

# Effect of many-body correlations on mesoscopic charge relaxation

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# The quantum RC circuit (1)

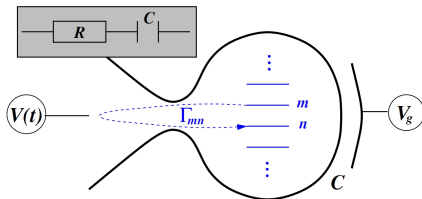
Low Frequency admittance of quantum RC circuit

$$g(\omega) = -i\omega C_\mu + \omega^2 C_\mu^2 R_q$$

Theoretical predictions

The relaxation resistance  $R_q$  is universal and quantized :

$$R_q = \frac{h}{2e^2} \quad (\text{for one channel})$$



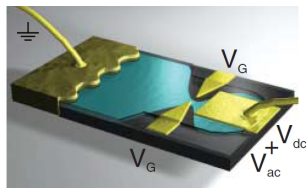
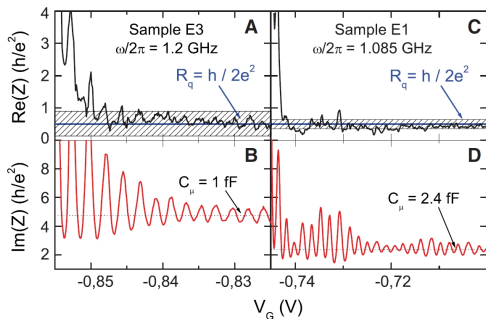
## References

- M. Büttiker, H. Thomas, and A. Prêtre, Phys. Lett. A **180**, 364 (1993). Original work
- S. E. Nigg, R. López, and M. Büttiker, Phys. Rev. Lett. **97**, 206804 (2006). Green function calculation - electronic interactions with "Hartree Fock"

# The quantum RC circuit (2)

## Experimental realization

Theoretical predictions confirmed experimentally in 2006.  
Observation of the quantized relaxation resistance !



## References

- J. Gabelli, G. Fève, J.-M. Berroir, B. Plaçais, A. Cavanna, B. Etienne, Y. Jin, and D. C. Glatli, *Science* **313**, 499 (2006)

# The quantum RC circuit (3)

## Further theoretical works

Recent works have studied in detail the role of electronic interactions and phase coherence

## Results

- Study of dephasing (needs several dephasing channels, and interchannel relaxation, to recover the classical result)
- Taking Coulomb interaction on the dot exactly :  $R_q$  not modified
- Strong interactions in the reservoir may lead to a phase transition to a incoherent regime
- For a large coherent dot ( $\Delta < \hbar\omega$ ), another universal value :  $R_q = \frac{h}{e^2}$

## References

- S.E. Nigg M. and Büttiker, Phys. Rev. B **77**, 085312 (2008)
- Y. Hamamoto, T. Jonckheere, T. Kato, and T. Martin, Phys. Rev. B **81**, 153305 (2010)
- C. Mora and K. Le Hur, Nature Physics **6**, 697 (2010)

# Open Questions

## Spin-polarized channel

Electronic interactions have been fully taken into account for a spin-polarized channel only. Experiment done in this regime so far (edge states of the Integer Quantum Hall effect), but could be done in a non-polarized regime.

What is the impact on the relaxation resistance of :

- the many-body correlations with spin and the Kondo effect
- the spin fluctuations
- a magnetic field modifying the spin up/down energies

# The model

## Hamiltonian

The system is described by the Anderson model, with the Hamiltonian :

$$\mathcal{H} = \mathcal{H}_L + \mathcal{H}_D + \mathcal{H}_T$$

## Details

$$\mathcal{H}_L = \sum_{\mathbf{k}\mu} \epsilon_{\mathbf{k}} c_{\mathbf{k}\mu}^\dagger c_{\mathbf{k}\mu}$$

$$\mathcal{H}_D = \sum_{\mu} \epsilon_{\mu} n_{\mu} + 2E_C n_{\uparrow} n_{\downarrow}$$

$$\mathcal{H}_T = \sum_{\mathbf{k}\mu} [t_{\mathbf{k}} d_{\mu}^\dagger c_{\mathbf{k}\mu} + (h.c.)]$$

## Flat band

Standard approximation :

$$t_{\mathbf{k}} = t, \quad \Gamma = \pi \rho_0 |t|^2$$

# Method

## Linear response Conductance

Applying a small time-dependent potential  $V(t)$  on the reservoir, and using linear response theory, the admittance  $g(t)$  can be expressed as :

$$g(t) = \frac{ie}{\hbar} \langle [\mathcal{I}(t), \mathcal{N}] \rangle \Theta(t)$$

$\mathcal{N} = \sum_{\mu} d_{\mu}^{\dagger} d_{\mu}$  is the occupation operator,  $\mathcal{I}(t) = e d\mathcal{N}/dt$  is the current operator.

## Charge susceptibility

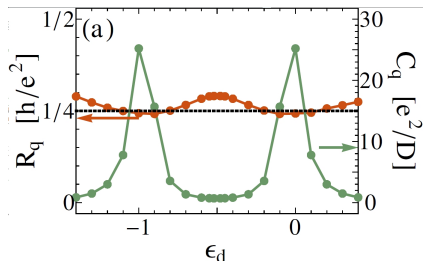
In practice, the Numerical Renormalization Group is used to compute the charge susceptibility  $\chi_c(t) = -i \langle [\mathcal{N}(t), \mathcal{N}] \rangle \Theta(t)$ , from which we can compute the quantum capacitance and the relaxation resistance :

$$\frac{R_q(\omega)}{h/e^2} = \text{Re} \left[ \frac{1}{2\pi i \omega \chi_c(\omega)} \right] \quad \frac{e^2/h}{C_q(\omega)} = \text{Im} \left[ \frac{1}{2\pi i \chi_c(\omega)} \right]$$

# Results for the quantum capacitance

## Quantum capacitance (green curve)

- The capacitance shows two peaks, for  $\epsilon_d \sim \epsilon_F$  and  $\epsilon_d + 2E_C \sim \epsilon_F$ , which correspond to peaks in the density of states of the dot.
- But is small in the Kondo regime ( $\epsilon_d \sim -0.5$ ), although Kondo creates a huge density of states. Charge is “frozen” in the Kondo regime.

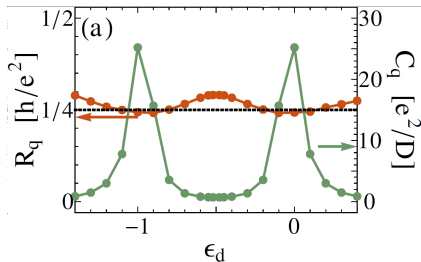


# Results for the relaxation resistance

Relaxation resistance (red curve)

$$R_q = \frac{h}{4e^2}$$

independently of  $U$  and  $\epsilon_d$  ( $1/4$  because of the two spin channels). The small deviations are caused by the finite bandwidth used in the calculations.



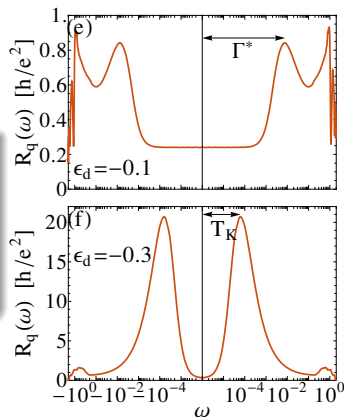
Does this mean that many-body effects have no impact on  $R_q$ ?

# Results for the relaxation resistance

## Frequency dependence of $R_q$

Looking at the  $\omega$  dependence of  $R_q(\omega)$

- in the fluctuating valence regime ( $\epsilon_d = -0.1$ ), large peak at  $\omega \sim \Gamma^*$
- in the Kondo regime, huge peak at  $\omega \sim T_K$

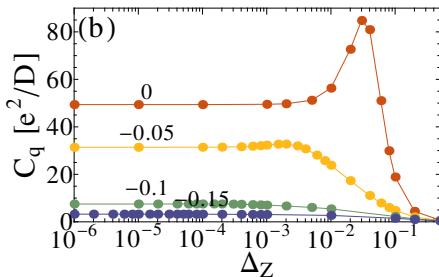
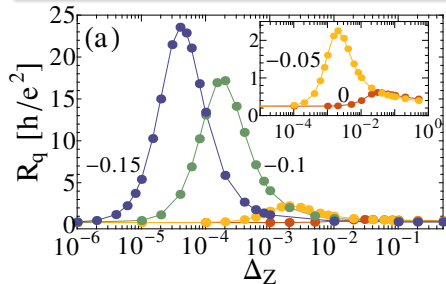


These peaks are absent in the non-interacting case : true many-body effect !

# Results in the presence of a magnetic field

## Effect of a magnetic field on $R_q(0)$ and $C_q$

A magnetic field will procure a Zeeman splitting  $\Delta_Z$  of the dot levels, and will allow us to probe the peak structure present in  $R_q(\omega)$ .



$R_q(0)$  shows huge peaks as a function of magnetic field (largest in the Kondo regime,  $\epsilon_d = -0.15$ ). The peak maximum is for  $\Delta_Z = T_K$

$C_q$  stays rather constant, except for a small peak at resonance ( $\epsilon_d = 0$ )

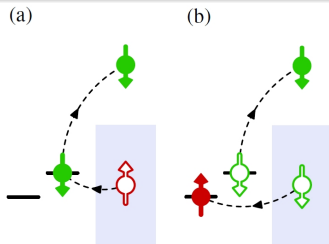
# Interpretation

## Relaxation mechanism

The relaxation resistance is attributed to electron-hole pair creation in the conduction band.

## e-h pair creation

The Zeeman splitting lowers the energy cost of an e-h pair creation. When  $\Delta_Z \sim \Gamma^*$ , the energy cost is close to zero.



The large increase of the relaxation resistance is due to spin-flip induced e-h pair creation, favored by the magnetic field.

Theoretical calculations with Bethe-Ansatz : M. Filippone, K. Le Hur, C. Mora, cond-mat/1105.6353

# Conclusion

## Conclusions

- Numerical Renormalization Group study of the relaxation resistance of the quantum RC circuit, with full many-body correlations
- In the absence of magnetic field,  $R_q$  has a universal value  $R_q = h/(4e^2)$
- The density of states coming from the Kondo peak does not contribute to the quantum capacitance
- When a magnetic field is applied,  $R_q$  is not quantized, and has a huge peak for  $\Delta_Z \simeq T_K$ .
- The large increase of  $R_q$  is due to the enhancement of electron-hole pair creation by spin-flip processes, because of the magnetic field
- Experimental observation is in reach with current techniques

## Reference

M. Lee, R. Lòpez, M.-S. Choi, T. Jonckheere, and T. Martin  
Phys. Rev. B **83**, 201304(R) (2011)