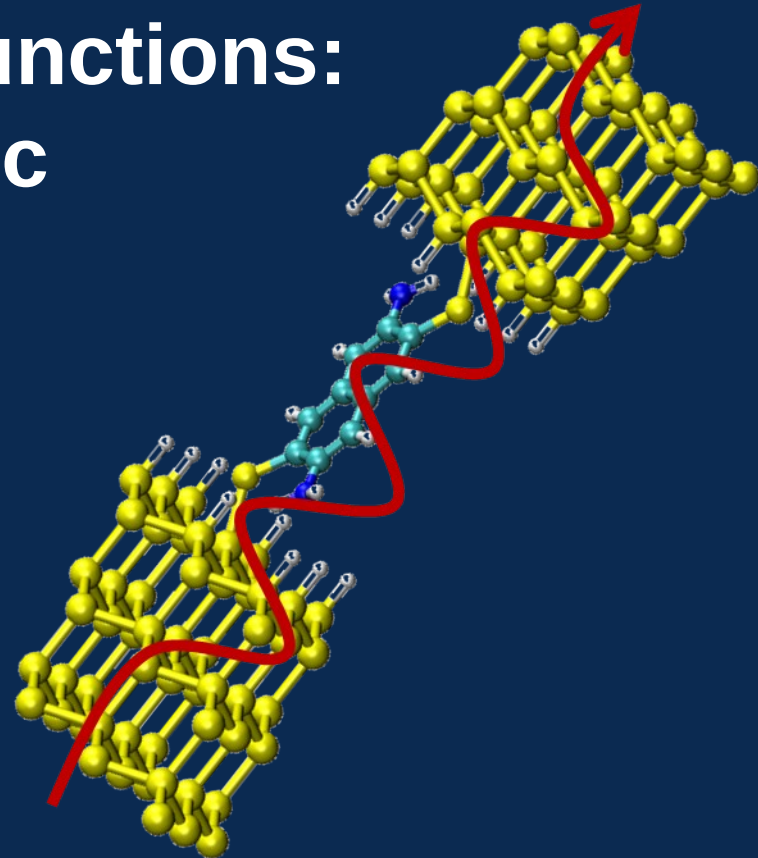


# Engineering the thermopower in semiconductor-molecule junctions: towards high thermoelectric efficiency at the nanoscale

D. Nozaki, H. Sevinçli,  
W. Li, R. Gutierrez, and G. Cuniberti

**Phys. Rev. B 81, 235406 (2010)**



# Dresden



# Research centers in Dresden

**IFW Dresden (Leibniz Institute)**



**FZD (Helmholtz center) Namlab**



**Max-Planck Institute (MPI-PKS)**



**Max-Planck Institute  
(MPI-CPFS)**



**Max-Bergmann Center**

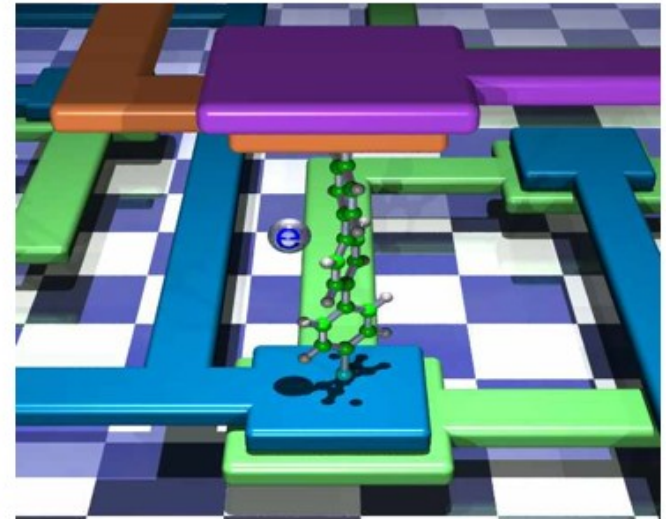
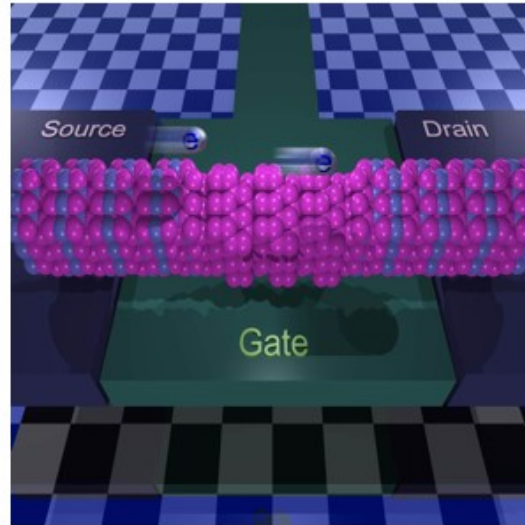
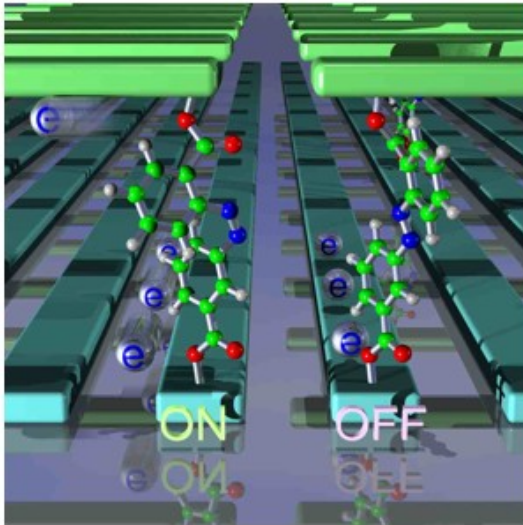


**Fraunhofer Institute**

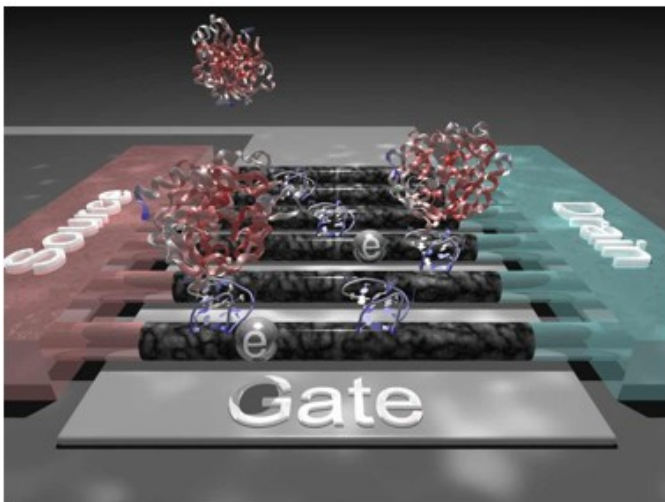




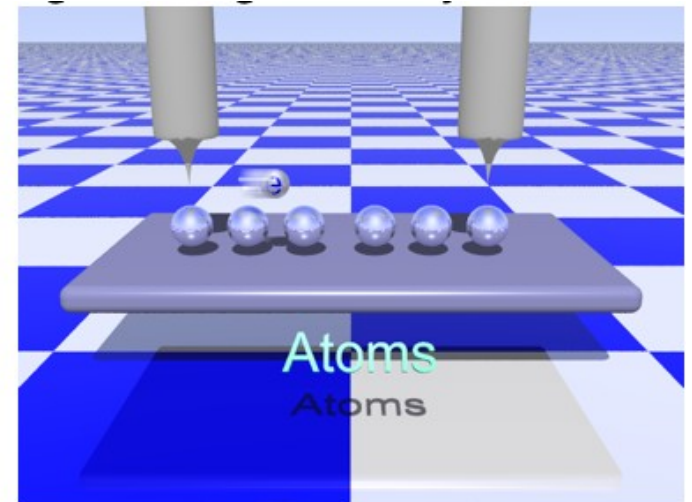
Nozaki *et al.* Nano Res. (2009) Nozaki *et al.* Nanotech. (2011) Dulic *et al.* Angew. Chem. Int.. (2010)



SiNW biosensors (ongoing)



Nozaki *et al.* New J. Phys. (2010)



All images  
by D. Nozaki



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(TU Dresden & POSTECH)

**Mr. Wu Li**

**Dr. Haldun Sevincli**

**Dr. Rafael Gutierrez**  
(TU Dresden)



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- **Sächsische AufbauBank (SAB)**
- **Namlab (Dr. Weber *et al.*)**

- 1. Introduction - thermoelectric effects, history, applications**
- 2. Motivation – recent experiments**
- 3. Toy model and application to molecular systems**
- 4. Results**
- 5. Summery**

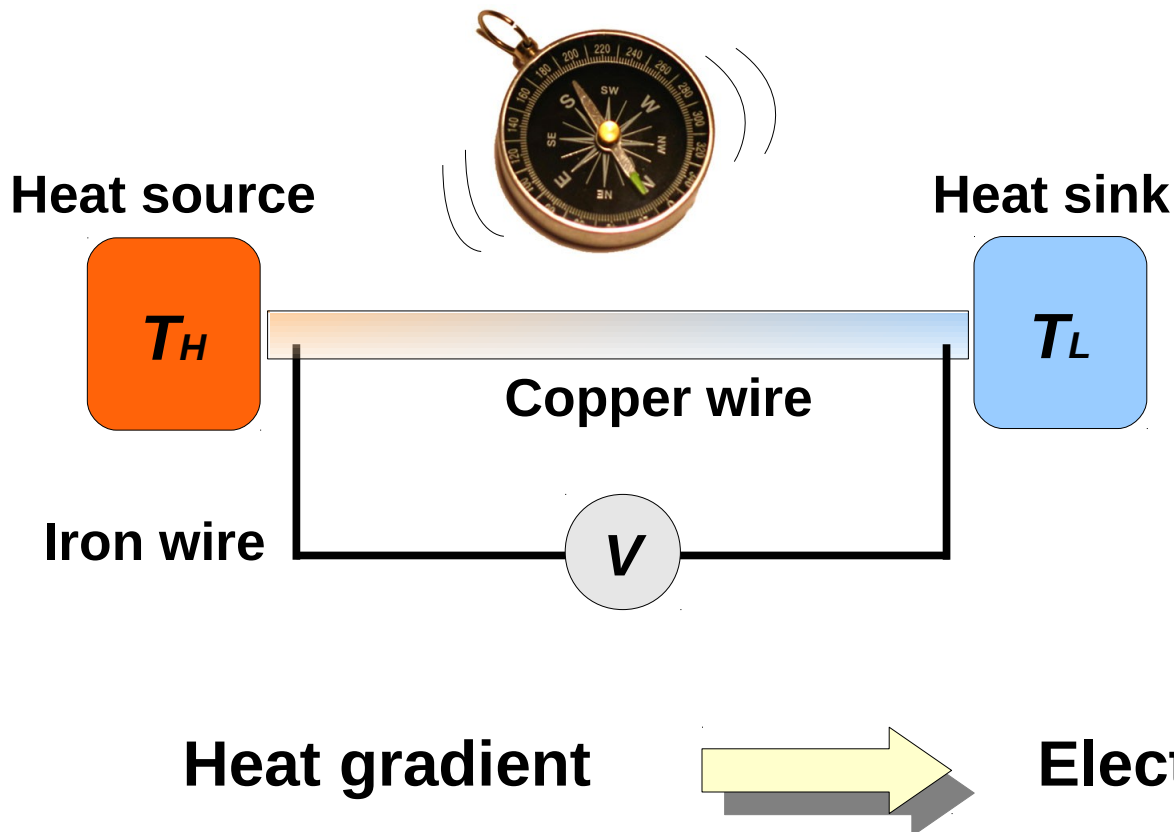
**Heat is wasted as byproducts in many situations.  
(ex. CPUs, industries, combustion etc.)**

**Thermoelectric devices**

**Merit: static, no motion, thin,  
shape can be changed**

**Demerit: low efficiency, low voltage**

1821 – He found deflection of compass when circuit made by two different metals was placed in a heat gradient.



Thomas Jhon Seebeck  
(1770-1831)

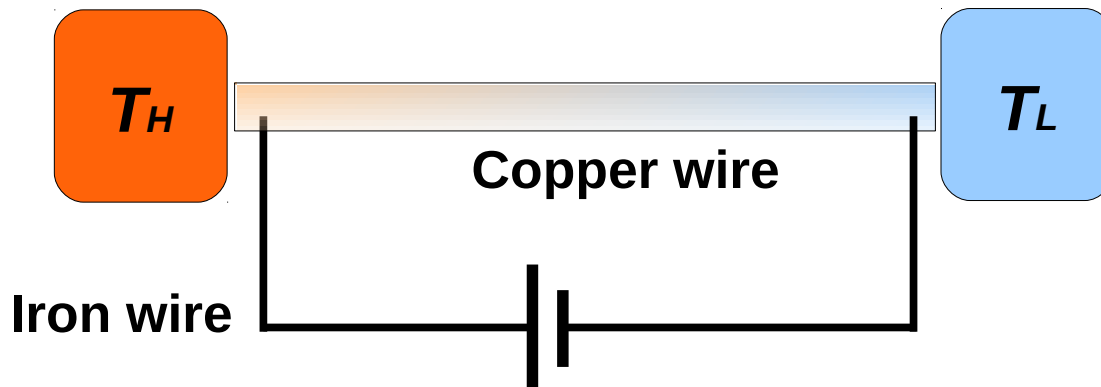
Thermopower

$$S = V / T \ (\mu\text{V}/\text{K})$$

1834 – He found temperature gradient was created when current was driven through circuit made by two different metals.



Jean Charles Athanase Peltier  
(1785-1845)

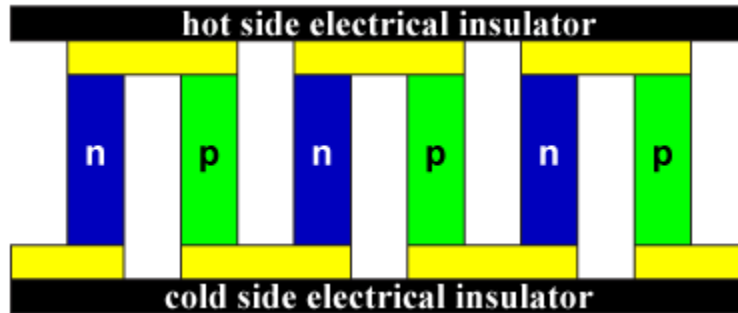


Heat gradient

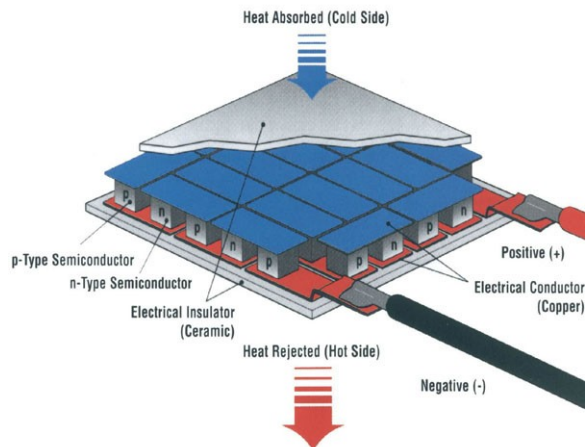


Electric current

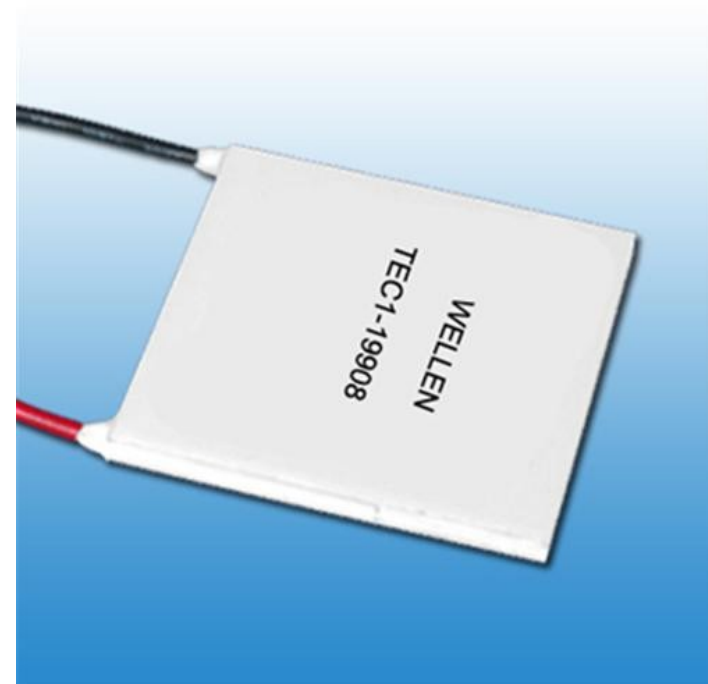
## Side view



*D. J. Paul, Univ. Glasgow*



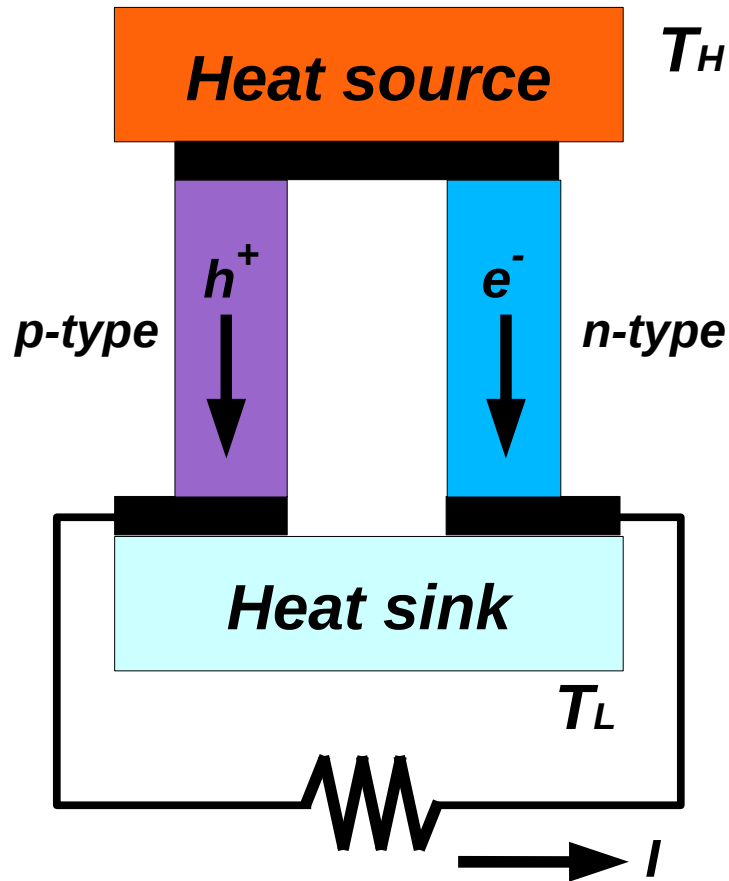
## Thermoelectric module



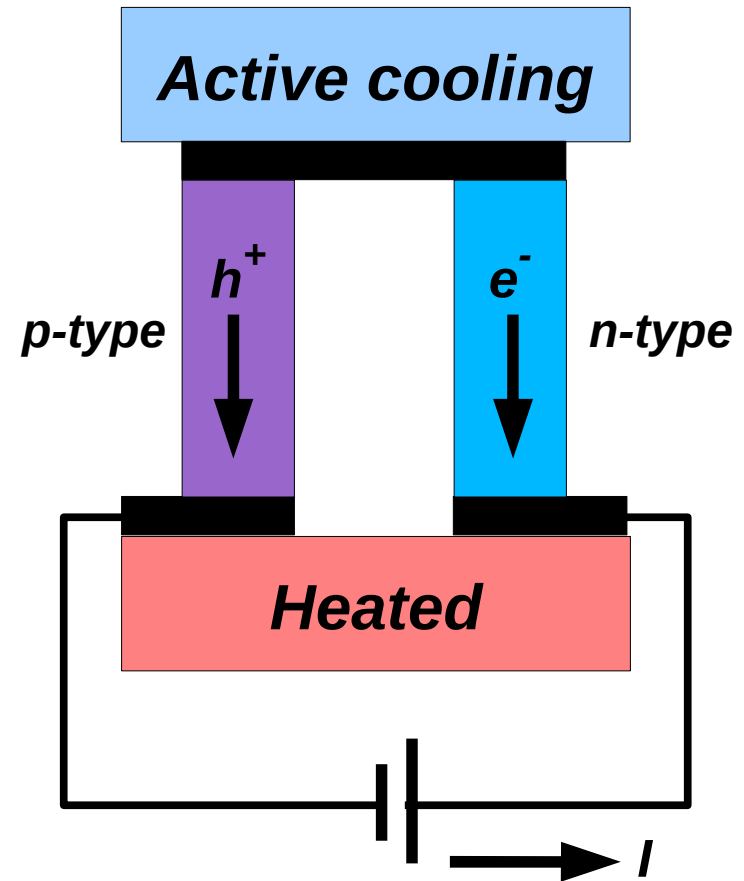
**Thermoelectric Modules Tec1-19908**  
**Wellen Technology Co. Ltd**

# How to understand Seebeck/Pelitier effect

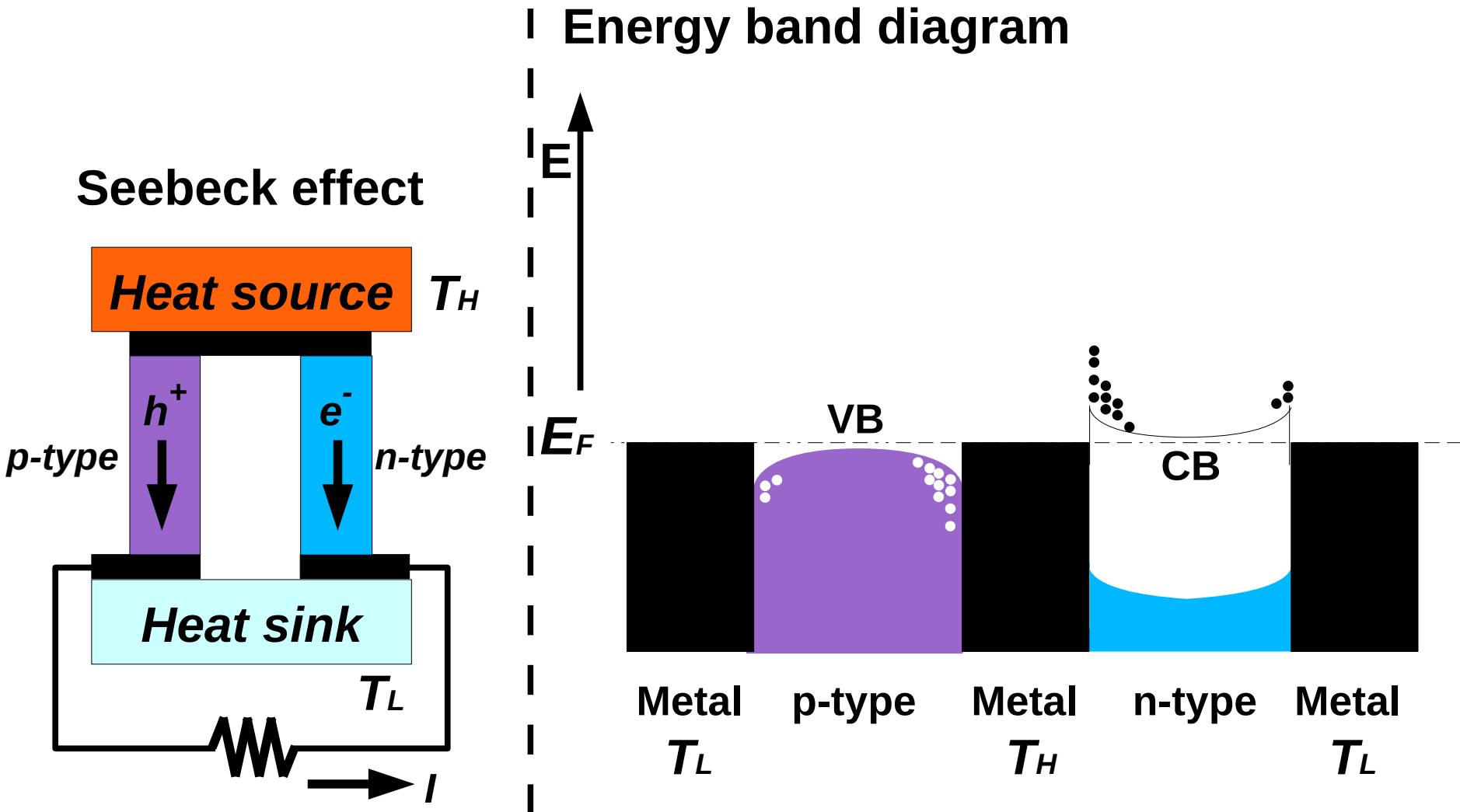
## Seebeck effect



## Pelitier effect

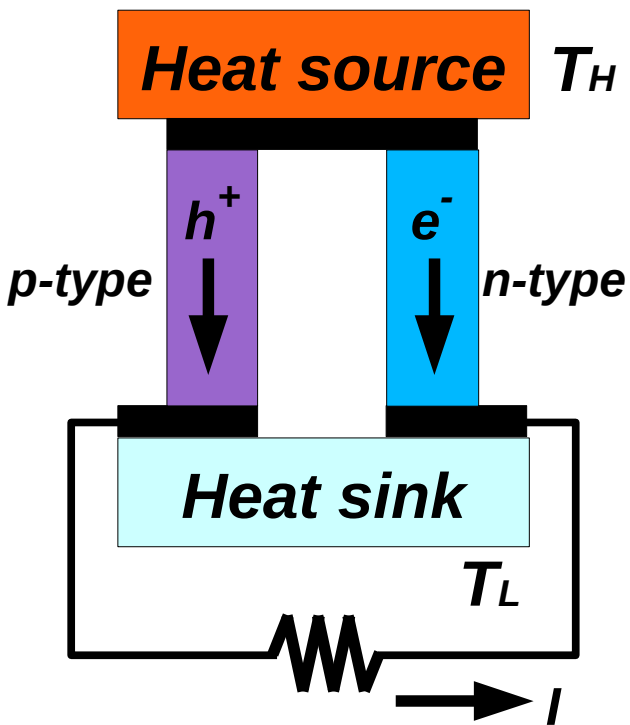


# How to understand Seebeck effect?

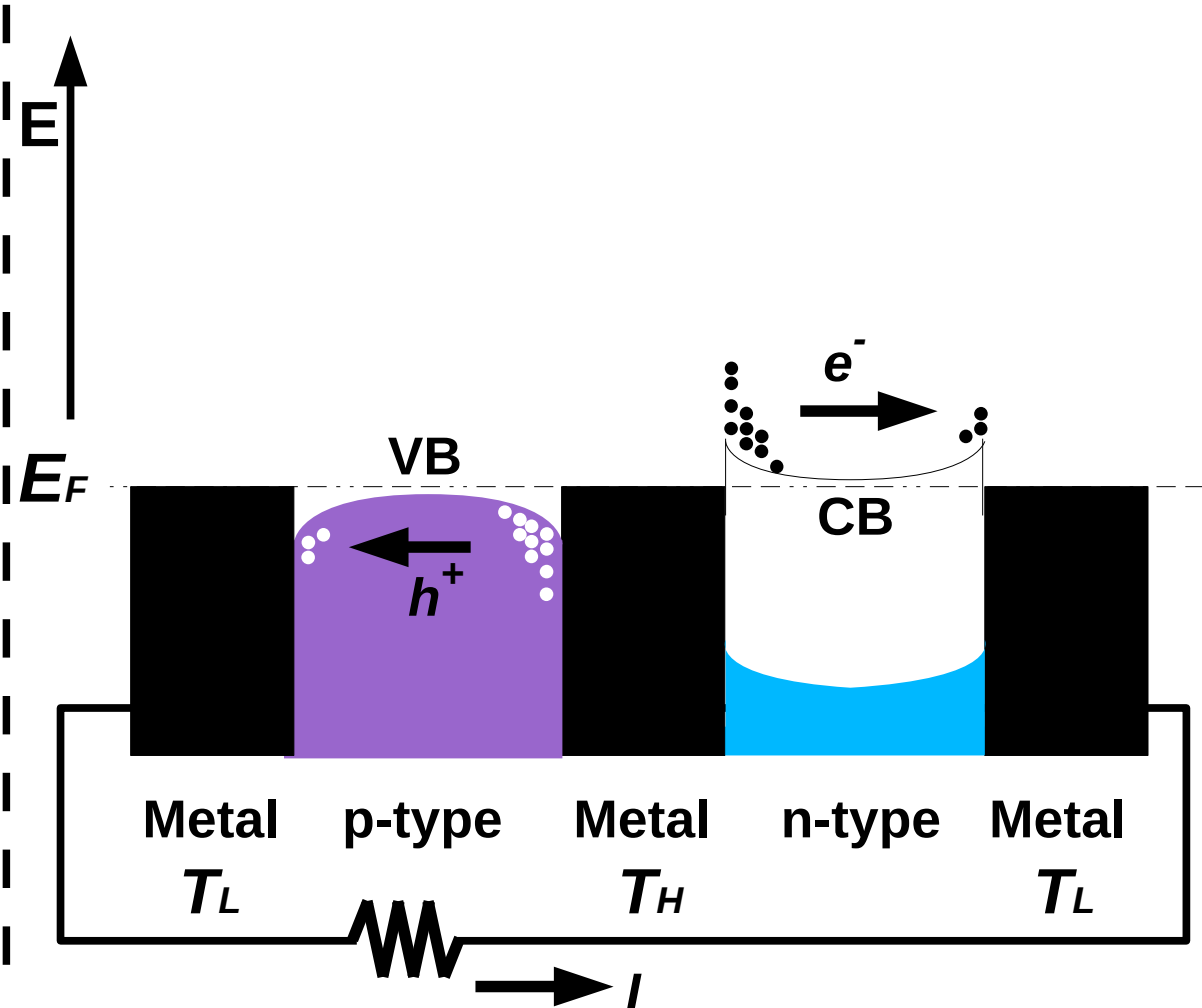


# How to understand Seebeck effect?

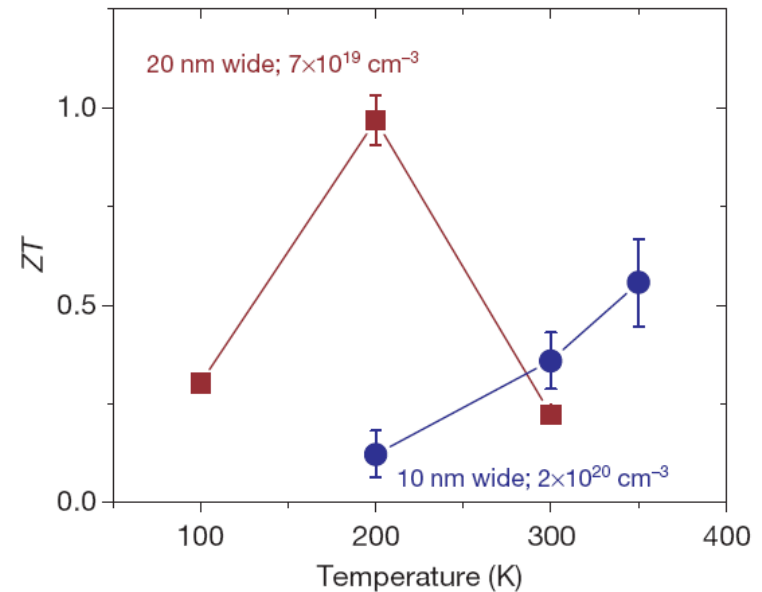
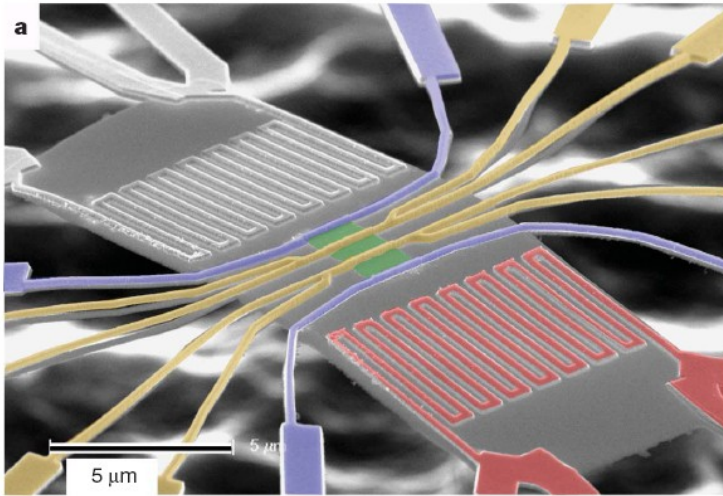
## Seebeck effect



## Energy band diagram



# Thermoelectricity at the nanoscale



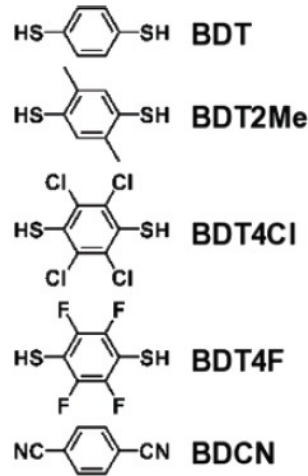
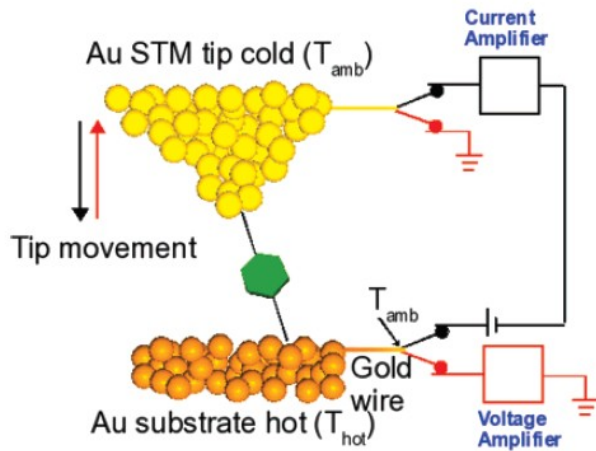
*“Silicon nanowires as efficient thermoelectric materials”*

A.I. Boukai *et al.*, Nature **451**, 168 (2008)

*“Enhanced thermoelectric performance of rough silicon nanowires”*

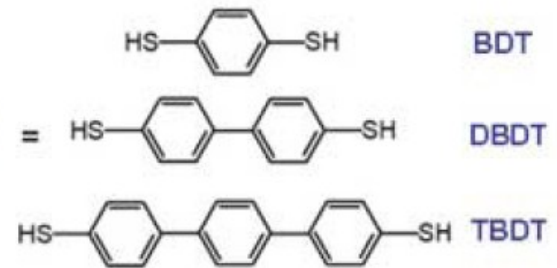
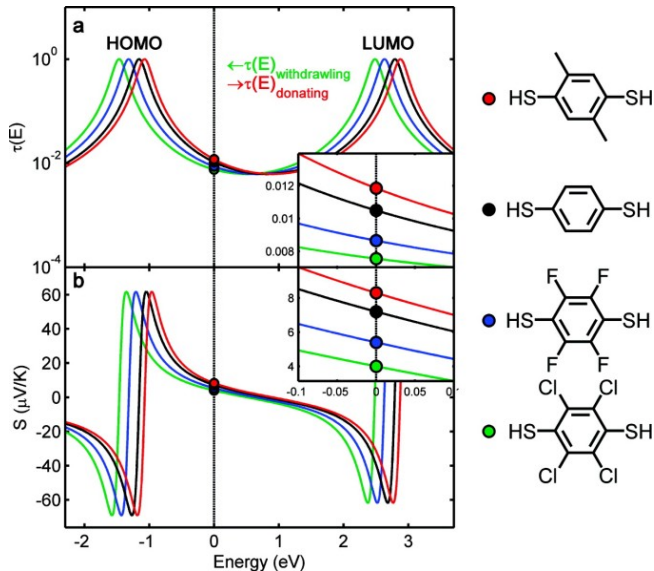
A. I. Hochbaum *et al.*, Nature **451**, 163 (2008)

# Thermoelectricity in molecular junctions



*“Probing the chemistry of molecular heterojunctions using thermoelectricity”*  
 K. Baheti et al.,  
 Nano Letters **8**, 715 (2008)

*“Thermoelectricity in molecular junctions”*  
 P. Reddy, et al.  
 Science **315**, 1568 (2007)



*Seebeck coeff. sensitive to position of the Fermi level*

# How to calculate figure of merit ?

**Thermoelectric  
figure of merit**

Seebeck coeff. ( $\mu\text{V}/\text{K}$ )

Electrical  
conductivity

$$ZT = S^2 T \frac{\sigma}{\underbrace{\kappa_{\text{el}} + \kappa_{\text{ph}}}_{\text{Thermal conductivity}}}$$

Thermal  
conductivity

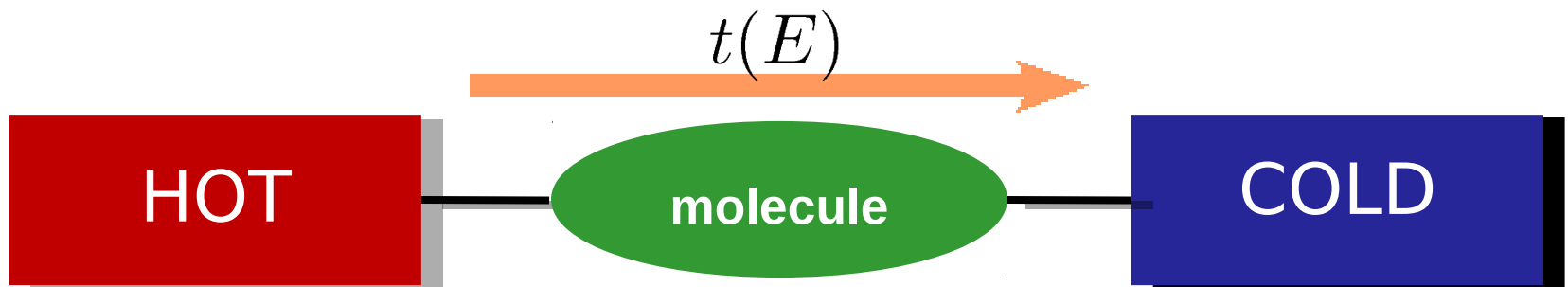
## **Breakthrough: Nanostructuring**

Hicks & Dresselhaus

*Thermoelectric figure of merit of a 1D conductor*

Phys. Rev. B **47**, 16631 (1993)

Electronic part of the thermoelectric transport coefficients:  
if no inelastic effects → Landauer approach



$$ZT = \frac{S^2 \sigma T}{\kappa_{el} + \kappa_{ph}}$$

$$\sigma = \frac{e^2}{h} L_0(\mu)$$

$$S = \frac{1}{eT} \frac{L_1(\mu)}{L_0(\mu)}$$

$$\kappa_{el} = \frac{1}{hT} \left( L_2(\mu) - \frac{L_1^2(\mu)}{L_0(\mu)} \right)$$

$$L_n(\mu) = \int dE t(E) (E - \mu)^n \frac{\partial f}{\partial E}$$

Transmission function (Fisher-Lee relation)

$$t(E) = T_{el}(E) = \text{Tr} \left[ G^R(E) \Gamma_L(E) G^A(E) \Gamma_R(E) \right]$$

Retarded Green's function

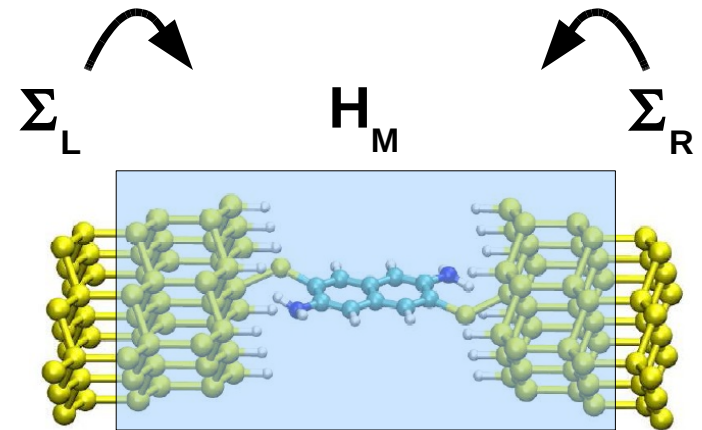
$$G^R(E) = \left[ (E + \delta i) S_M - H_M(E) - \Sigma_L(E) - \Sigma_R(E) \right]^{-1}$$

Broadening function

$$\Gamma_{L/R}(E) = i \left[ \Sigma_{L/R}(E) - \Sigma_{L/R}(E)^\dagger \right]$$

Self-energy

$$\Sigma_{L/R}(E) = (E S_{L/R} - V_{L/R}) g_{L/R}(E) (E S_{L/R} - V_{L/R})^\dagger$$



- Surface Green function: algorithm by Lopez-Sancho
- Self-consistent NEGF: gDFTB by Alesandro Pecchia

Transmission function for phonon transport

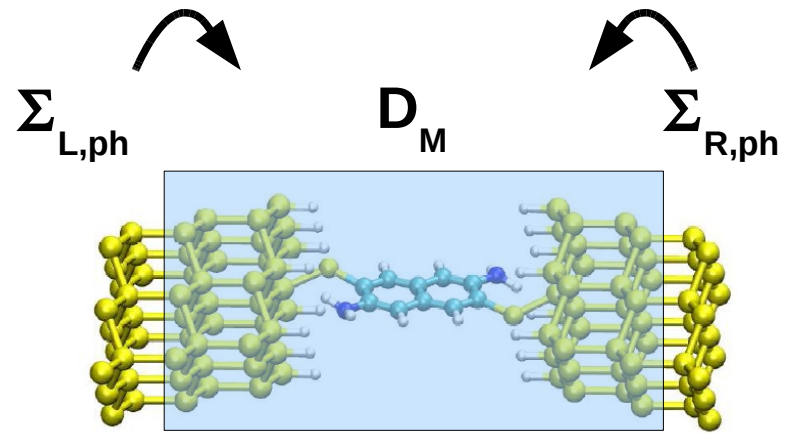
$$T_{ph}(\omega) = Tr[G_{ph}^R(\omega)\Gamma_{L,ph}(\omega)G_{ph}^A(\omega)\Gamma_{R,ph}(\omega)]$$

Retarded Green's function

$$G_{ph}^R(\omega) = [(\omega + \delta i)^2 - D_M(E) - \Sigma_{L,ph}(E) - \Sigma_{R,ph}(E)]^{-1}$$

Phonon contribution to the thermal conductance

$$\kappa_{ph}(T) = \int_0^\infty \frac{d\omega}{2\pi} \hbar\omega \frac{\partial f_B(\omega, T)}{\partial T} T_{ph}(\omega)$$



**Main goal:**

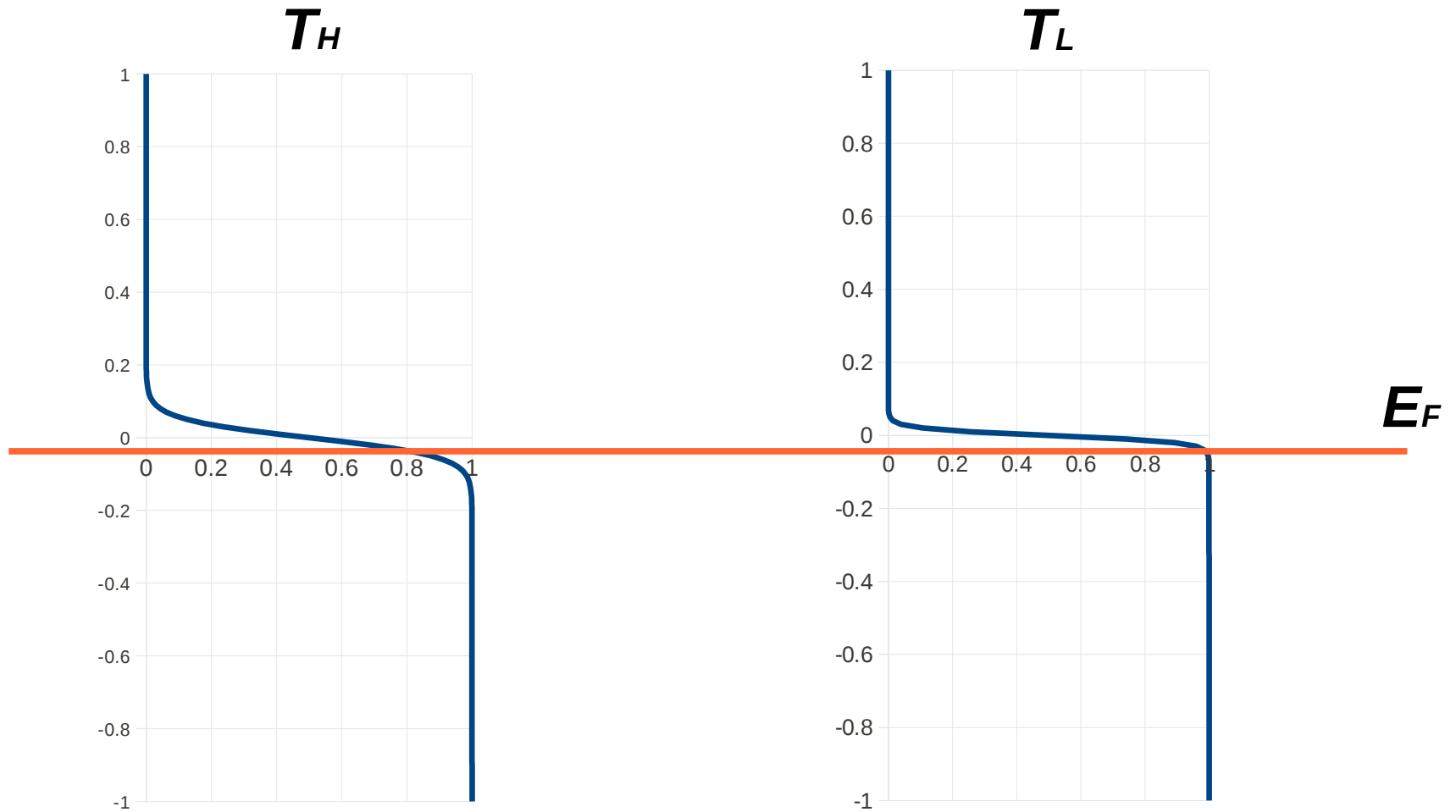
**increase** thermopower  $S$  and figure of merit  $ZT$

**Possible road:**

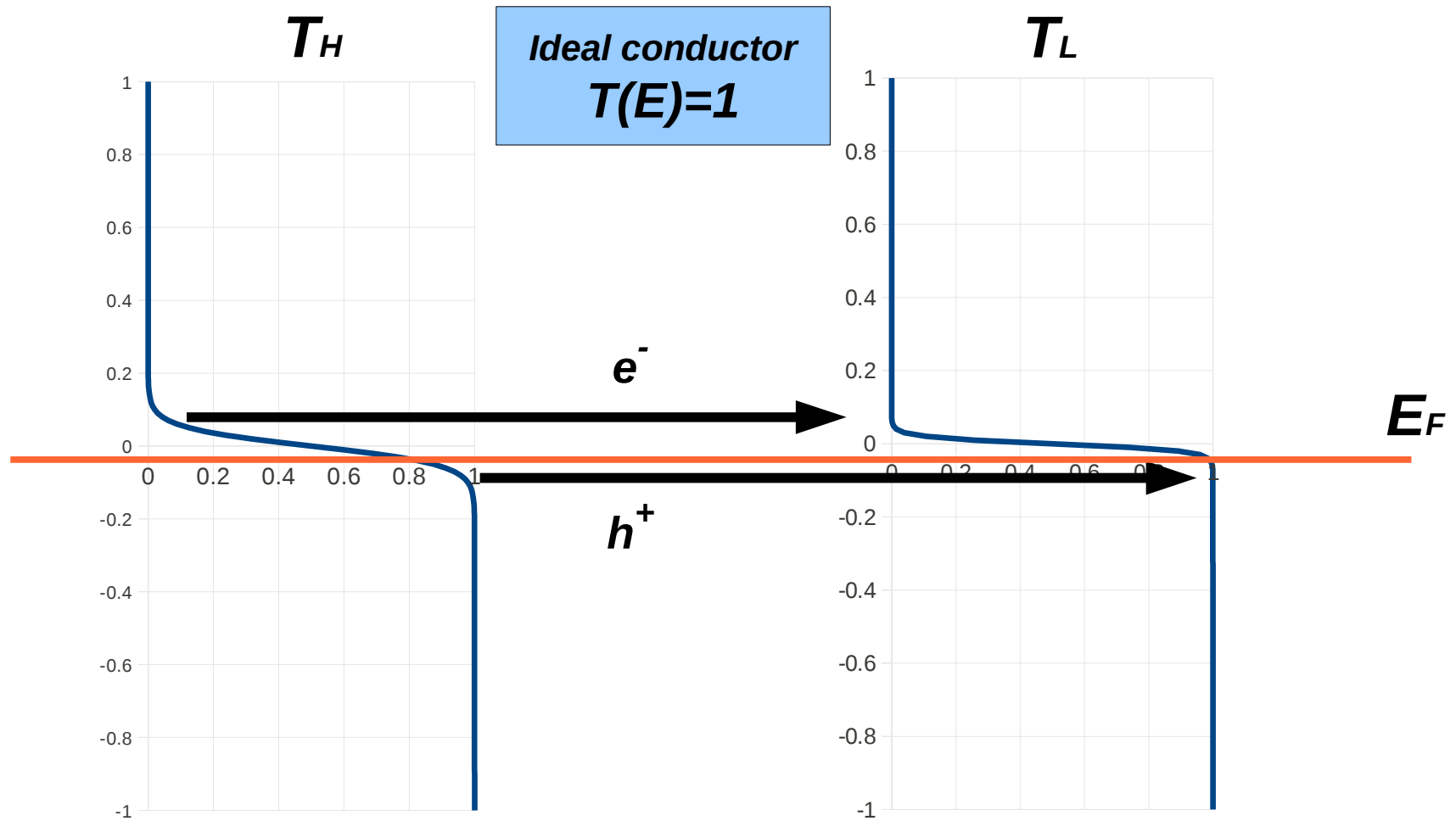
- **decouple** electronic and vibronic thermal conductance channels
- **suppress** (ideally) vibronic thermal conductance  
T. Markussen, A.-P. Jauho, and M. Brandbyge, PRL **103**, 055502 (2009)
- **filter** electron (hole) contribution to  $S$   
$$S = S_{\text{elec}} - S_{\text{hole}}$$
- **resonance** near Fermi level (log-derivative!)  
G. D. Mahan, J.O. Sofo, Proc. Natl. Acad. Sci. **93**, 7436 (1996)

**Chemical tuning of thermoelectricity in molecular junctions!?**

# How to optimize electronic $ZT$ ?



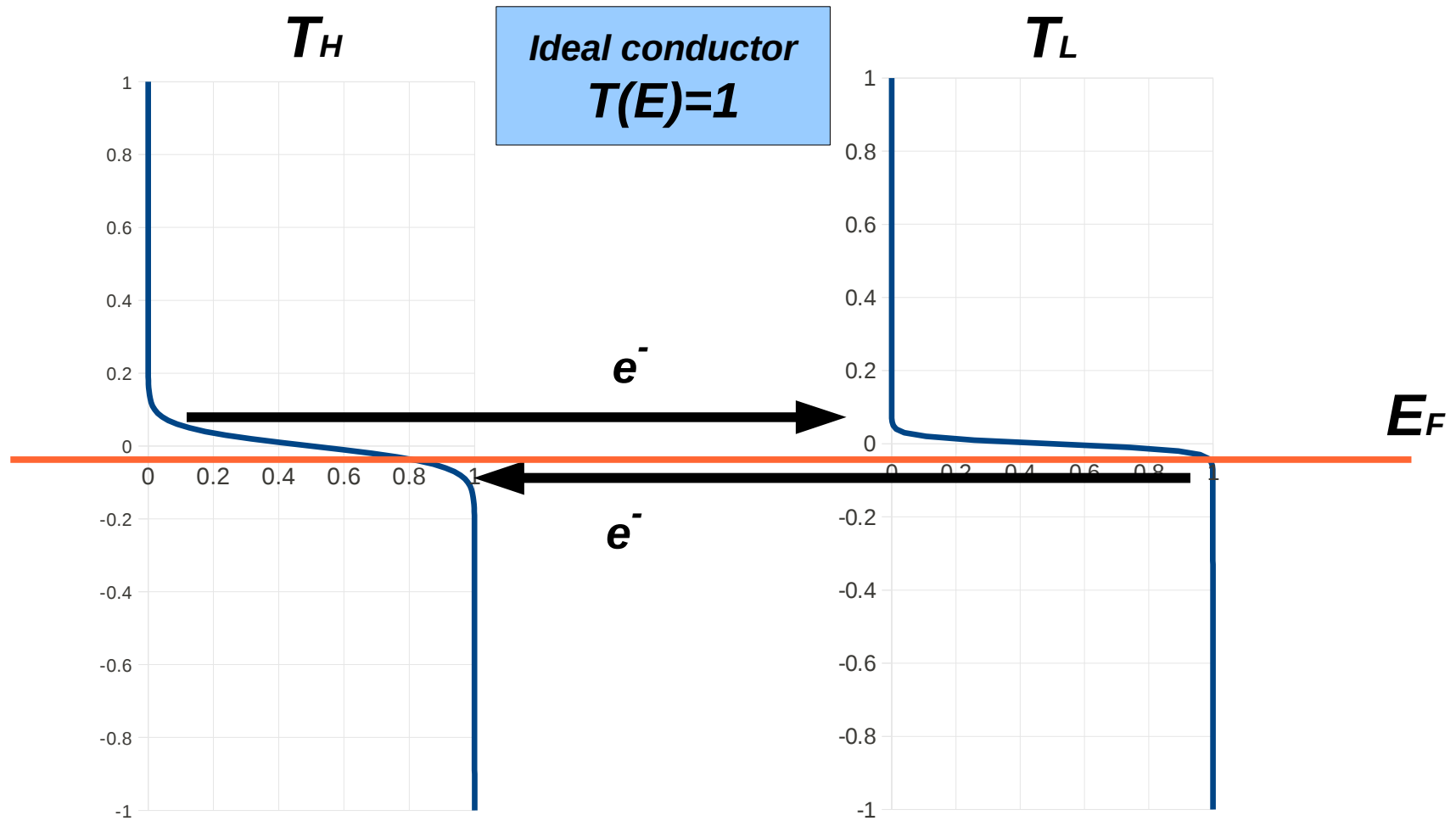
# How to optimize electronic $ZT$ ?



$$N_L(E) = DOS_L(E) * F_L(E)$$

$$N_R(E) = DOS_R(E) * F_R(E)$$

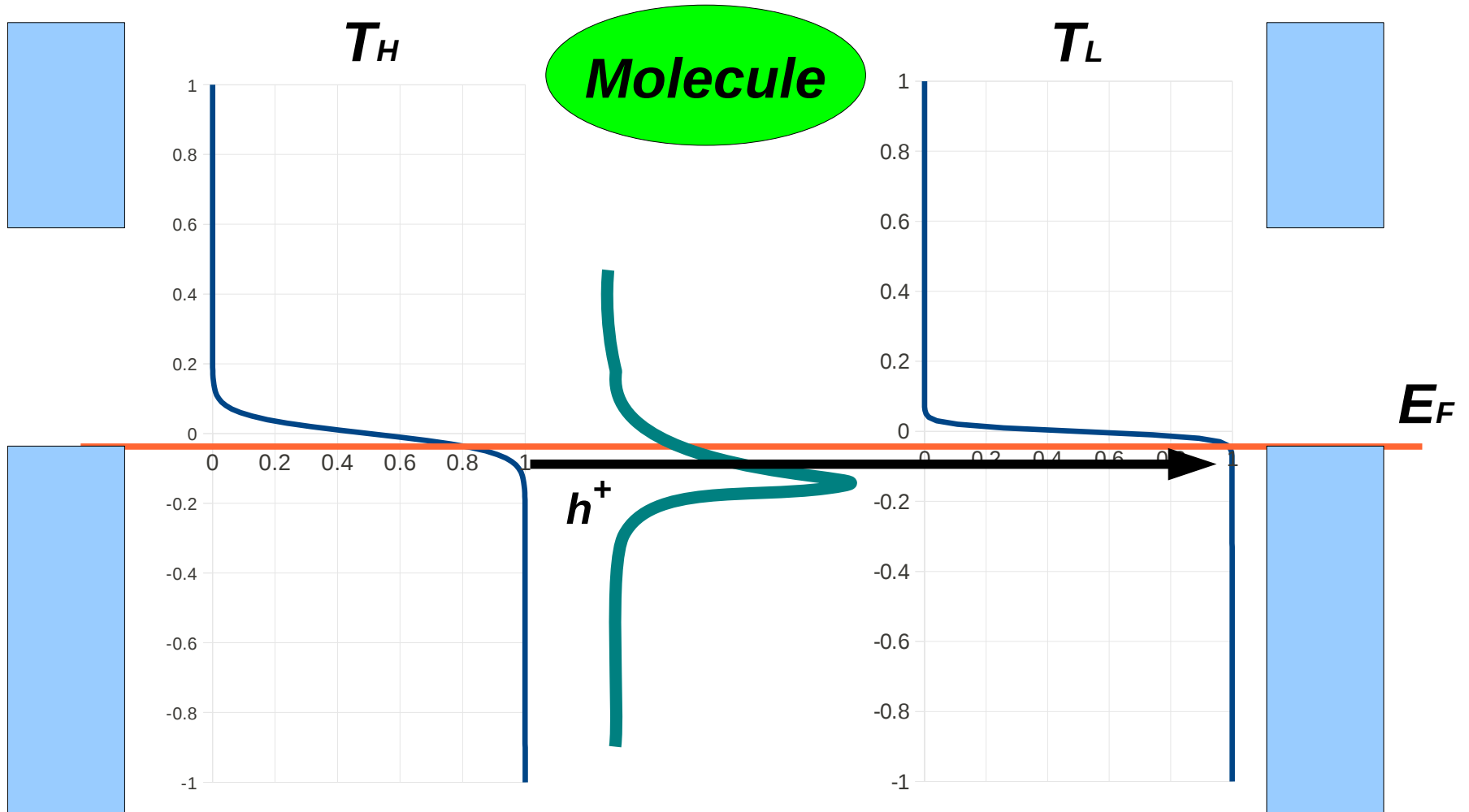
# How to optimize electronic $ZT$ ?



$$N_L(E) = DOS_L(E) * F_L(E)$$

$$N_R(E) = DOS_R(E) * F_R(E)$$

# How to optimize electronic $ZT$ ?

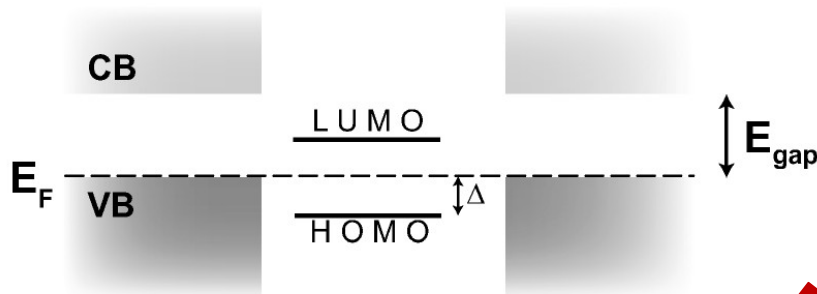


$$N_L(E) = DOS_L(E) * F_L(E)$$

$$N_R(E) = DOS_R(E) * F_R(E)$$

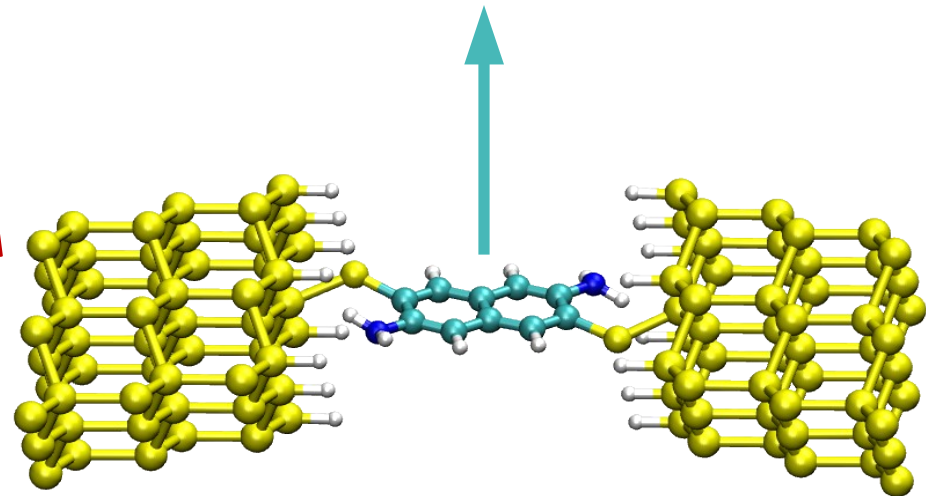
# Si electrodes+polyacene molecules

Si(111) electrodes are used in order to increase the thermopower to **filter out the negative contribution of electrons**.



*Toy model*

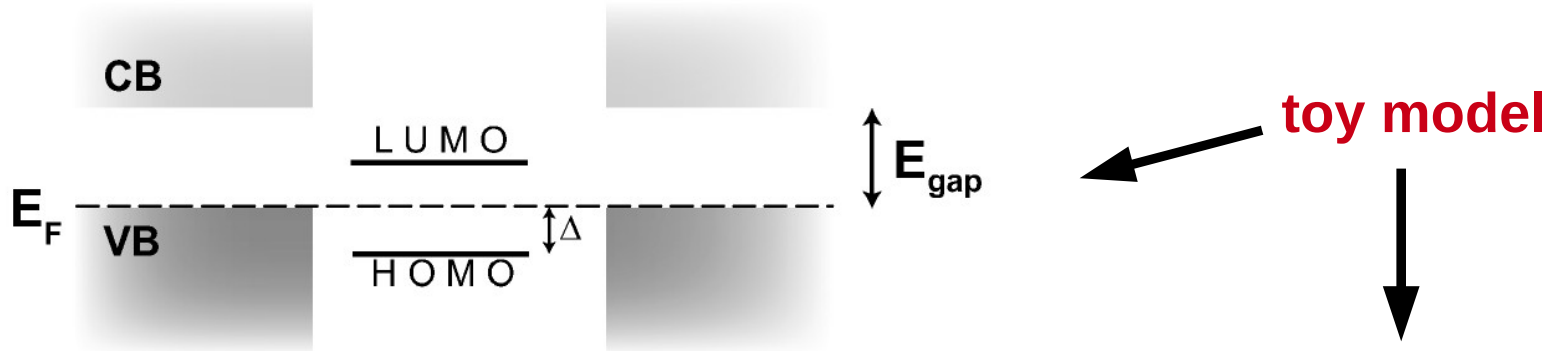
benzene, naphthalene, and anthracene with  $NH_2$  side groups



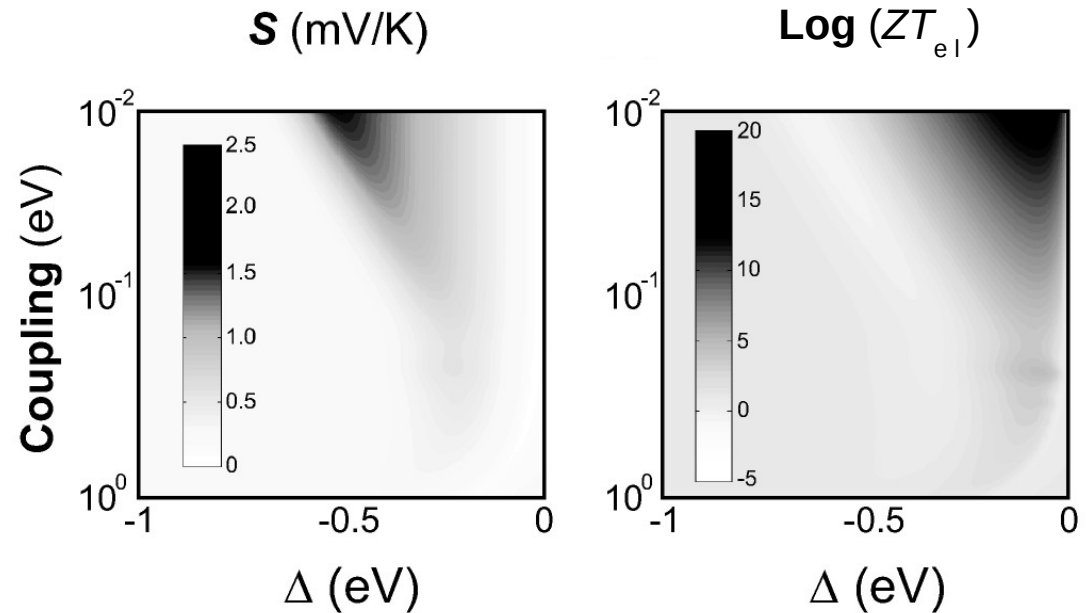
*Atomistic model*

**Methodology:** DFT-based approach (DFTB) + Green's function approach

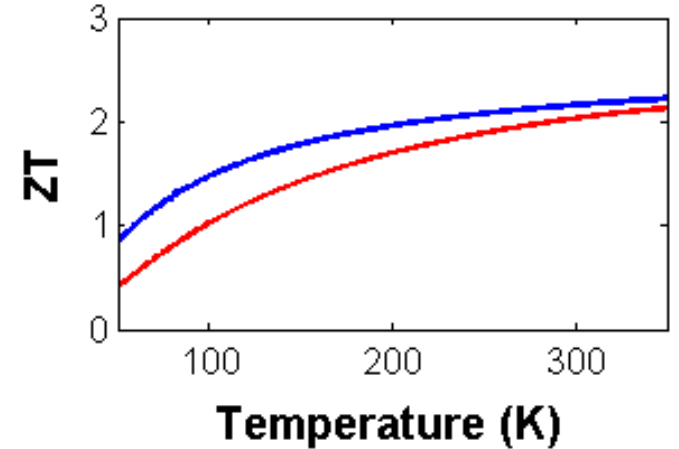
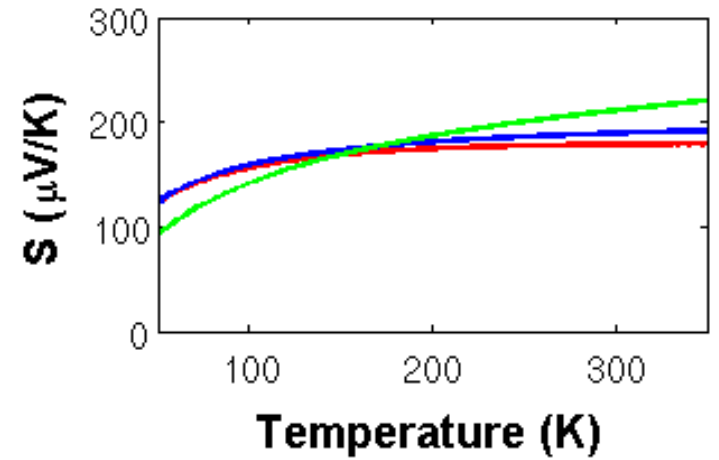
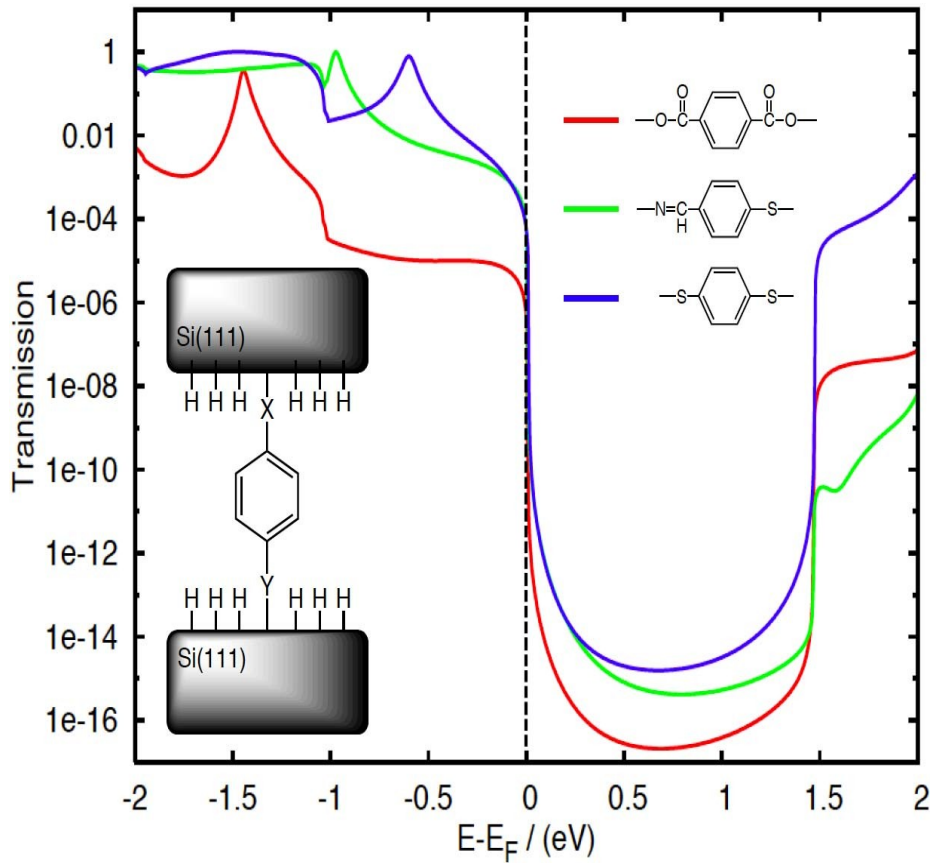
# strategy: semiconducting electrodes



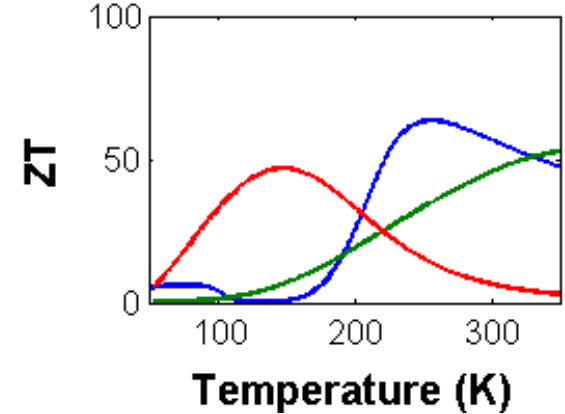
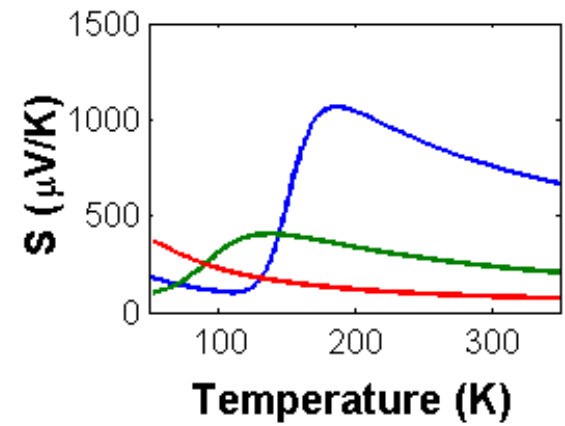
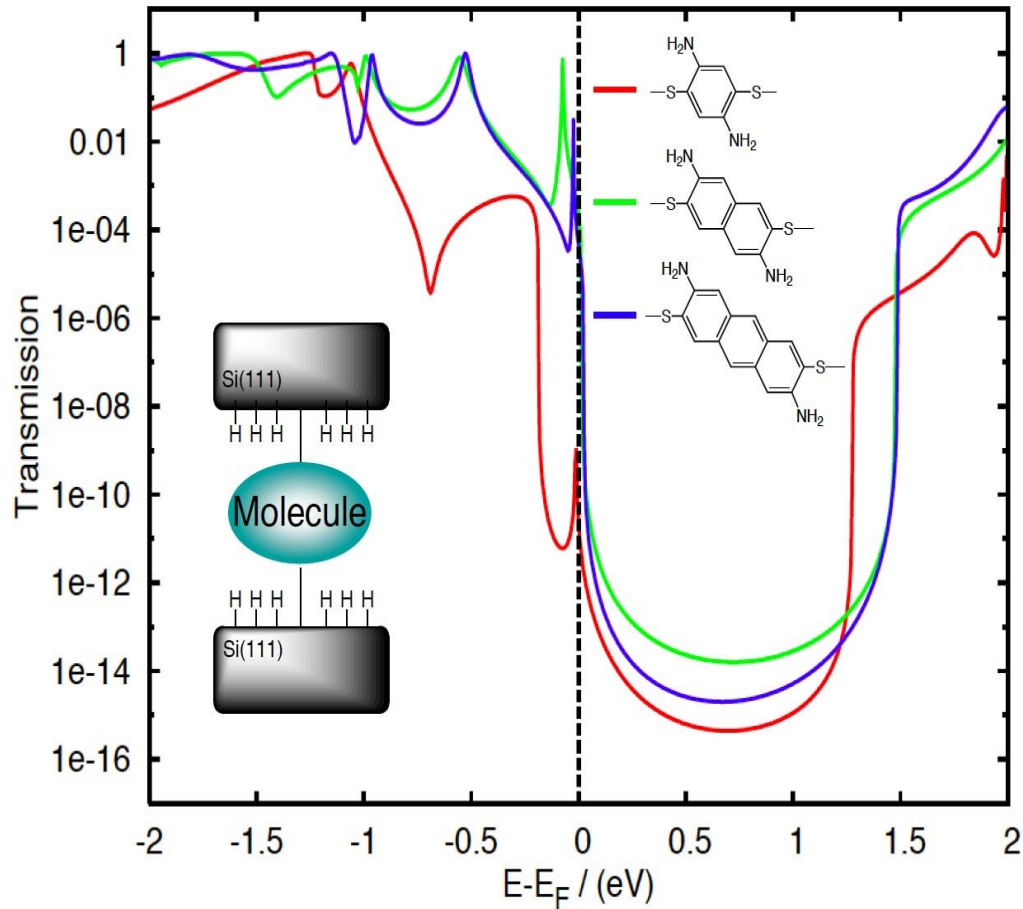
$S$  and  $ZT$  are maximized for ***weak coupling*** and when the ***HOMO*** level is close to the ***Fermi level***

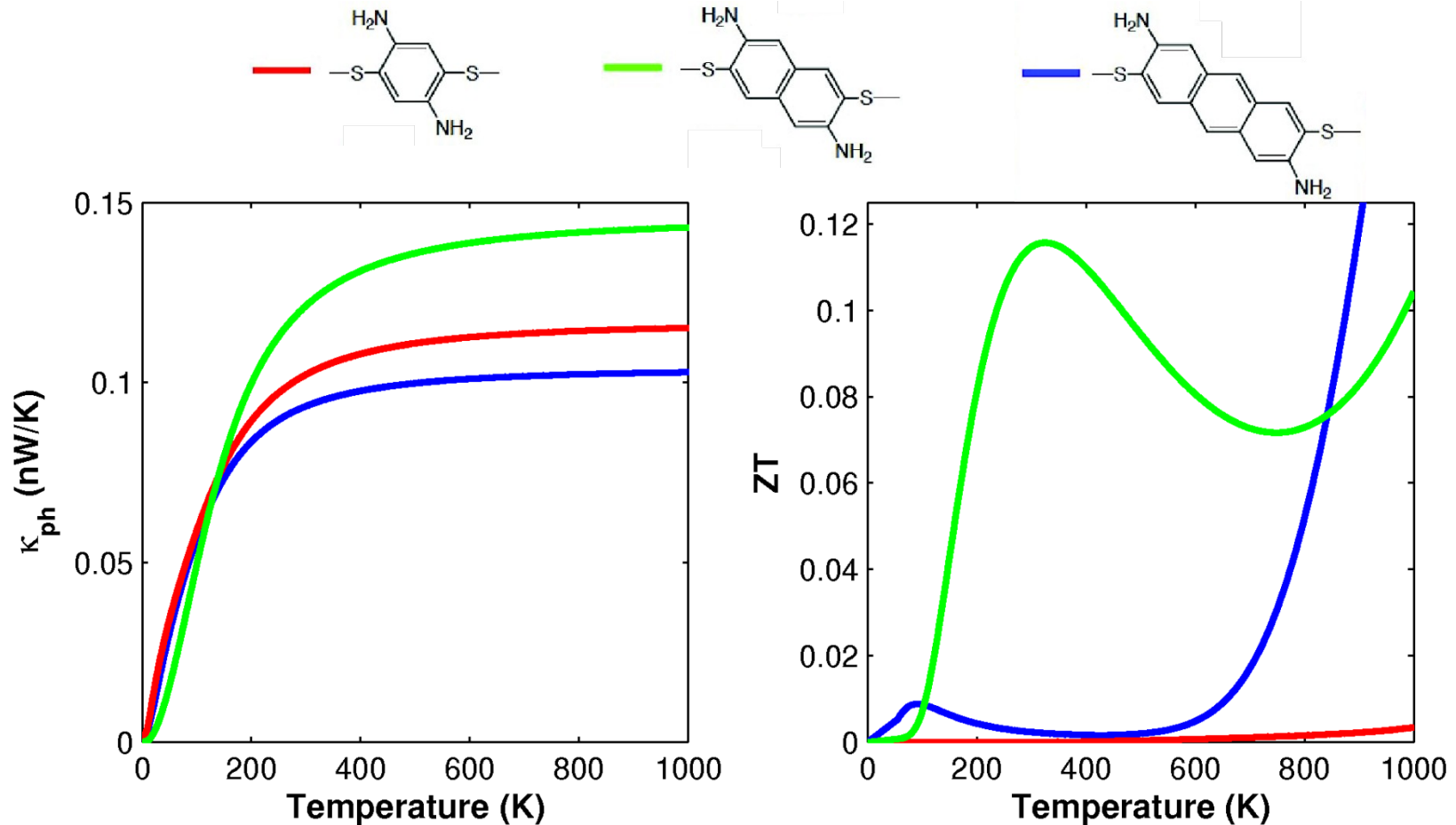


# influence of the linkers



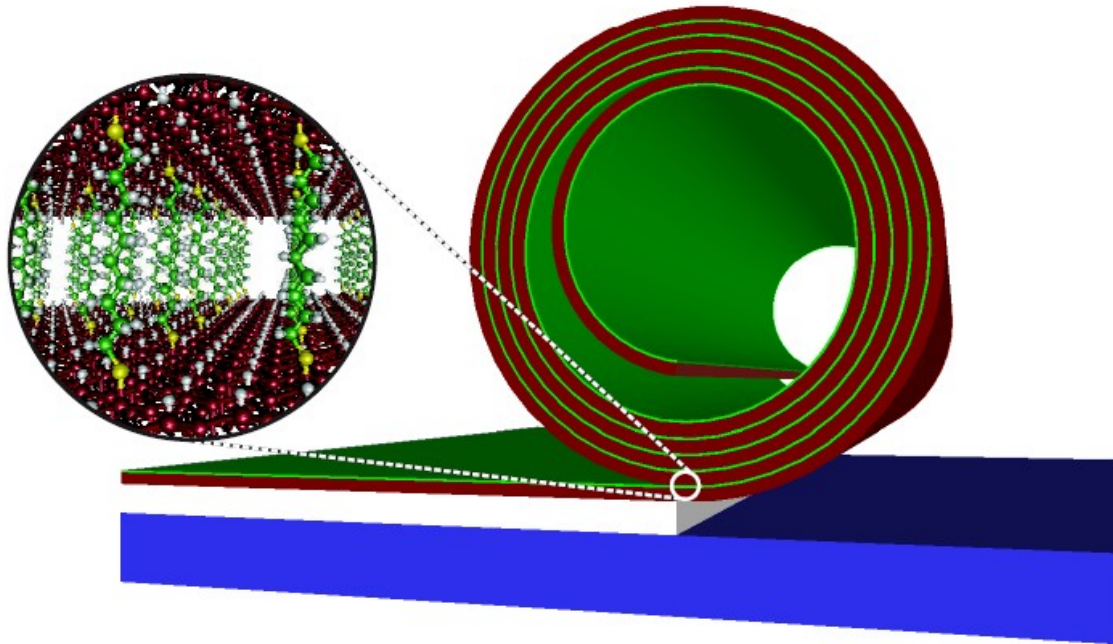
# electronic $ZT$ for polyacenes





Vibrational thermal conductance (**naphthalene**), around **150 pW/K @ RT**  
 $ZT_{max}$  is reduced to about **0.11 @ RT**

## Thermoelectricity in rolled-up functionalized Si-nanostructures



In cooperation with  
Oliver Schmidt (IFW Dresden)  
Within SPP 1386 *Nanostrukturierte Thermoelektrika:  
Theorie, Modellsysteme und kontrollierte Synthese*