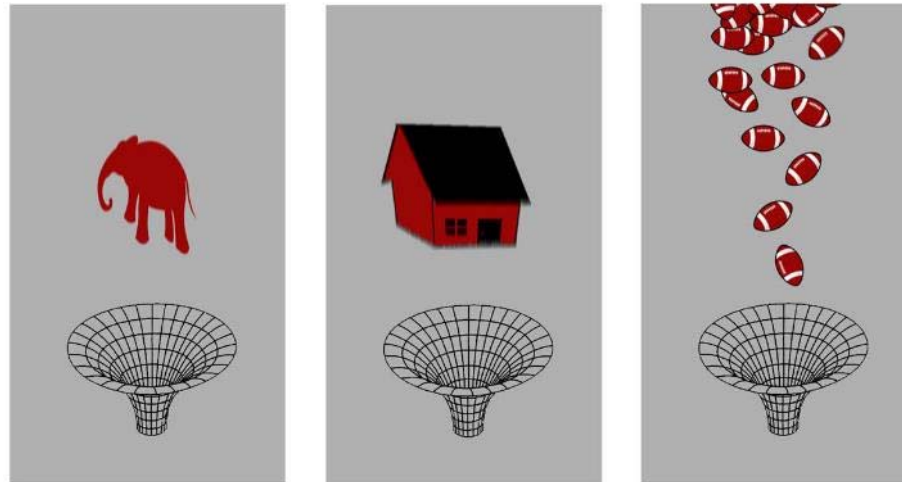


Black holes have no hair

One star made of matter and other of antimatter, produce identical BHs.

A stationary BH is characterized by only three quantities:

mass, spin and electric charge



Note: B & L numbers are also non-conserved in black hole physics

Why study dynamics

Gravitational-wave detection, GW astrophysics

Fundamental physics

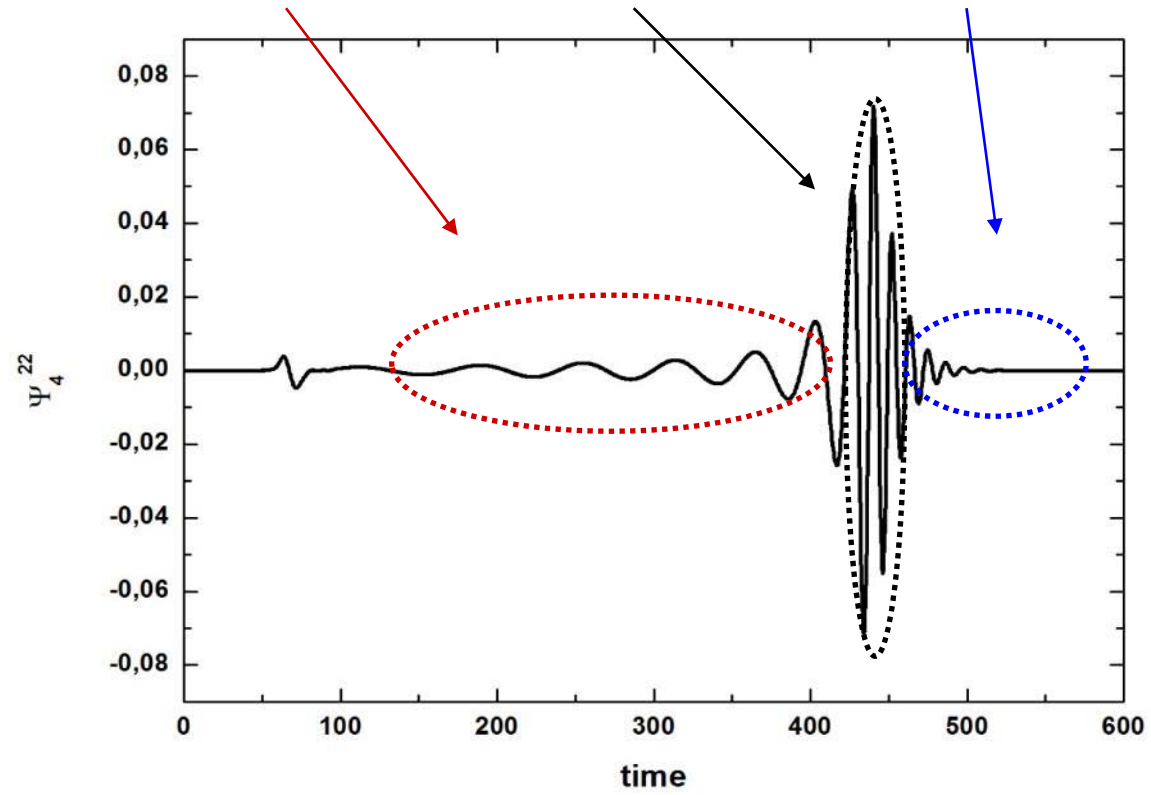
High-energy physics

Particle physics

Inspiral

Merger

Ringdown

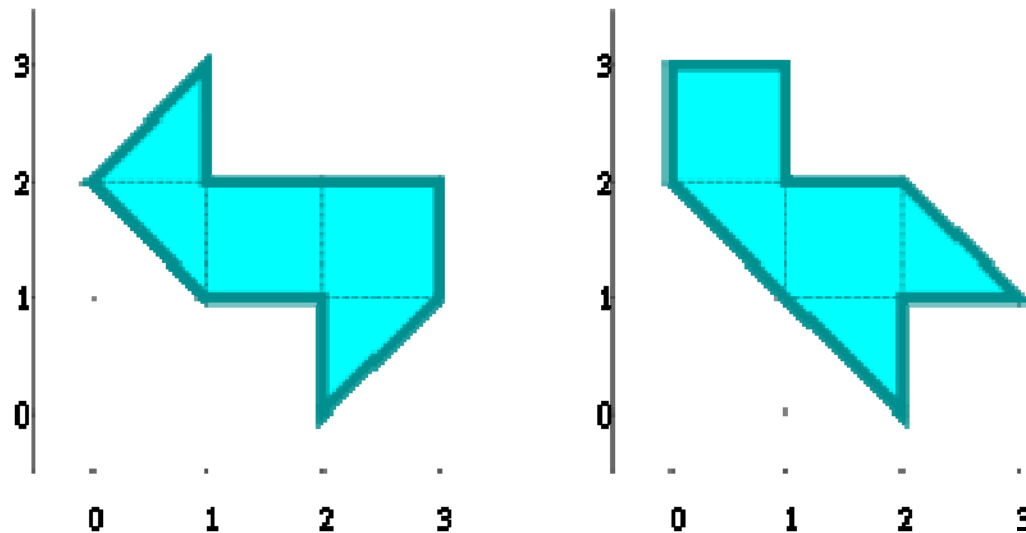


“Can one hear the shape of a drum?”

Mark Kac, American Mathematical Monthly, 1966

$$A = (2\pi)^d \lim_{R \rightarrow \infty} \frac{N(R)}{R^{d/2}}$$

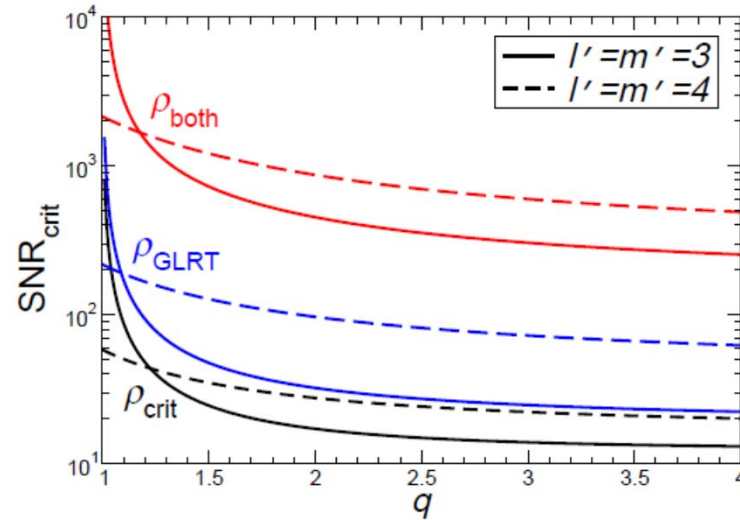
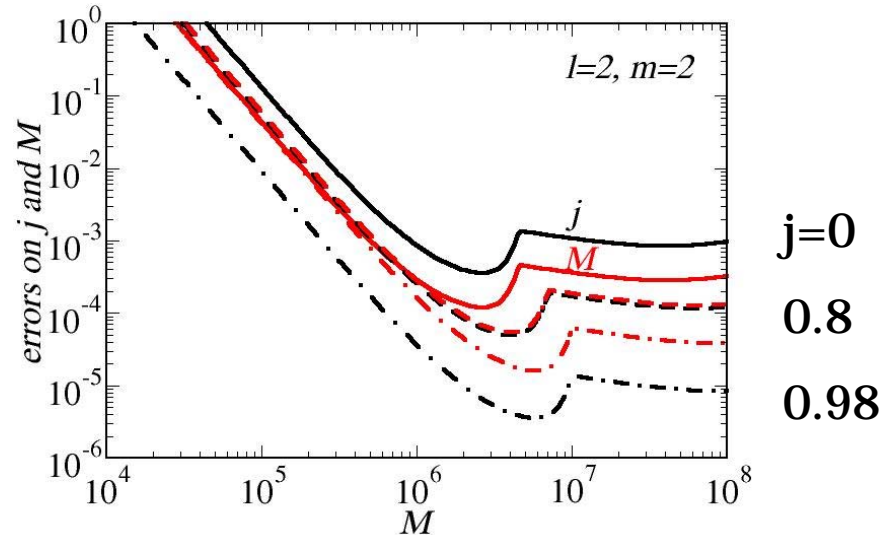
H. Weyl 1911



Gordon, Webb & Wolpert, Inventiones Mathematicae 1992

Can one hear the shape of a BH?

$D_L = 3\text{Gpc}$, $\epsilon_{\text{rd}} = 3\%$



Berti et al PRD76, 104044(2007)

$$\begin{aligned} \epsilon &= 10^{-2}\% \\ M &= 10^6 M_{\odot} \quad \sigma_{j,M} = 1\% \\ j &= 0.8 \end{aligned}$$

Berti, Cardoso & Will PRD73, 064030(2005)

Kamaretsos et al PRD85, 024018 (2012)

Stability, spectroscopy?



Cosmic Censorship?



New dynamical, long-term stable solutions?

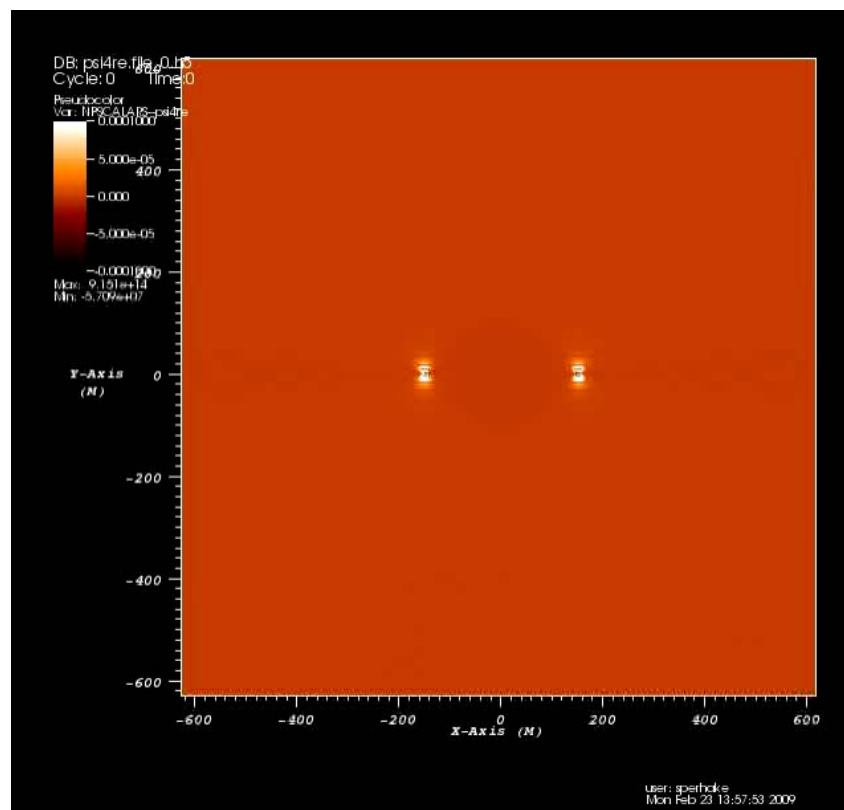


Universal limit on maximum luminosity c^5/G (10^{59} erg/sec)

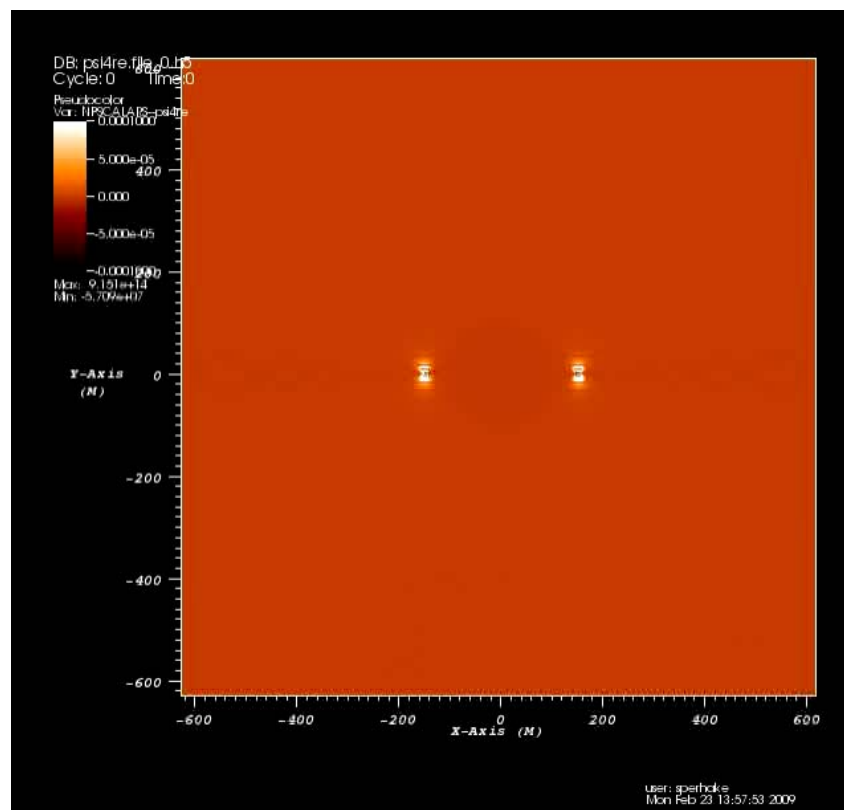
Barrow & Gibbons MNRAS 446, 3874 (2015)



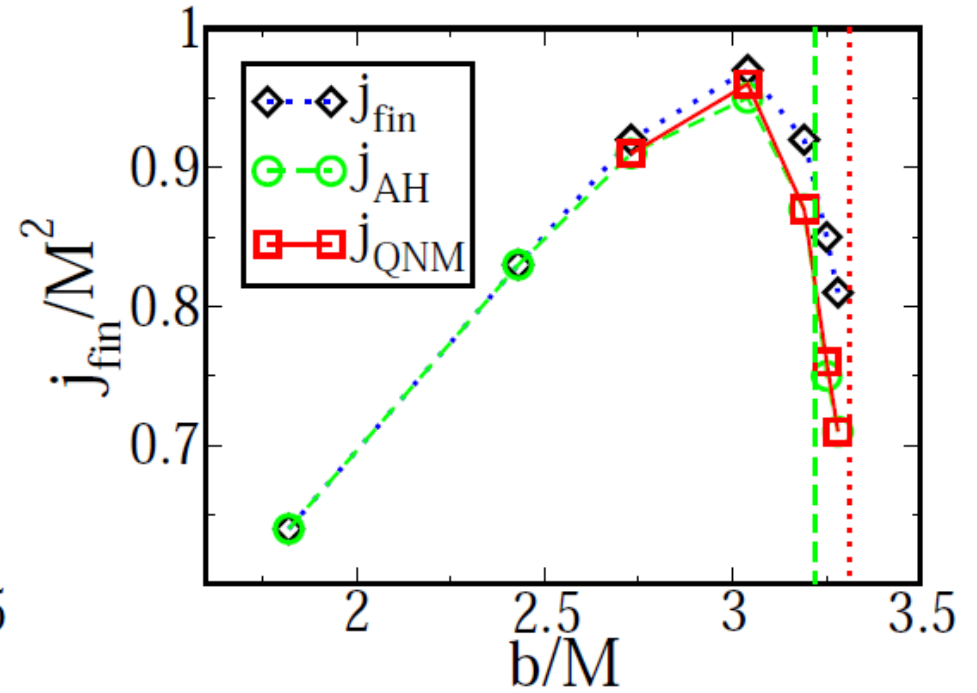
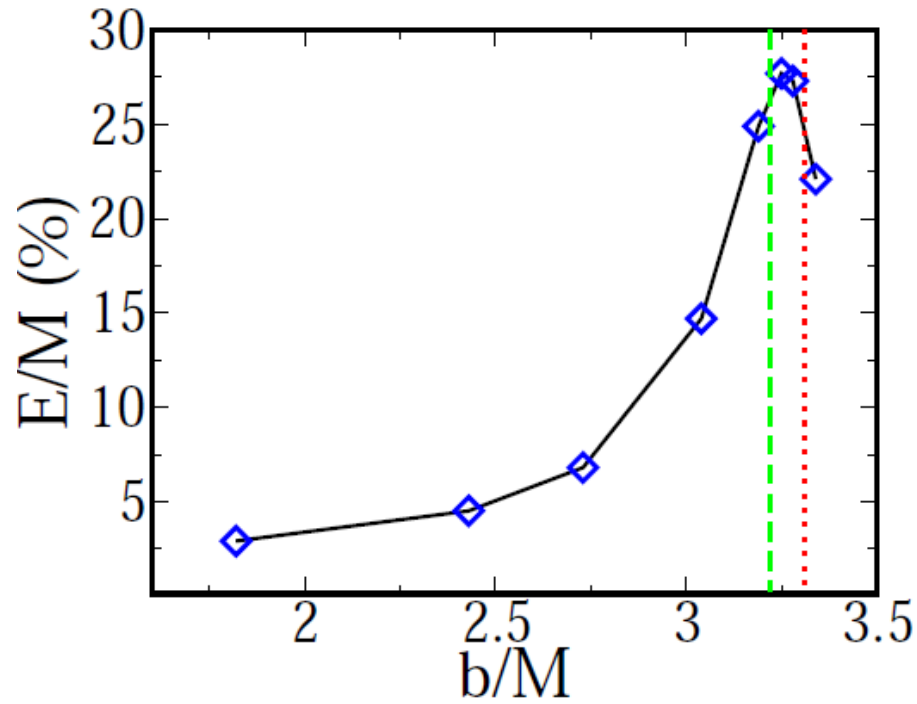
Critical behavior, etc



Sperhake et al PRL 2009, 2013



Sperhake et al PRL 2009, 2013



More than 25% (35%) CM energy radiated for $v=0.75 c$ ($0.92c$)!

Final BH rapidly spinning

Strong field and fundamental fields

Massive scalars

Interesting as effective description; proxy for more complex interactions

Arise as interesting extensions of GR* (*BD or generic ST theories; $f(R)$*)

DM candidates (*boson and soliton stars, Axiverse scenarios - moduli and coupling constant in string theory, Peccei-Quinn mechanism in QCD*)

Plan

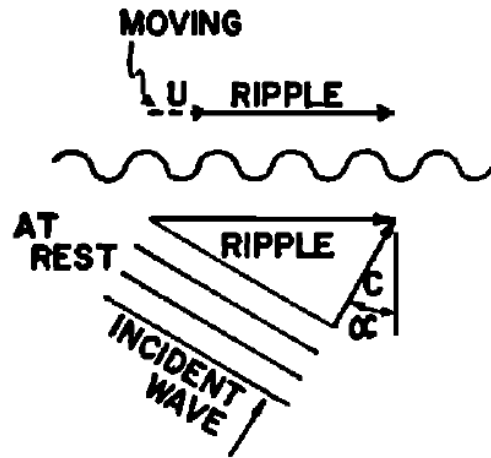
Energy extraction, bound states; evading no-hair theorems

Accretion and gravitational-wave emission

Bounds on ultra-light fields

* *Poorly constrained for massive fields*

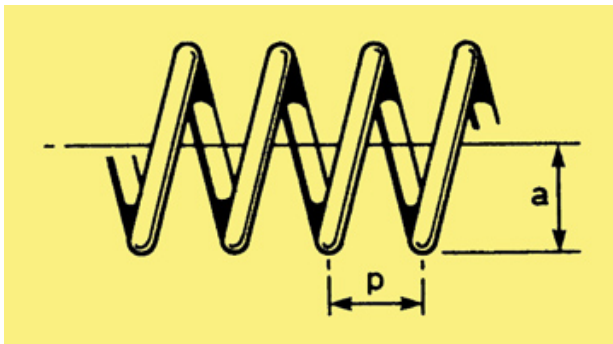
Friction & superradiance



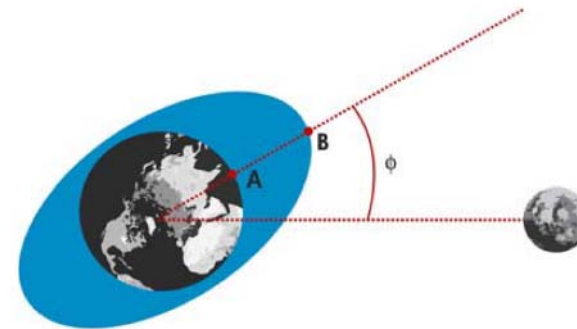
Ribner, J. Acous. Soc. Amer. 29 (1957)



Tamm & Frank, Doklady AN SSSR 14 (1937)

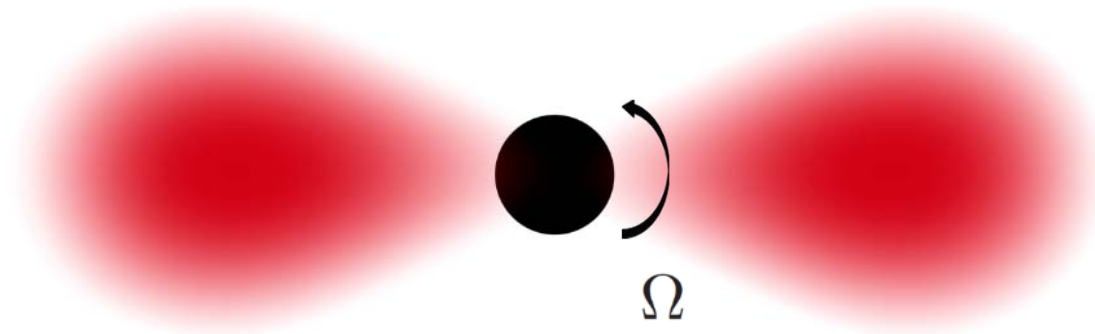


Pierce (& Kompfner), Bell Lab Series (1947)
Ginzburg, anomalous Doppler year



G. H. Darwin, Philos. Trans. R. Soc. London 171 (1880)

$$\Phi \sim e^{-i\omega t + im\phi} \rightarrow (\text{Angular}) \text{ phase velocity} = \frac{\omega}{m}$$

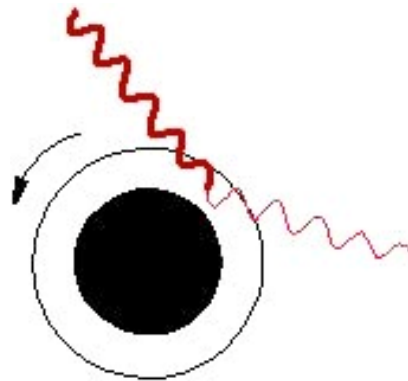


$$\omega < m\Omega$$

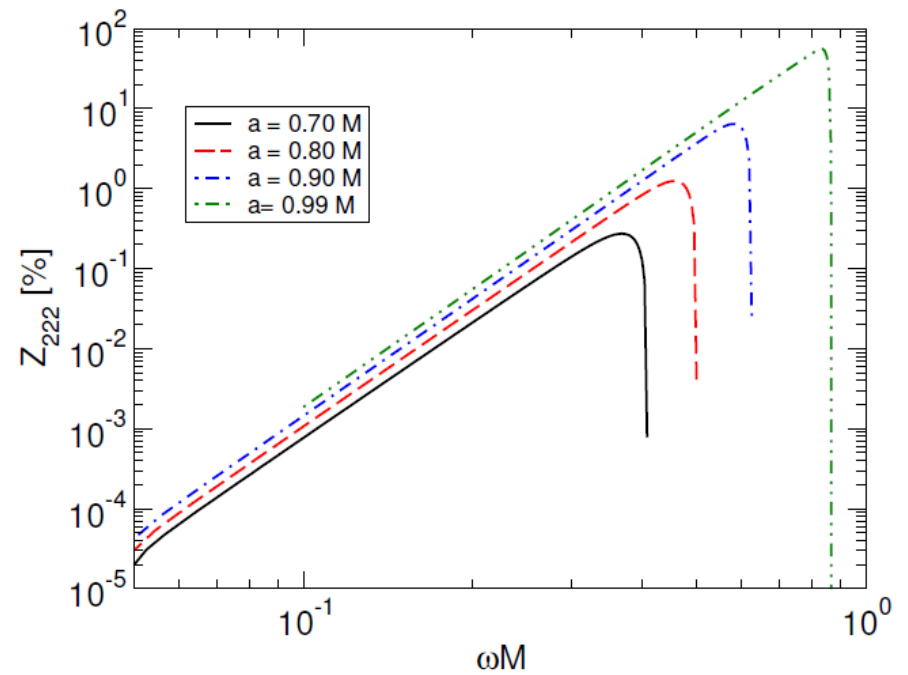
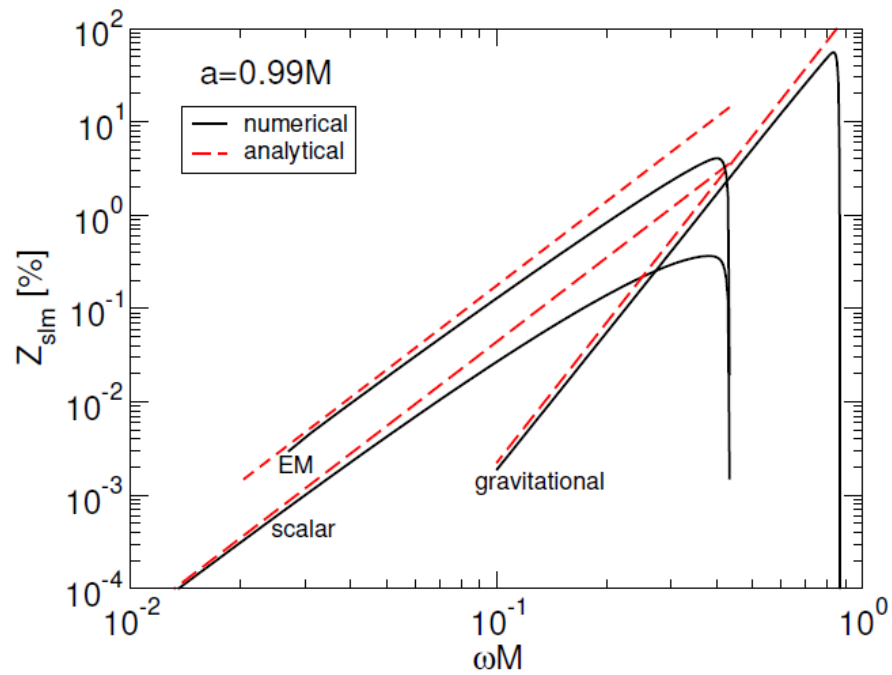
Zel'dovich, Pis'ma Zh. Eksp. Teor. Fiz. 14 (1971)

Black holes and superradiance

Friction built-in through one-way membrane (horizon)



Zel'dovich, Pis'ma Zh. Eksp. Teor. Fiz. 14 (1971), Brito et al, arXiv:1501.06570



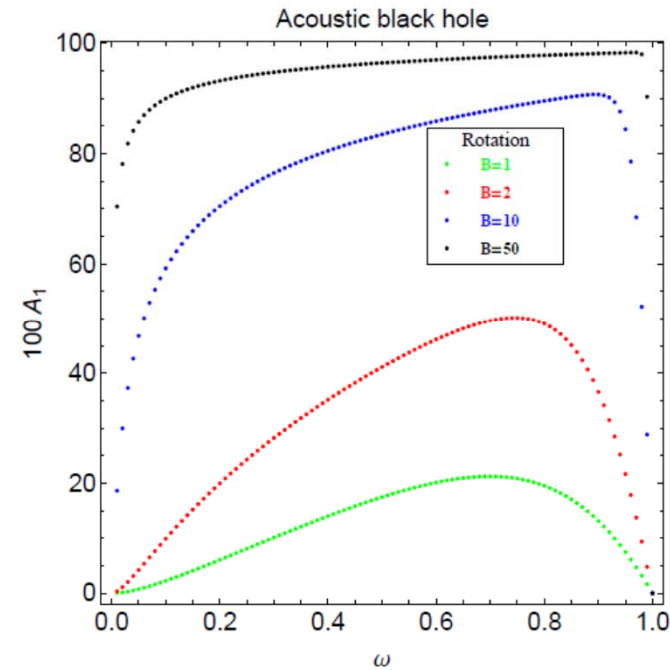
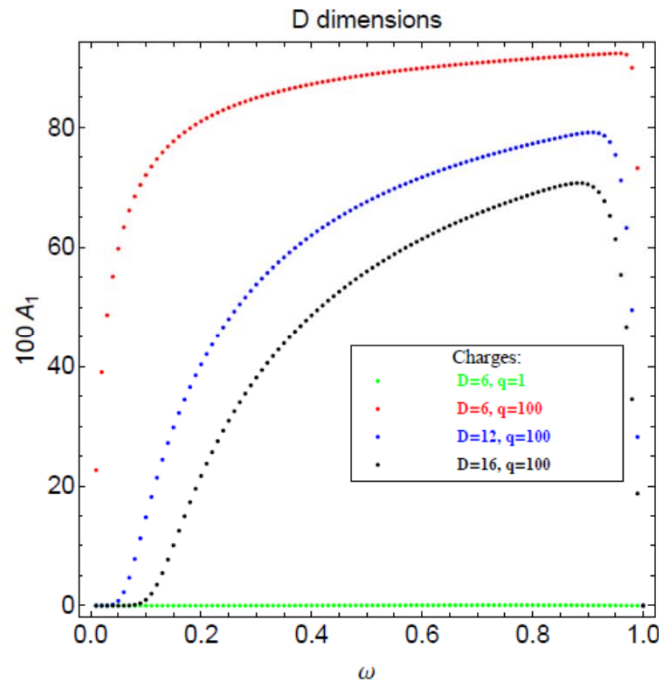
Brito, Cardoso & Pani, arXiv:1501.06570

(Rotational) superradiance in the lab?



Need absorbing surface, characterized by complex acoustic impedance Z

Cardoso, Coutant , Richartz & Weinfurtner, in progress



Amplification < 100%...fundamental bound on superradiance?

$$(\nabla_{\mu} - iqA_{\mu}) (\nabla^{\mu} - iqA^{\mu}) \Psi = 0$$

$$\frac{d^2 X}{dx^2} + \left[(\omega - qA_0)^2 - V \right] X = 0$$

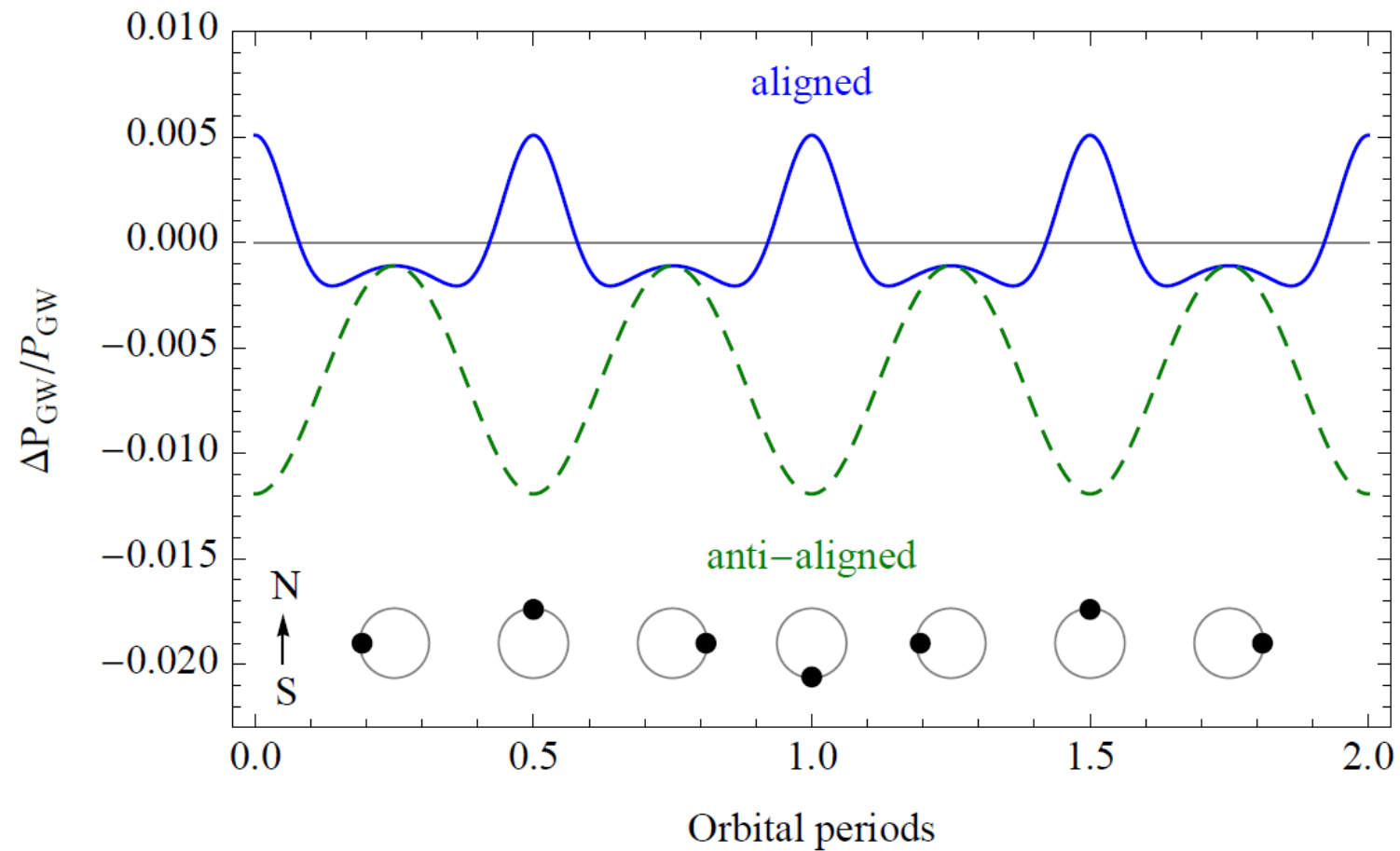
Baibhav, Cardoso and Emparan, in progress

Binaries?

Backreaction?

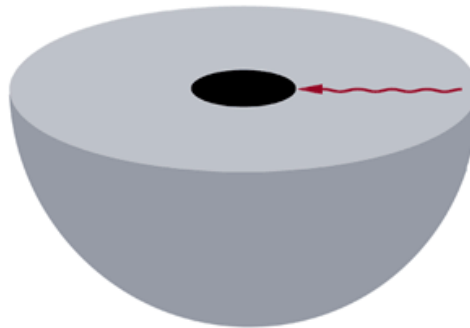
Superradiance in stars?

Direct observational effects?



Superradiant instabilities

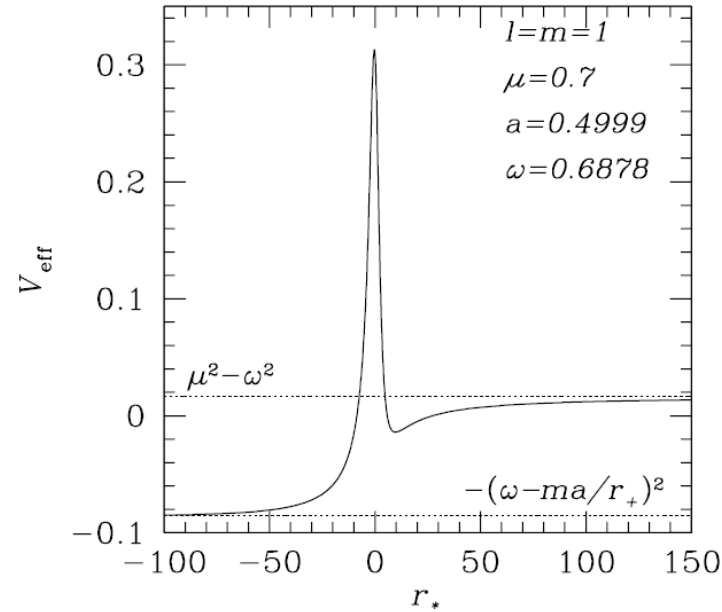
Can construct unstable states by forcing wave to bounce back



© A.S. Dybko

Zel'dovich, Pis'ma Zh. Eksp. Teor. Fiz. 14 (1971);

Cardoso & Dias, PRD70 (2004) ; Brito, Cardoso & Pani, arXiv:1501.06570



$$\omega_{\text{res}}^2 = \mu_s^2 - \mu_s^2 \left(\frac{\mu_s M}{l+1+n} \right)^2 \quad \omega_I = \mu_s \frac{(\mu_s M)^8}{24} (a/M - 2\mu_s r_+)$$

Massive “states” around Kerr are linearly unstable

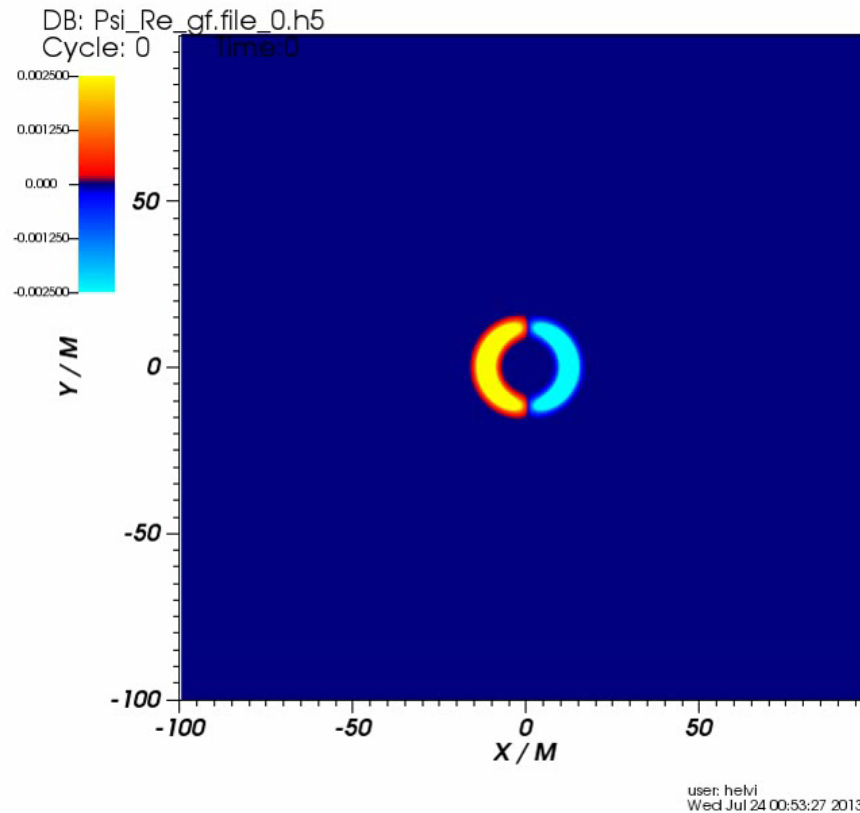
Damour et al '76; Detweiler PRD; Cardoso & Yoshida JHEP0507 (2005) 009

Dolan PRD76 (2007) 084001; Witek et al, PRD87 (2013) 4, 043513;

Cardoso, Carucci, Pani, Sotiriou PRL111 (2013) 111101

See reviews Brito et al arXiv:1501.06570 and Yoshino and Kodama arXiv:1505:00714

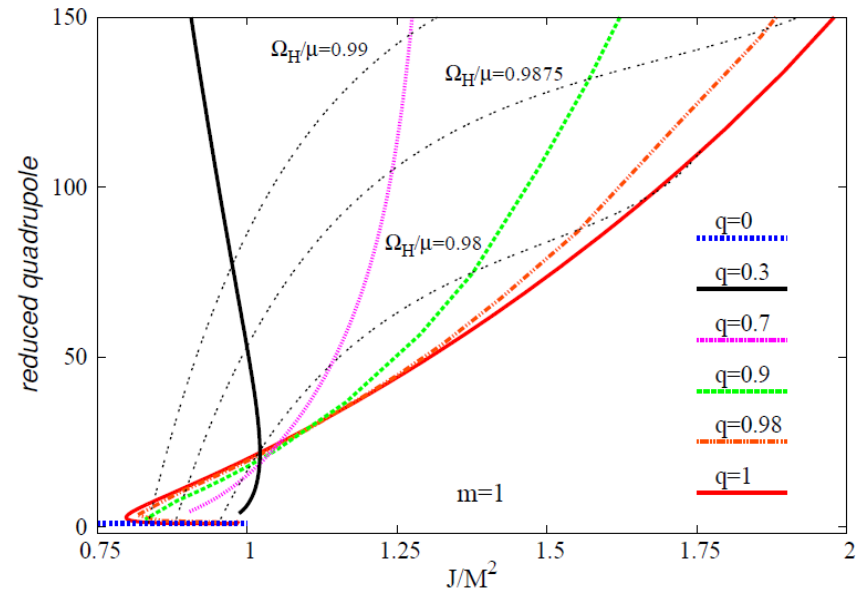
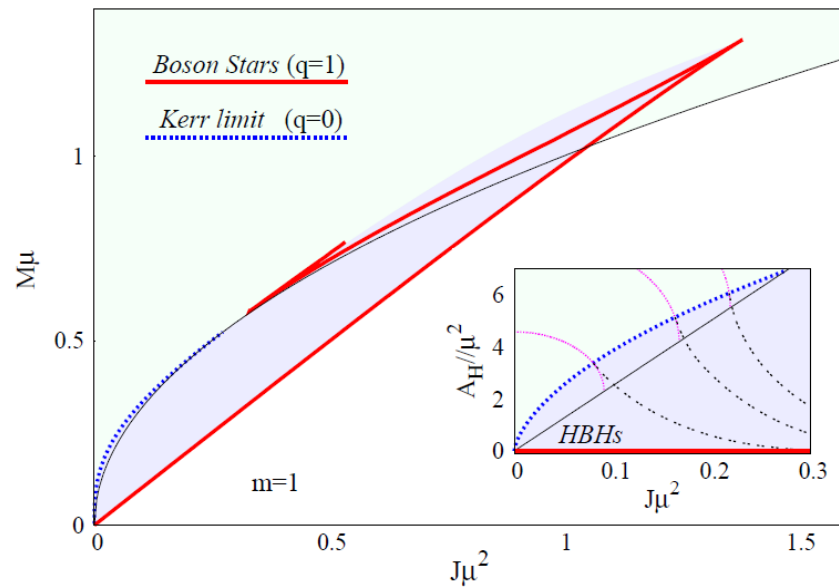
Final state I: almost-hairy BHs



$$\Psi = e^{-i\omega t} Y_{lm}(\theta, \phi) \psi(r)$$
$$T^{\mu\nu} = -g^{\mu\nu} (\Psi^*_{,\alpha} \Psi^{,\alpha} + \mu^2 \Psi^* \Psi) + \Psi^{*,\mu} \Psi^{,\nu} + \Psi^{,\mu} \Psi^{*,\nu}$$

Okawa et al PRD89, 104032 (2014)

Final state II: hairy black holes?



Herdeiro & Radu, *PRL*112, 221101 (2014)

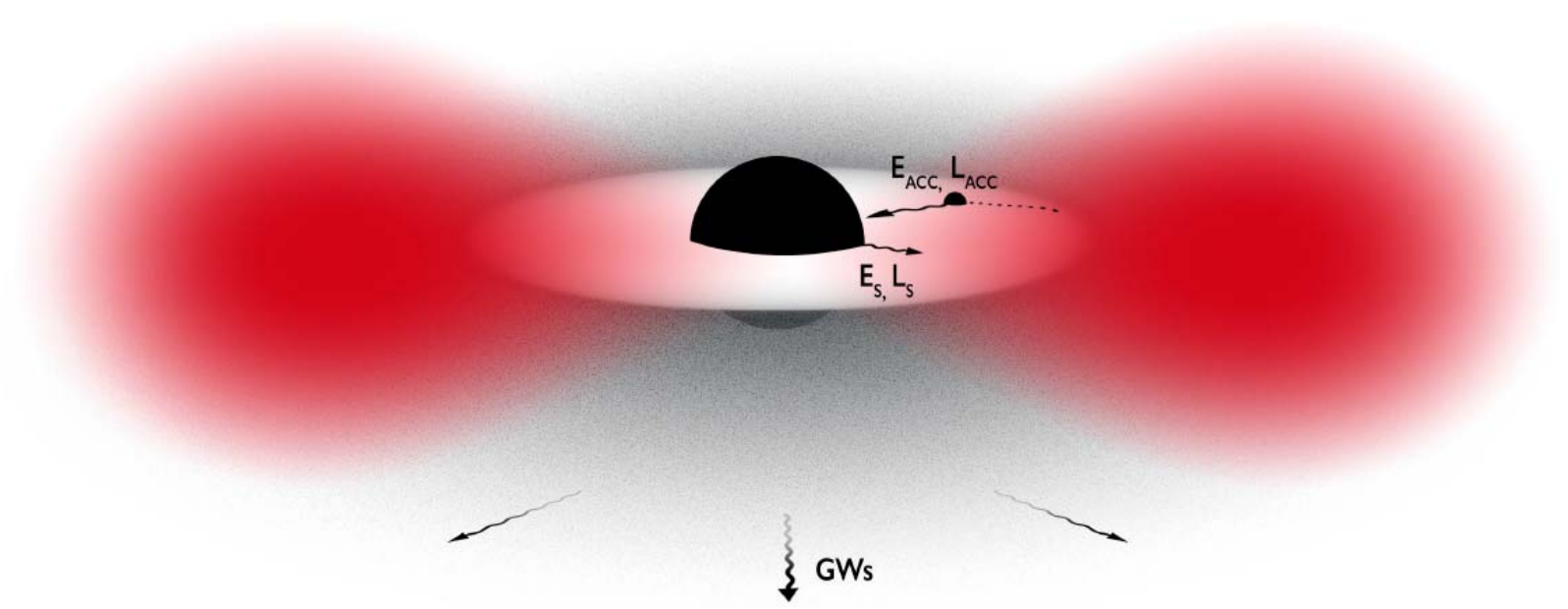
Are themselves unstable in parts of the parameter space

Brito, Cardoso & Pani, arXiv:1501.06570

End-state of linear instability?

Gravitational-wave emission and accretion?

Are hairy solutions formed?



Accretion:

$$\dot{M}_{\text{ACC}} \equiv f_{\text{Edd}} \dot{M}_{\text{Edd}} \sim 0.02 f_{\text{Edd}} \frac{M(t)}{10^6 M_{\odot}} M_{\odot} \text{yr}^{-1}$$

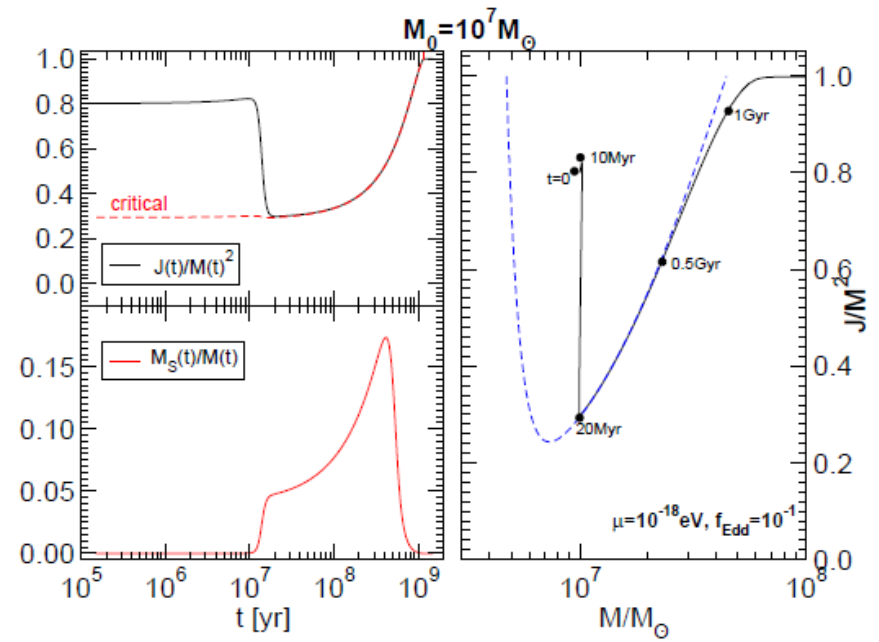
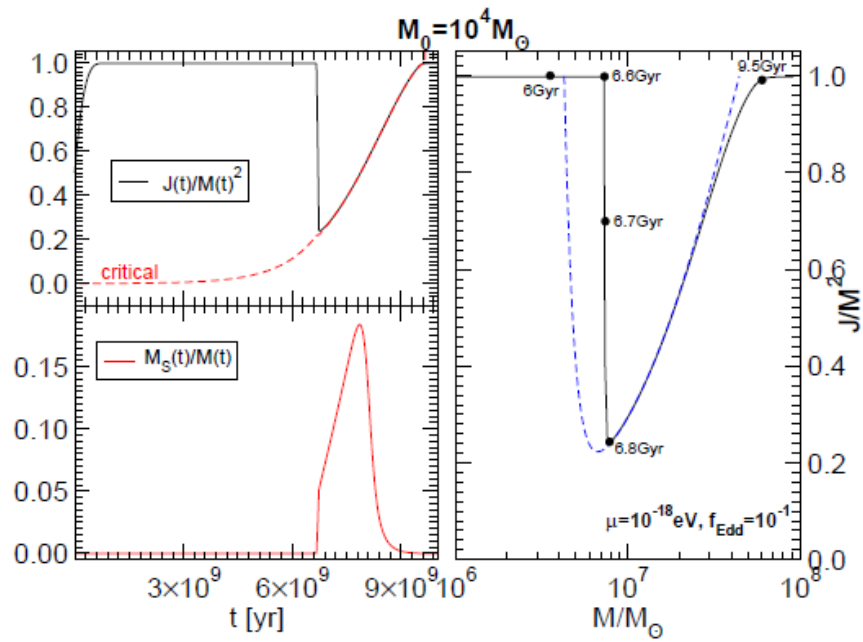
$$\dot{J}_{\text{ACC}} \equiv \frac{L(M, J)}{E(M, J)} \dot{M}_{\text{ACC}}$$

Gravitational-wave emission:

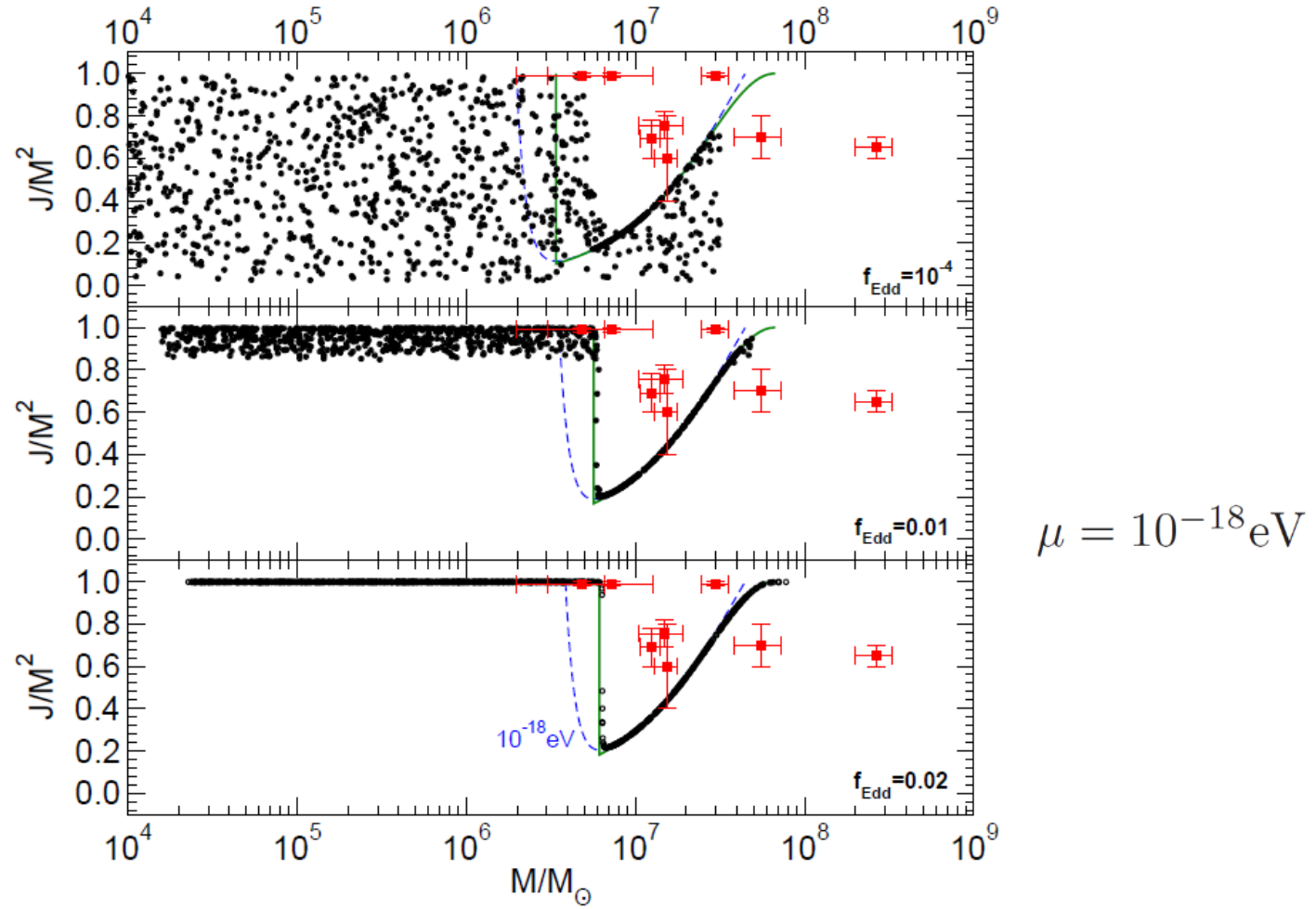
$$\dot{E}_{\text{GW}} = \frac{484 + 9\pi^2}{23040} \left(\frac{M_S^2}{M^2} \right) (M\mu)^{14}$$

$$\dot{J}_{\text{GW}} = \frac{1}{\omega_R} \dot{E}_{\text{GW}}$$

Yoshino & Kodama PTEP 2014 (043E02); Brito et al CQG32 (2015) 13, 134001



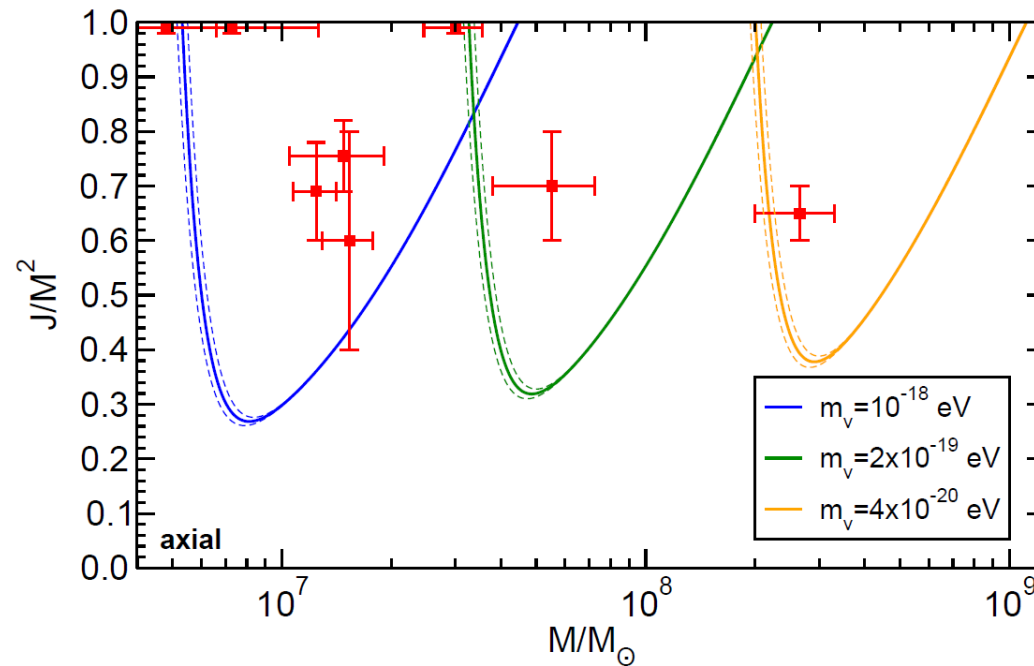
Brito, Cardoso, Pani arXiv:1411.0686



Random distributions 1000 BHs, with initial mass between $\log_{10} M_0 \in [4, 7.5]$ and $J_0/M_0^2 \in [0.001, 0.99]$ extracted at $t = t_F$, with t_F distributed on a Gaussian centered at $\bar{t}_F \sim 2 \times 10^9 \text{yr}$ with width $\sigma = 0.1\bar{t}_F$.

Bounding the boson mass

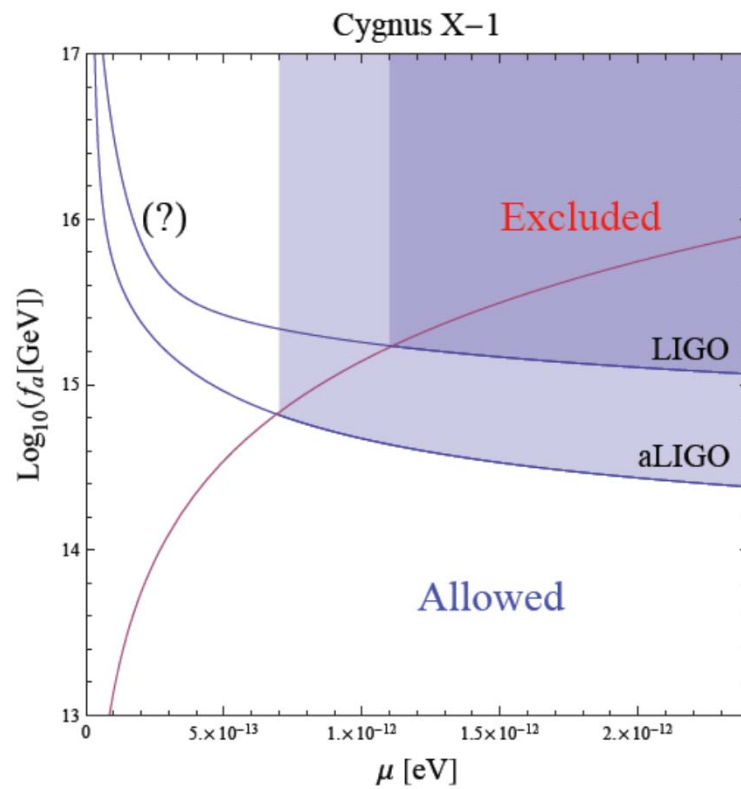
Pani et al PRL109, 131102 (2012)

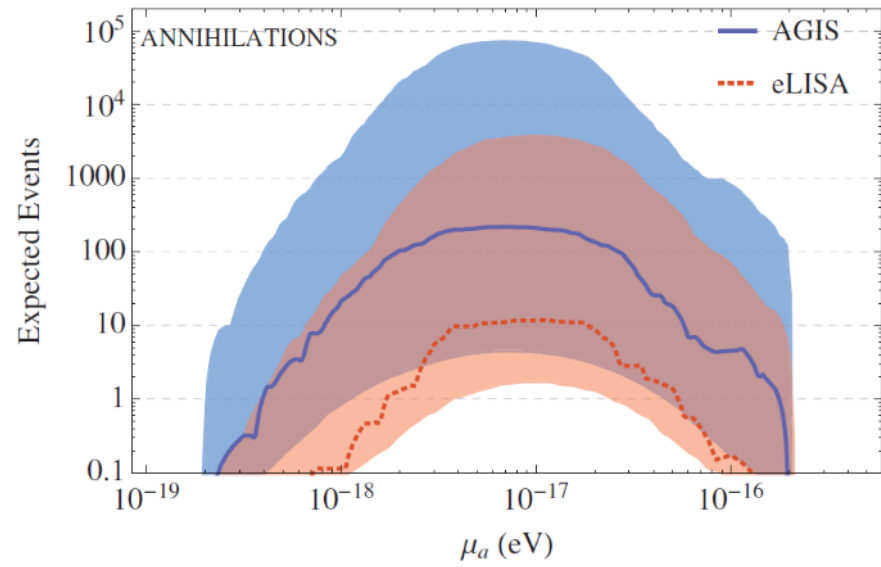
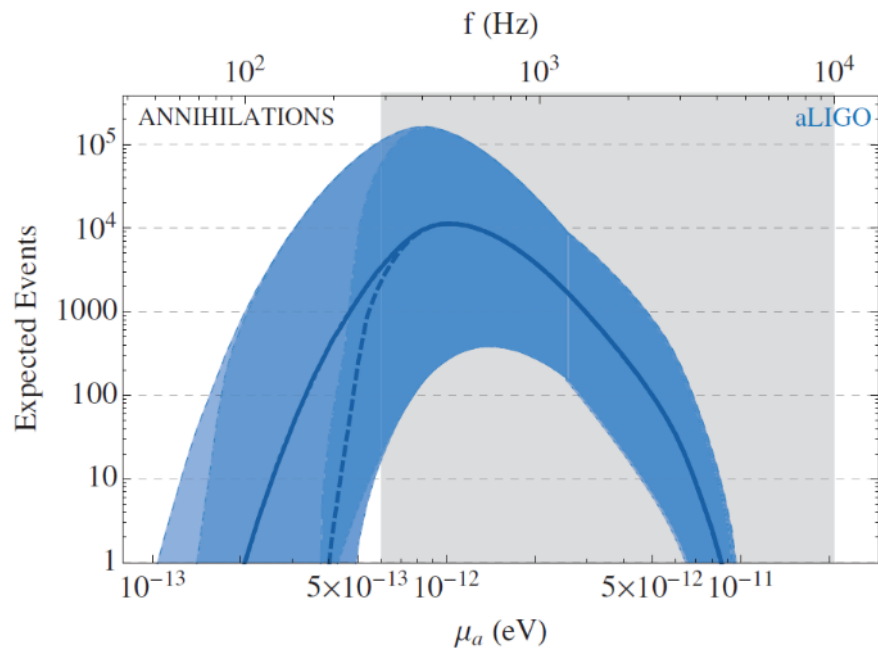


Bound on photon mass is model-dependent: details of accretion disks or intergalactic matter are important...but gravitons interact very weakly!

$$m_g < 5 \times 10^{-23} \text{ eV}$$

Brito et al PRD88:023514 (2013); Review of Particle Physics 2014





Arvanitaki, Baryakhtar, Huang arXiv:1411.2263

(rates may be overly optimistic)

Strong field gravity is a fascinating topic

Fundamental fields, either in form of minimally coupled fields or under curvature couplings have a very rich and unexplored phenomenology: condensates outside BHs and compact stars act as gravitational-wave lighthouses, but can also act as dark matter.

Superradiant instabilities can provide strong constraints on masses of ultra-light bosons, turning black holes into effective particle detectors.

Thank you

