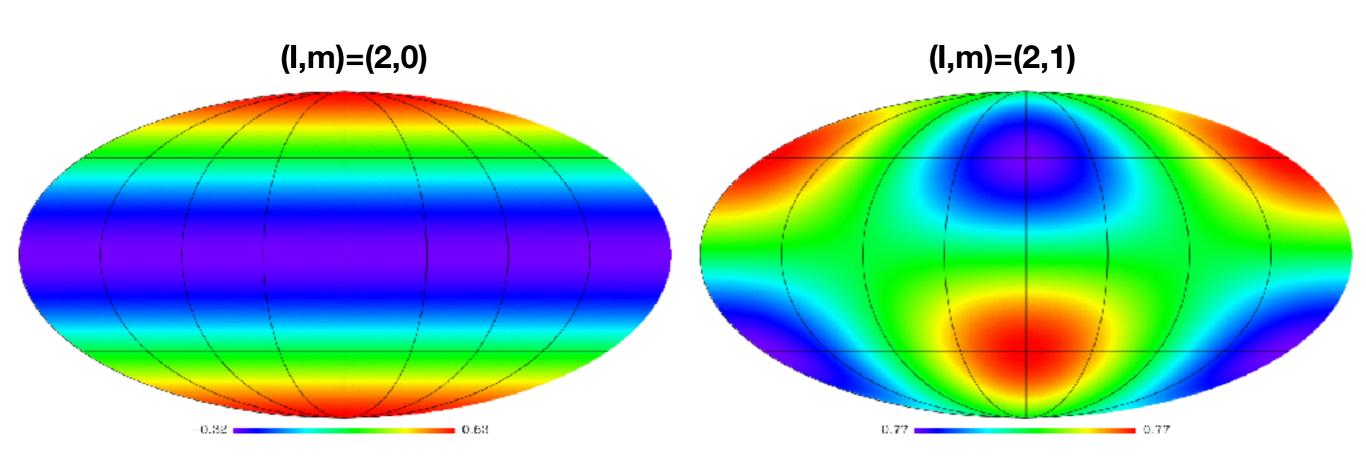
## Lecture 5

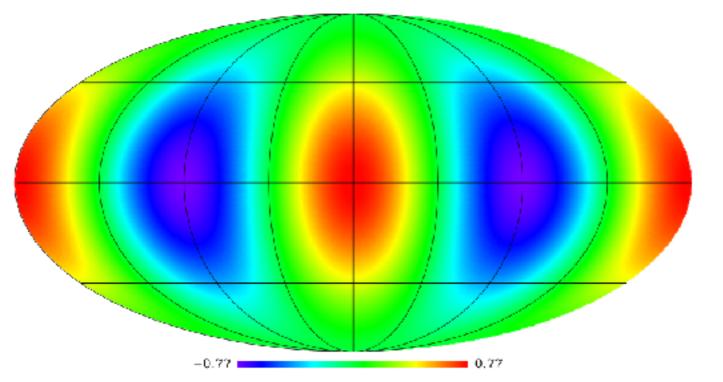
- Polarisation (continued)
- Gravitational waves and their imprints on the CMB

#### The Single Most Important Things You Need to Remeber

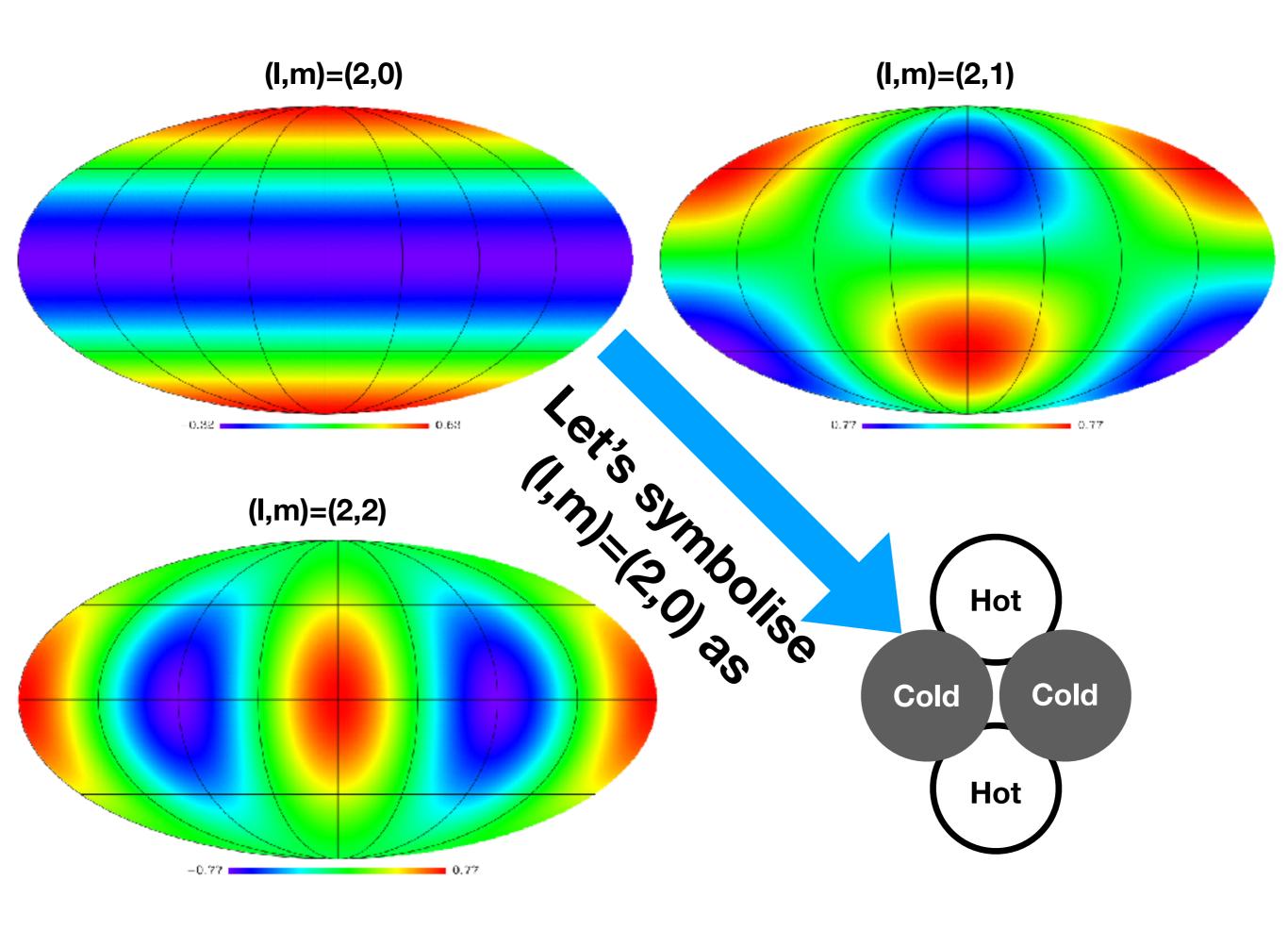
 Polarisation is generated by the local quadrupole temperature anisotropy, which is proportional to Viscosity

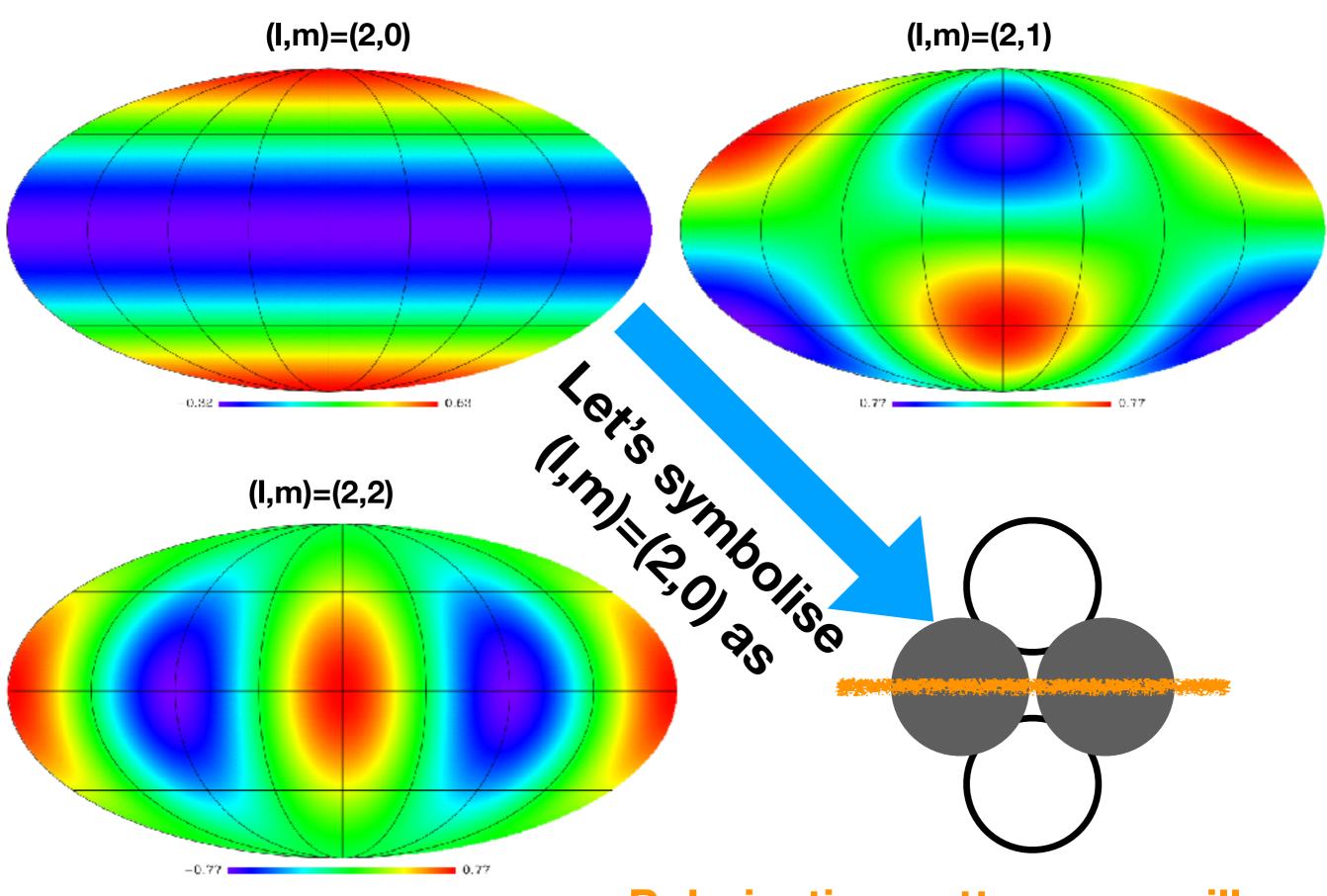


(l,m)=(2,2)

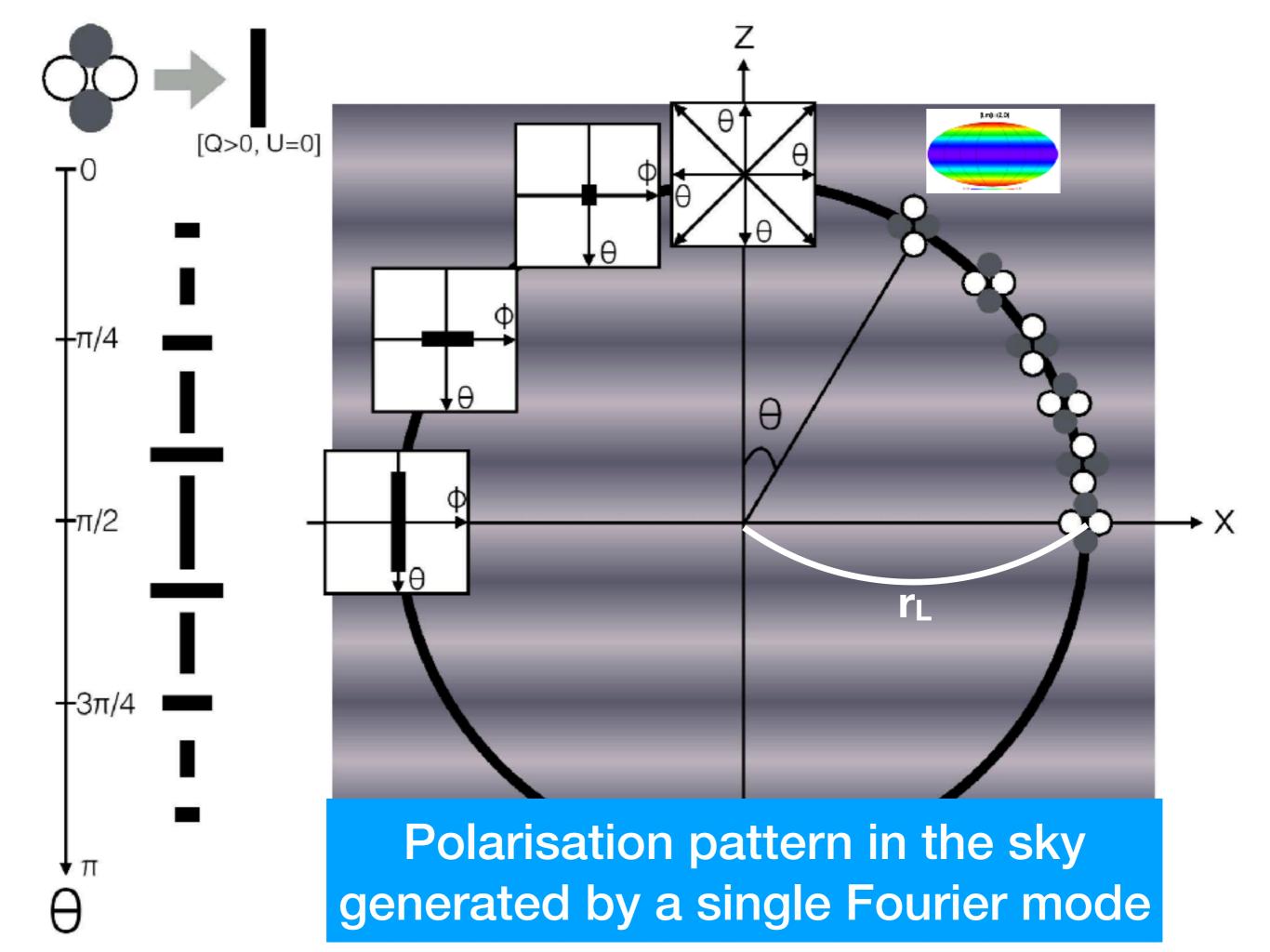


Local quadrupole temperature anisotropy seen from an electron





**Polarisation pattern you will see** 



θ [Q>0, U=0] θ θ, Œ +π/4 θ θ **E-mode!** -π/2 Х θ ٢L -3π/4 Polarisation pattern in the sky π generated by a single Fourier mode

## E-mode Power Spectrum

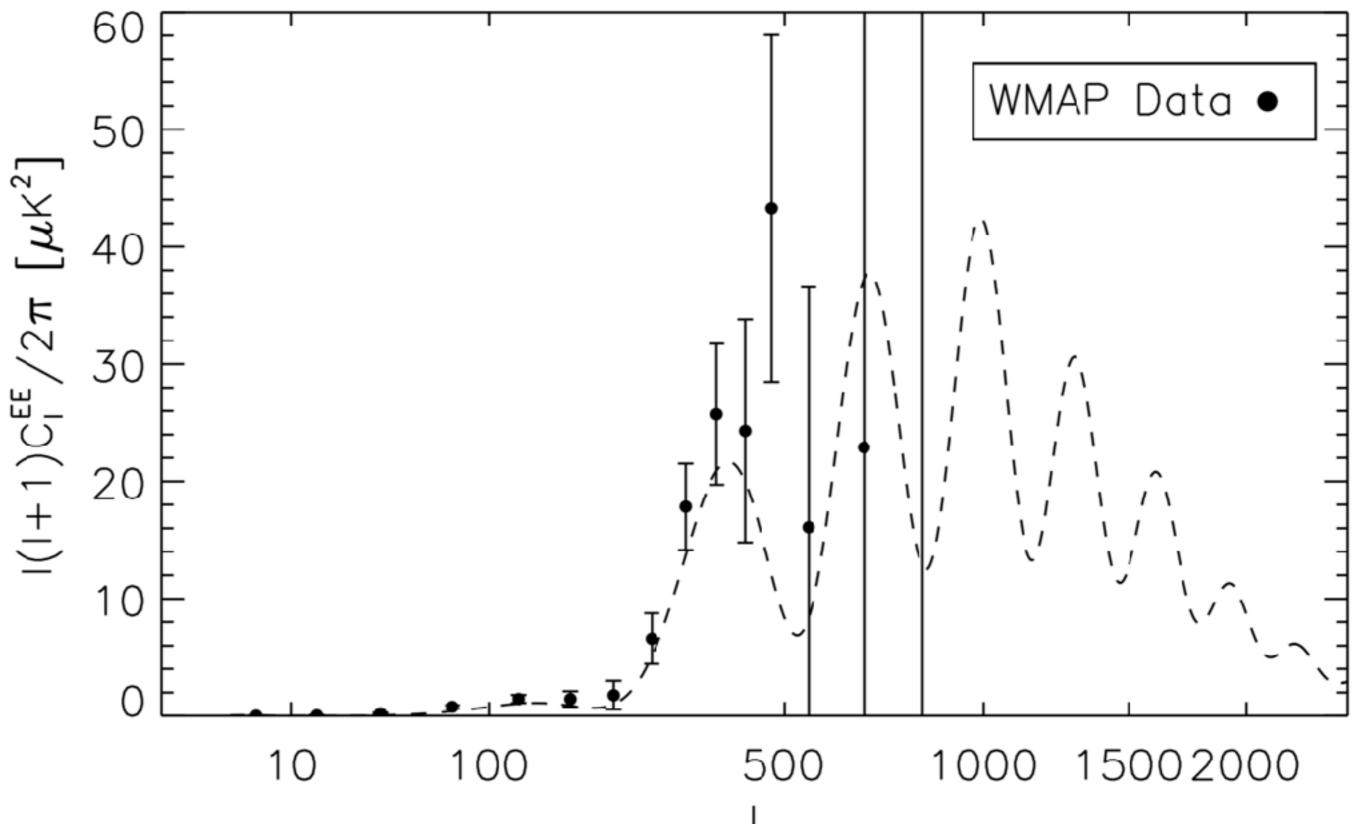
Viscosity at the last-scattering surface is given by the velocity potential:

$$\pi_{\gamma} = -\frac{32}{45} \frac{\bar{\rho}_{\gamma}}{\sigma_{\tau} \bar{n}_{e}} \frac{\delta u_{\gamma}}{a^{2}}$$

• Velocity potential is  $Sin(qr_L)$ , whereas the temperature power spectrum is predominantly  $Cos(qr_L)$ 

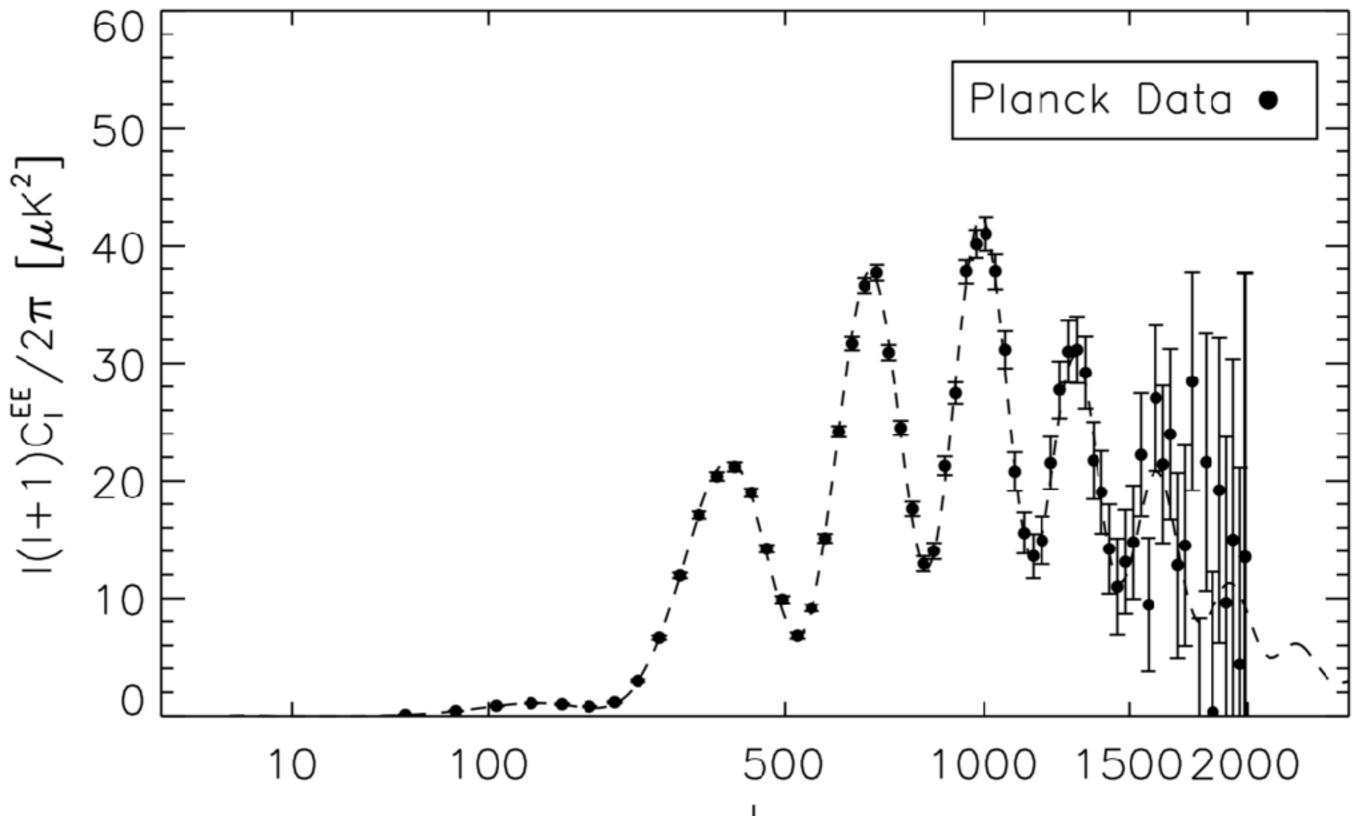
Bennett et al. (2013)

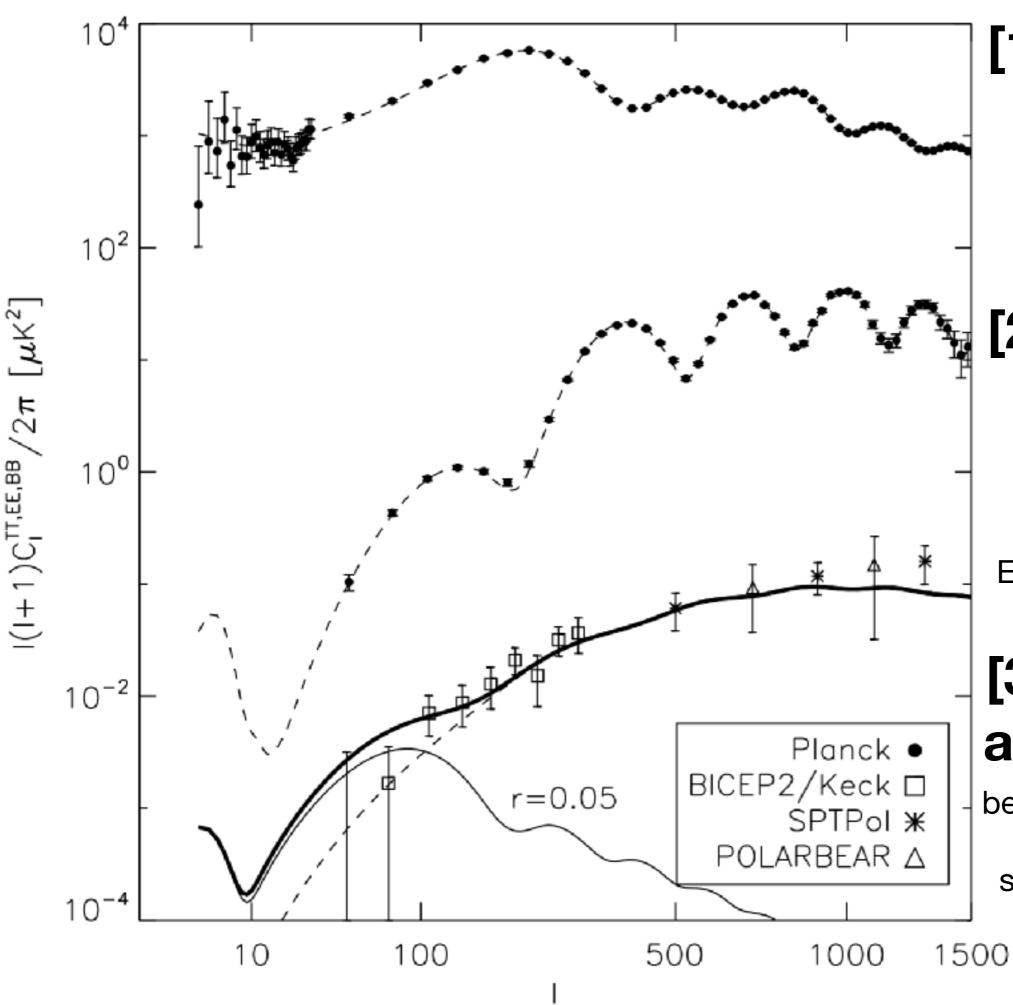
#### WMAP 9-year Power Spectrum



Planck Collaboration (2016)

#### Planck 29-mo Power Spectrum





#### [1] Trough in T -> Peak in E

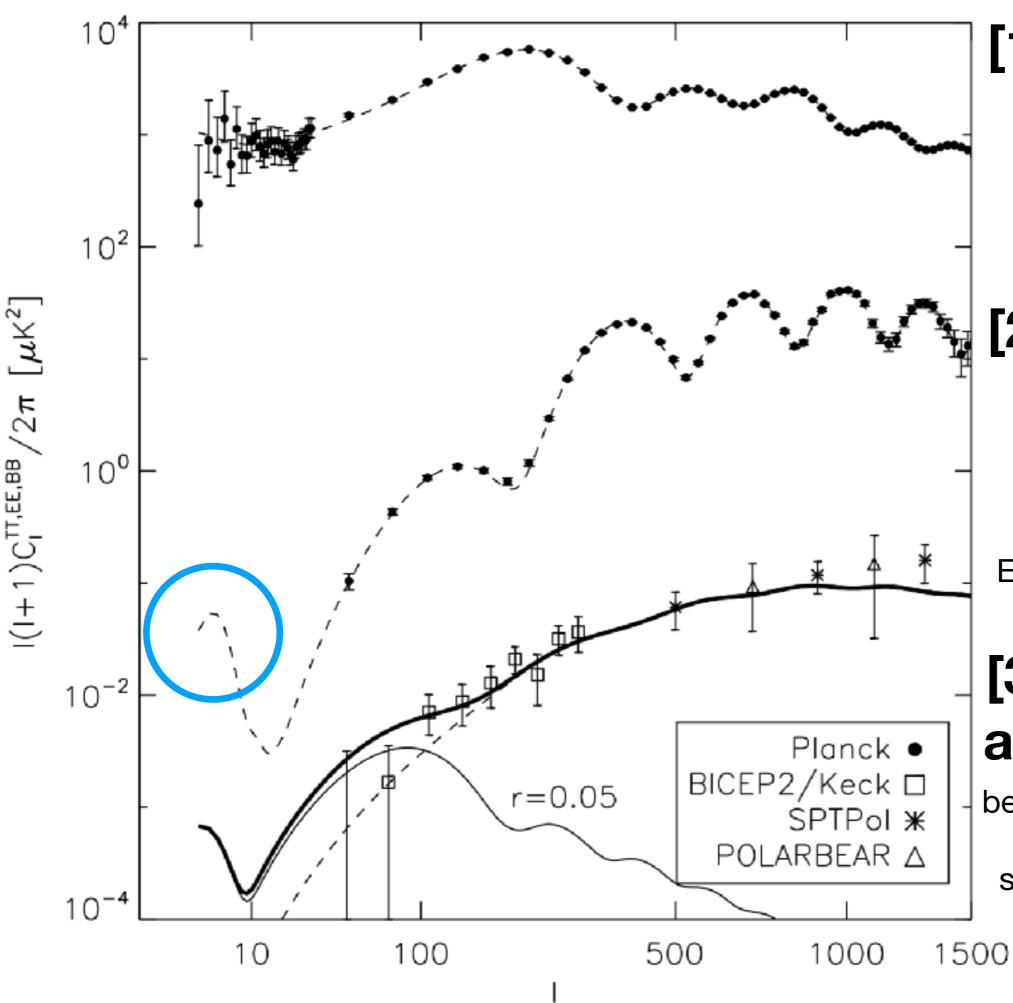
because  $C_{I}^{TT} \sim cos^{2}(qr_{s})$ whereas  $C_{I}^{EE} \sim sin^{2}(qr_{s})$ 

#### [2] T damps -> E rises

because T damps by viscosity, whereas E is created by viscosity

#### [3] E Peaks are sharper

because C<sub>I</sub><sup>TT</sup> is the sum of cos<sup>2</sup>(qr<sub>L</sub>) and Doppler shift's sin<sup>2</sup>(qr<sub>L</sub>), whereas C<sub>I</sub><sup>EE</sup> is just sin<sup>2</sup>(qr<sub>L</sub>)



#### [1] Trough in T -> Peak in E

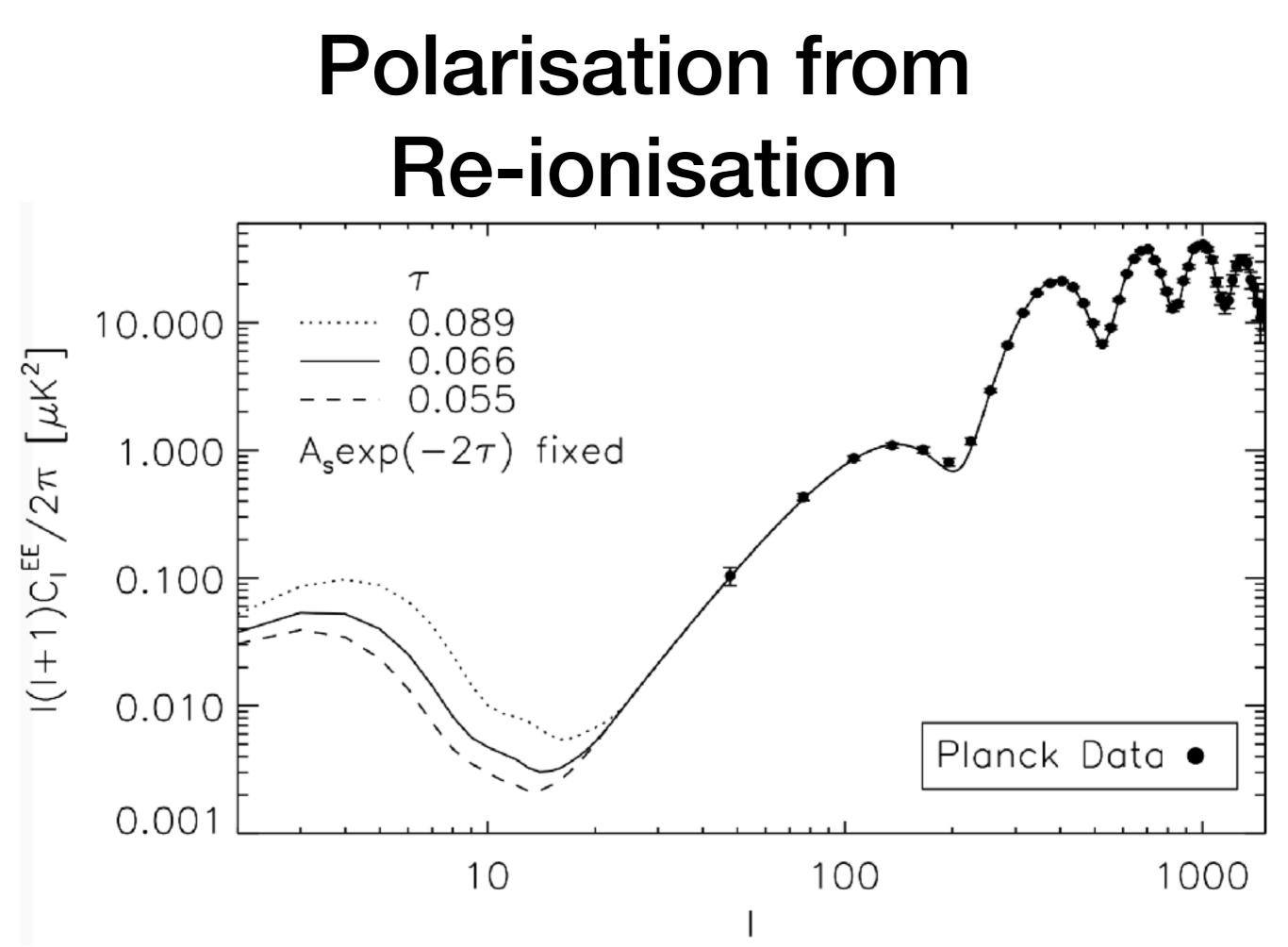
because  $C_{I}^{TT} \sim cos^{2}(qr_{s})$ whereas  $C_{I}^{EE} \sim sin^{2}(qr_{s})$ 

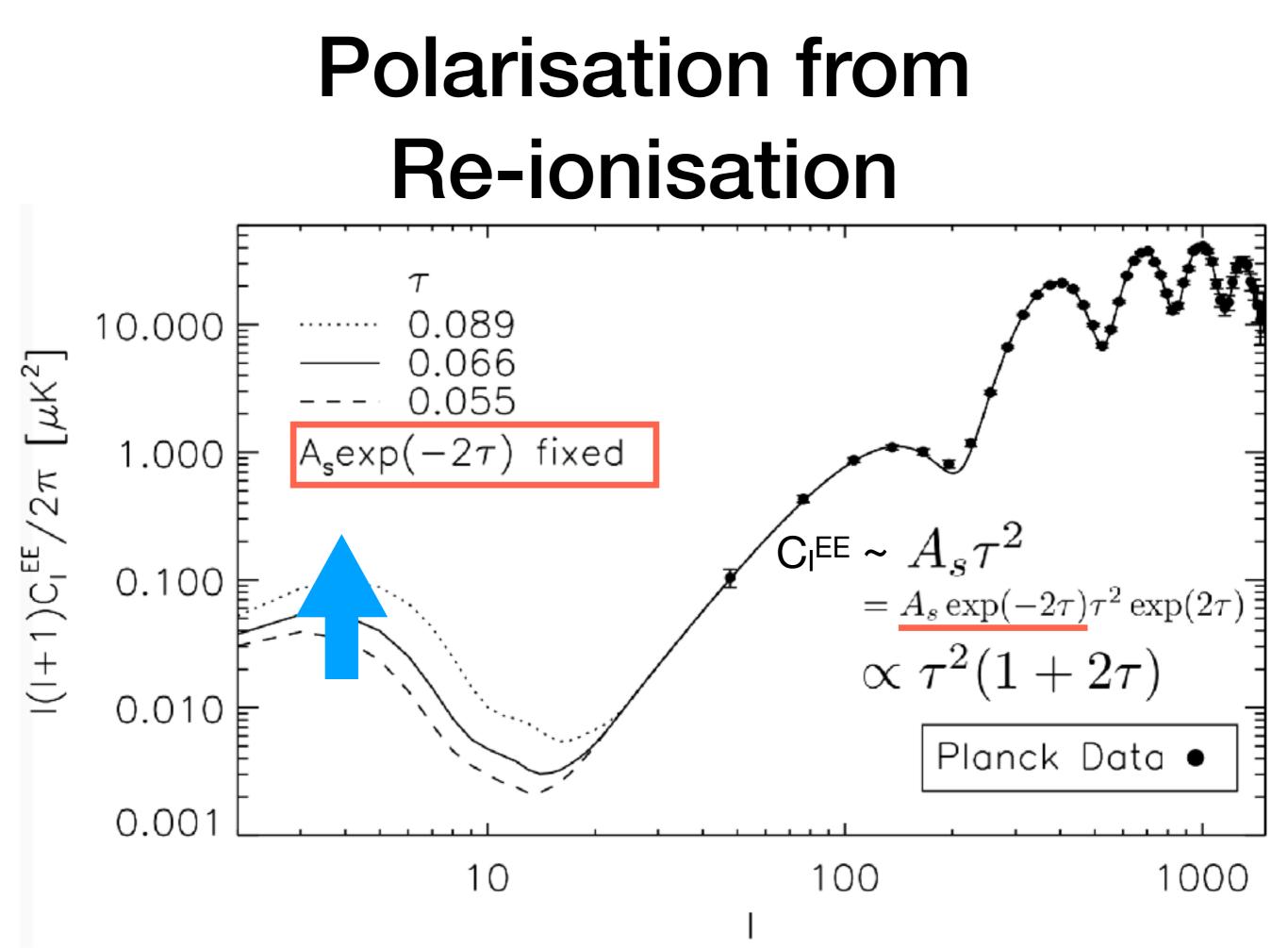
#### [2] T damps -> E rises

because T damps by viscosity, whereas E is created by viscosity

#### [3] E Peaks are sharper

because C<sub>I</sub><sup>TT</sup> is the sum of cos<sup>2</sup>(qr<sub>L</sub>) and Doppler shift's sin<sup>2</sup>(qr<sub>L</sub>), whereas C<sub>I</sub><sup>EE</sup> is just sin<sup>2</sup>(qr<sub>L</sub>)



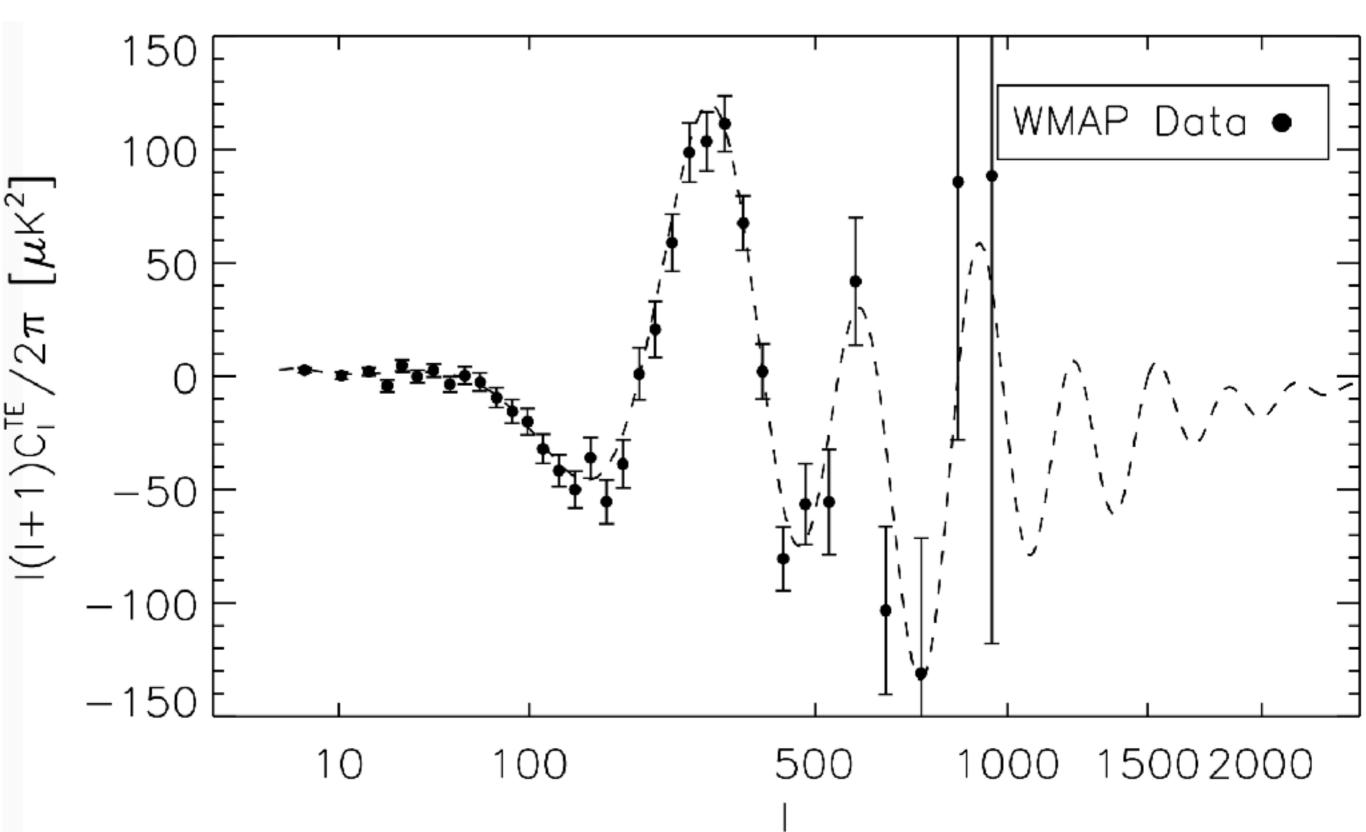


#### Cross-correlation between T and E

- Velocity potential is  $Sin(qr_L)$ , whereas the temperature power spectrum is predominantly  $Cos(qr_L)$
- Thus, the TE correlation is Sin(qr<sub>L</sub>)Cos(qr<sub>L</sub>) which can change sign

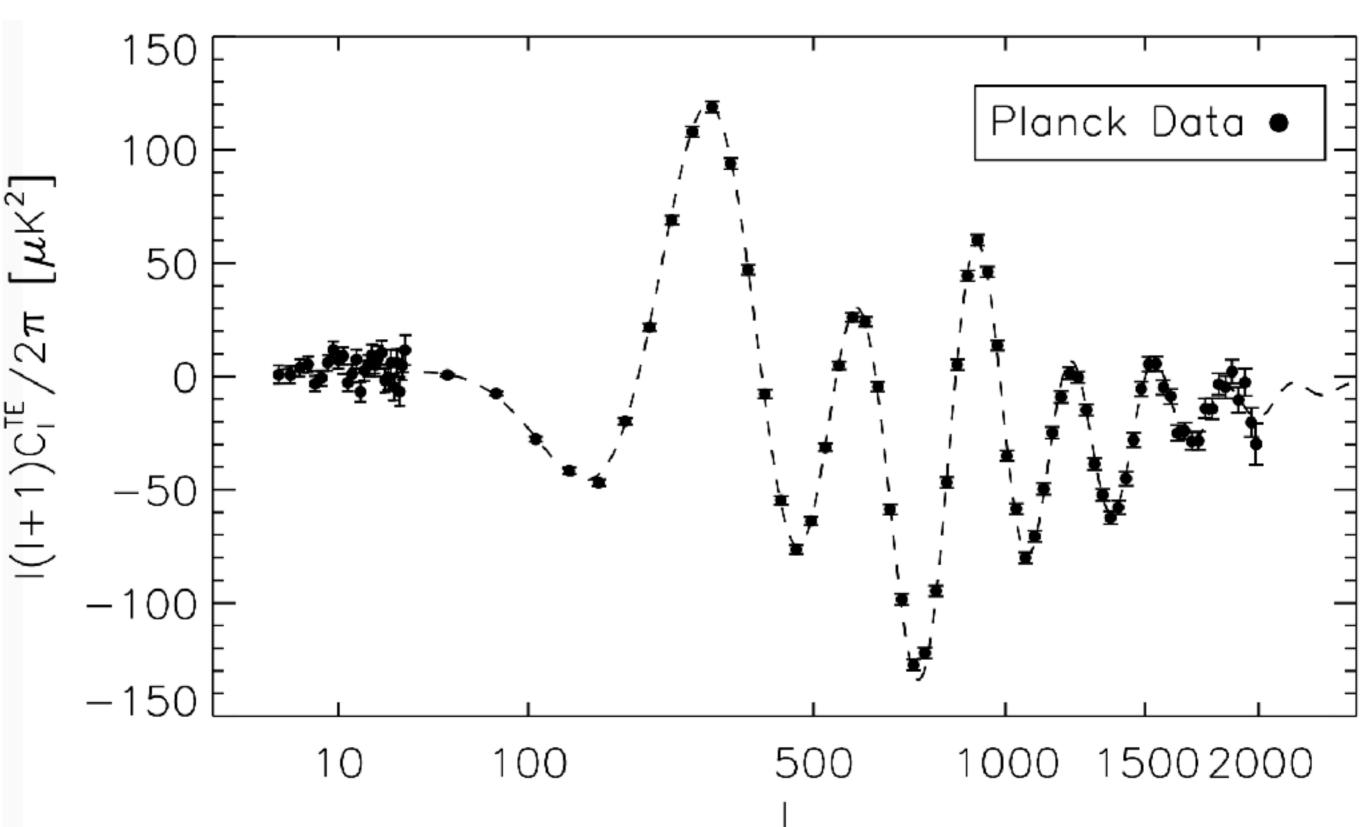
Bennett et al. (2013)

### WMAP 9-year Power Spectrum



Planck Collaboration (2016)

#### Planck 29-mo Power Spectrum

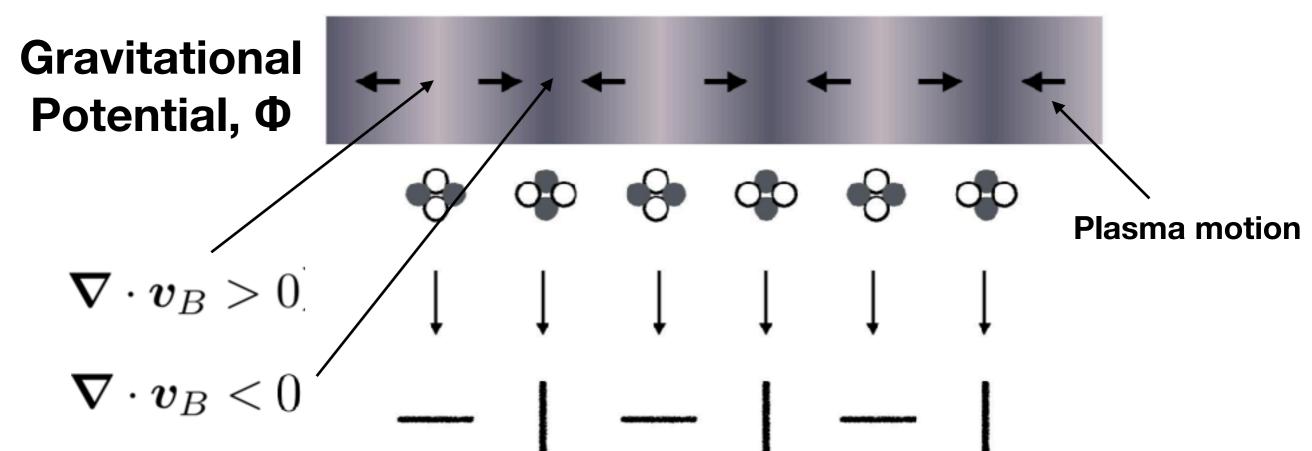


## TE correlation is useful for understanding physics

- Troughly traces gravitational potential, while E traces velocity  $q^2\pi_\gamma\propto -q^2\delta u_\gamma\propto {f \nabla}\cdot {f v}_B$
- With TE, we witness how plasma falls into gravitational potential wells!

Coulson et al. (1994)

#### Example: Gravitational Effects

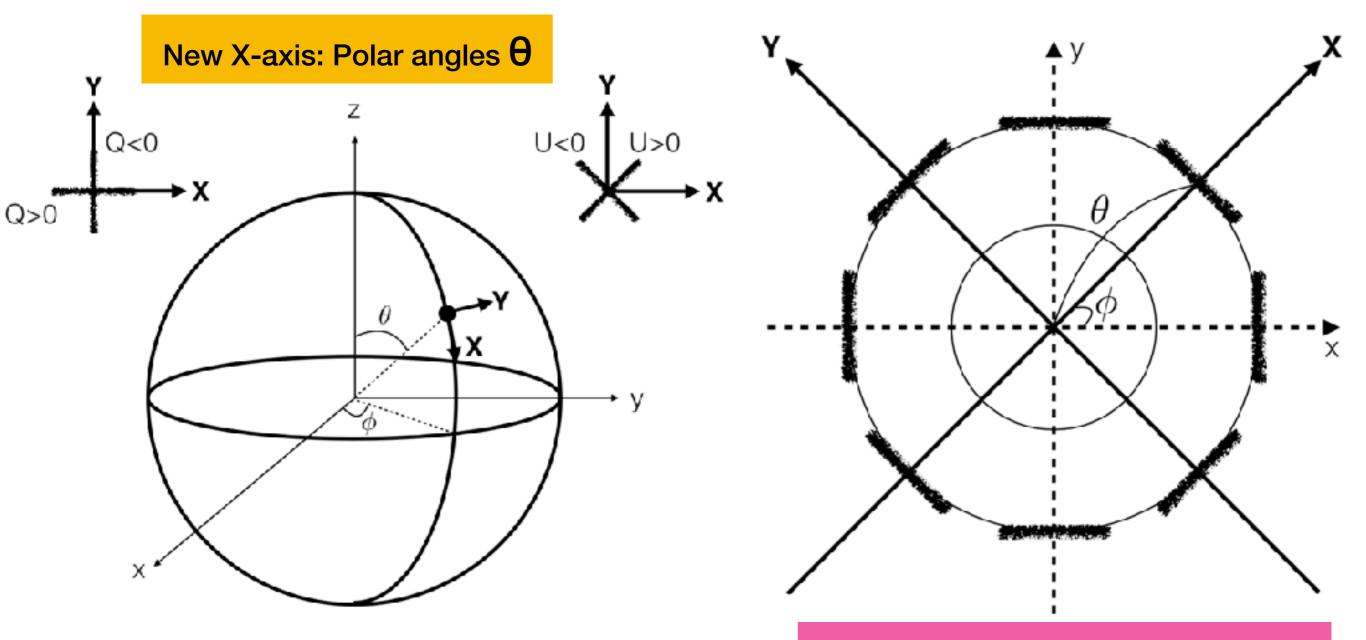


$$q^2 \pi_\gamma \propto -q^2 \delta u_\gamma \propto {oldsymbol 
abla} \cdot {oldsymbol v}_B$$



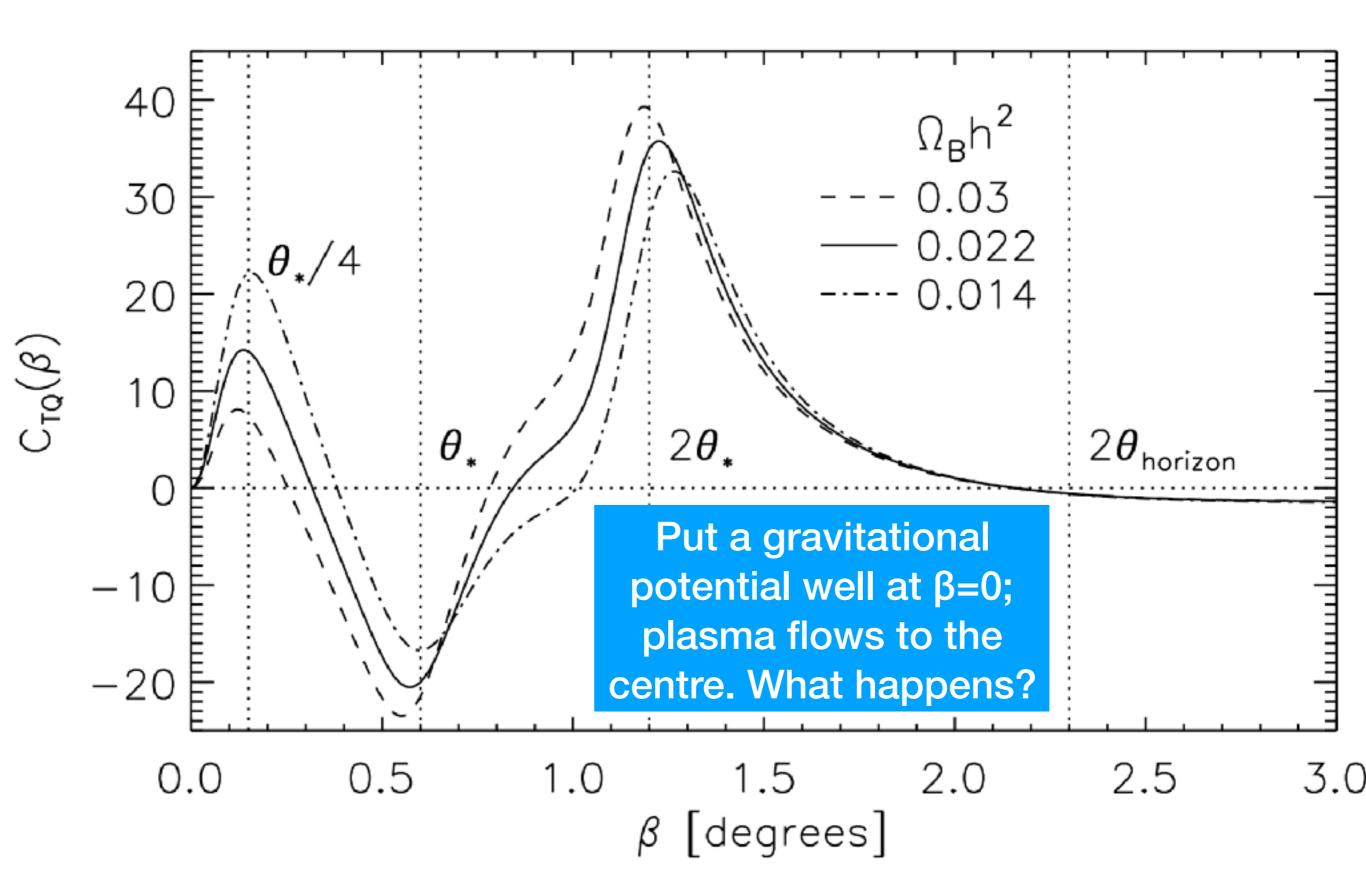
#### TE correlation in angular space

First, let's define Stokes parameters in sphere



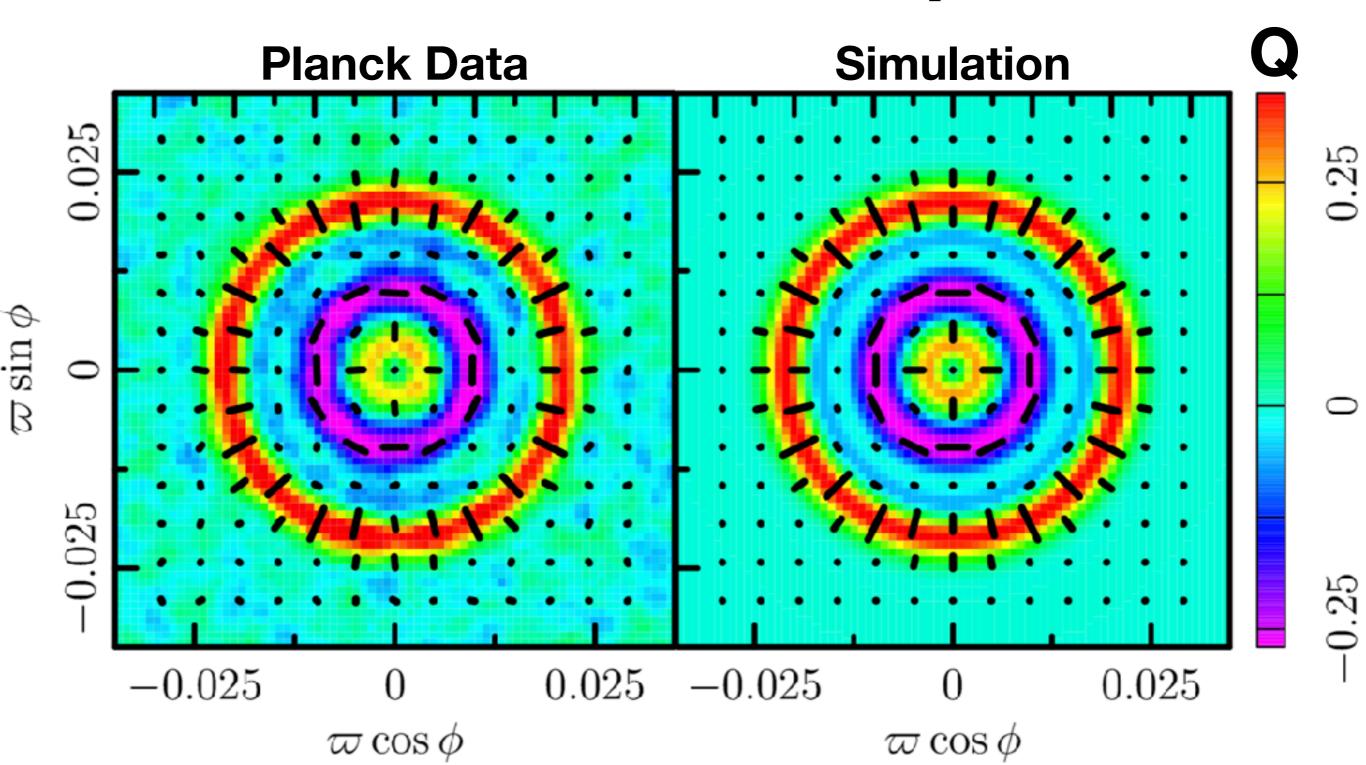
In this example, they are all Q<0

## TE correlation in angular space



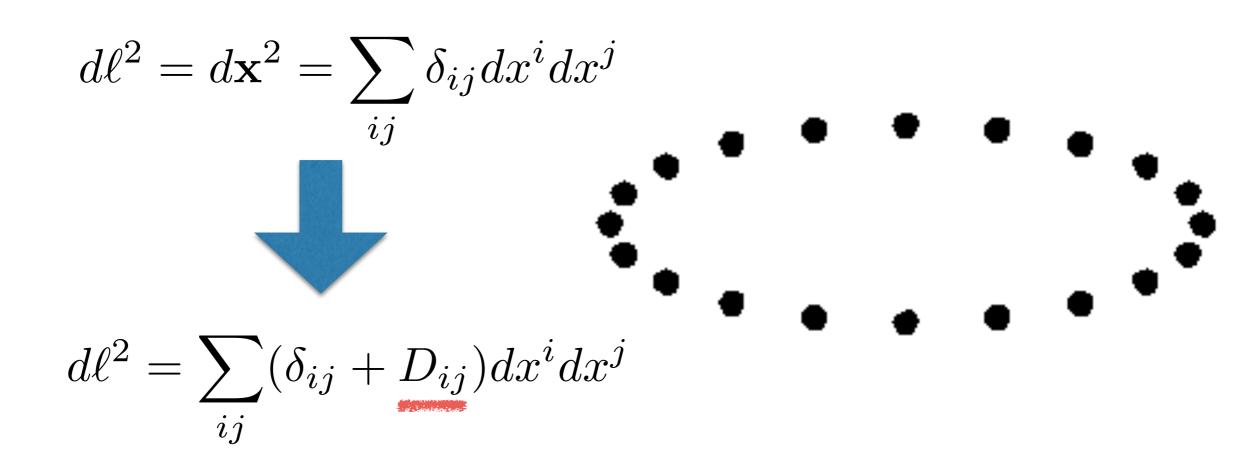
Komatsu et al. (2011); Planck Collaboration (2016)

# Average Q polarisation around temperature hot spots

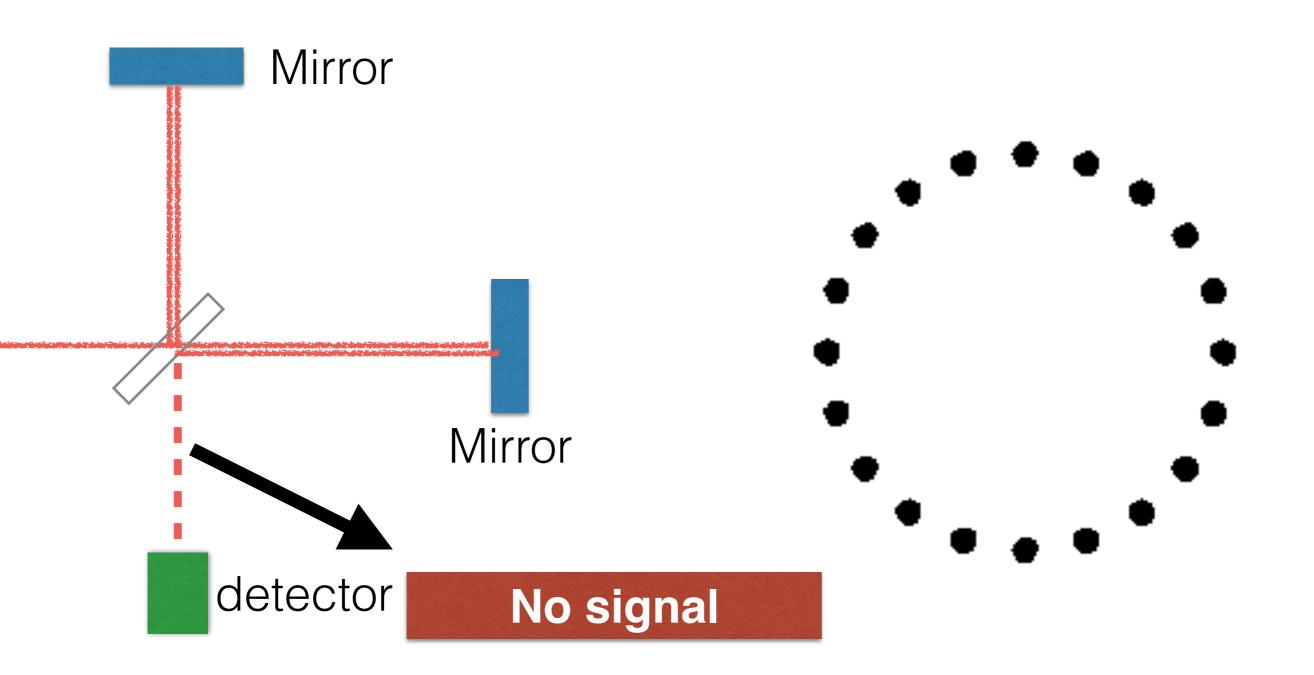


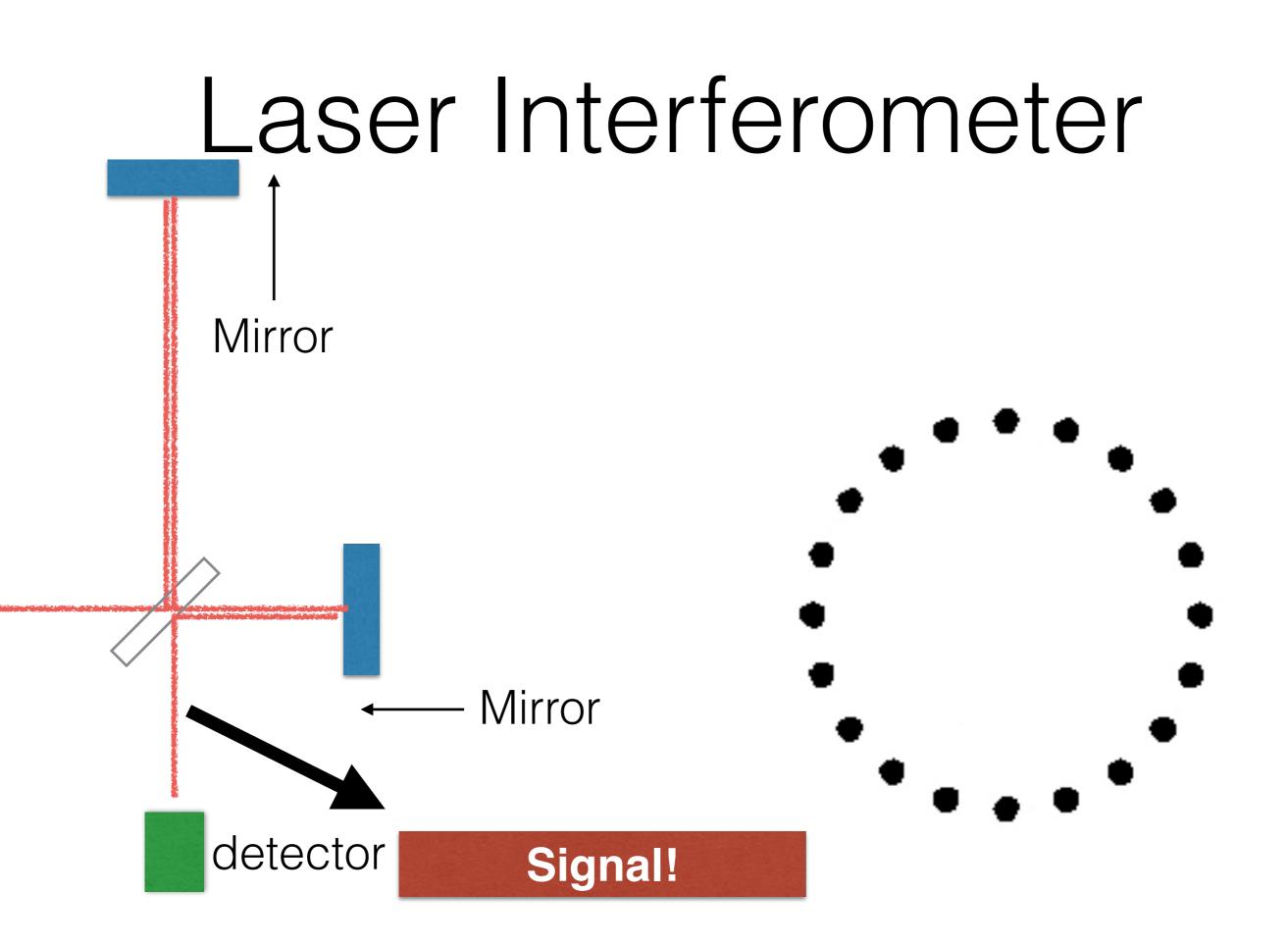
## Gravitational Waves

• GW changes the distances between two points

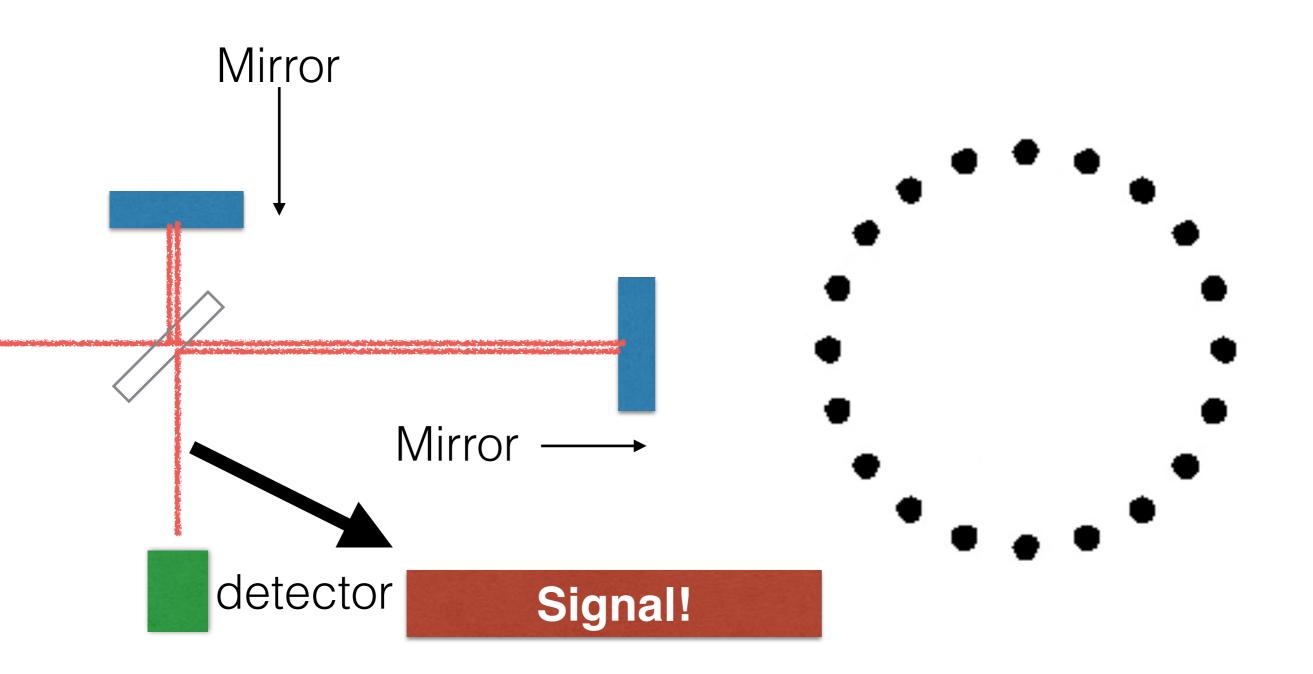


## Laser Interferometer





## Laser Interferometer



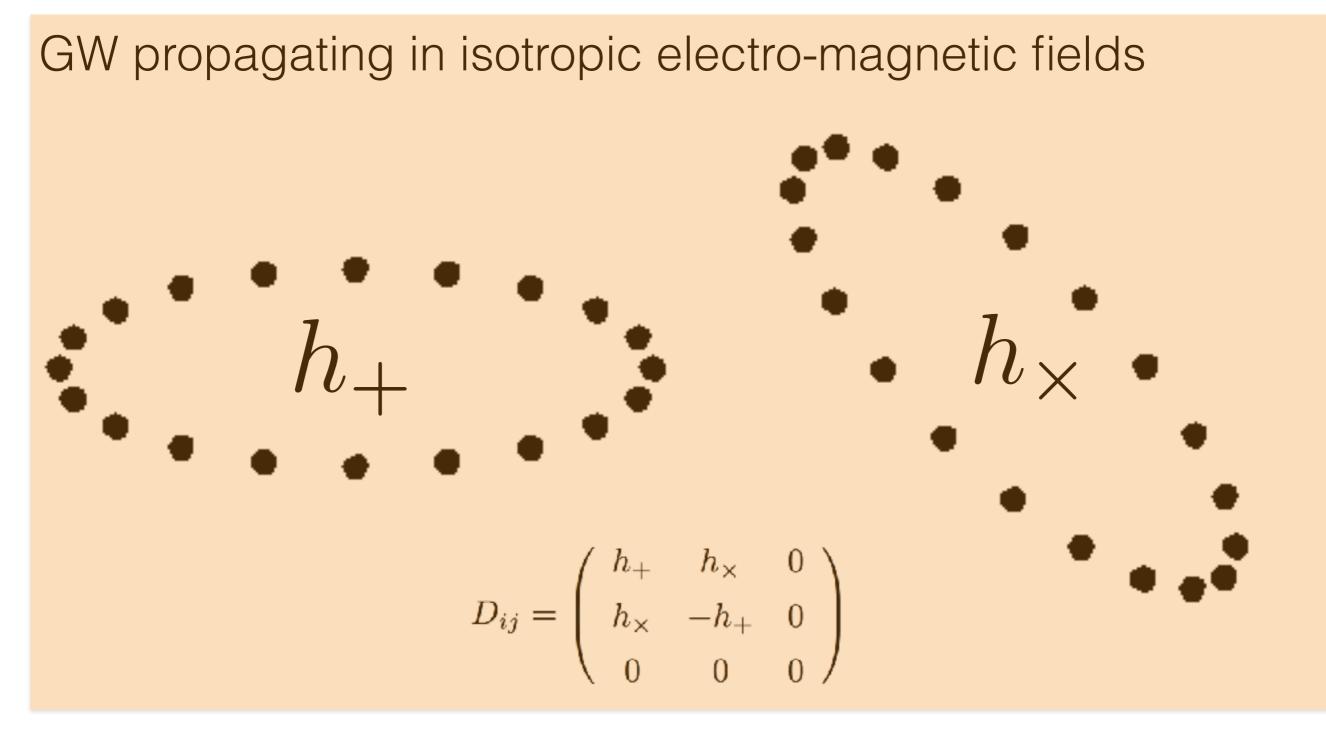
LIGO detected GW from binary blackholes, with the wavelength of thousands of kilometres

But, the primordial GW affecting the CMB has a wavelength of **billions of light-years**!! How do we find it?

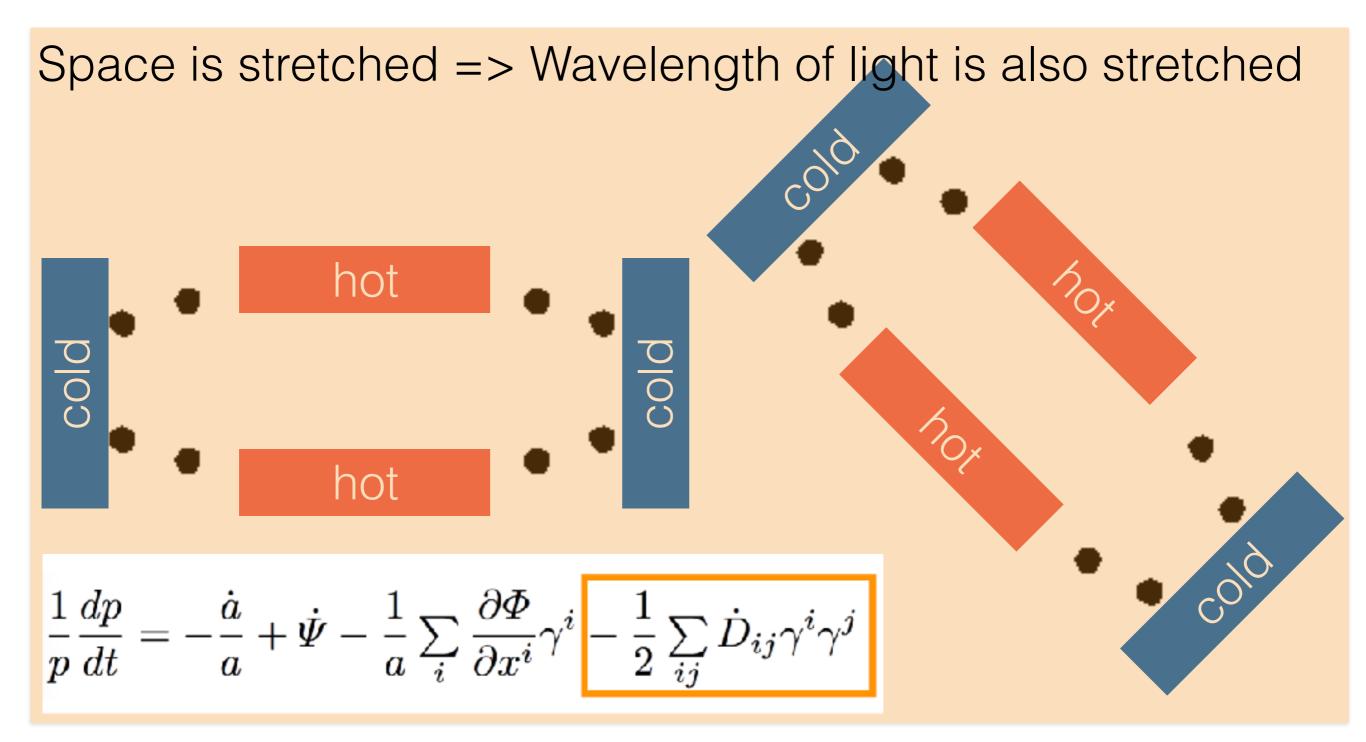
## Detecting GW by CMB

Isotropic electro-magnetic fields

# Detecting GW by CMB

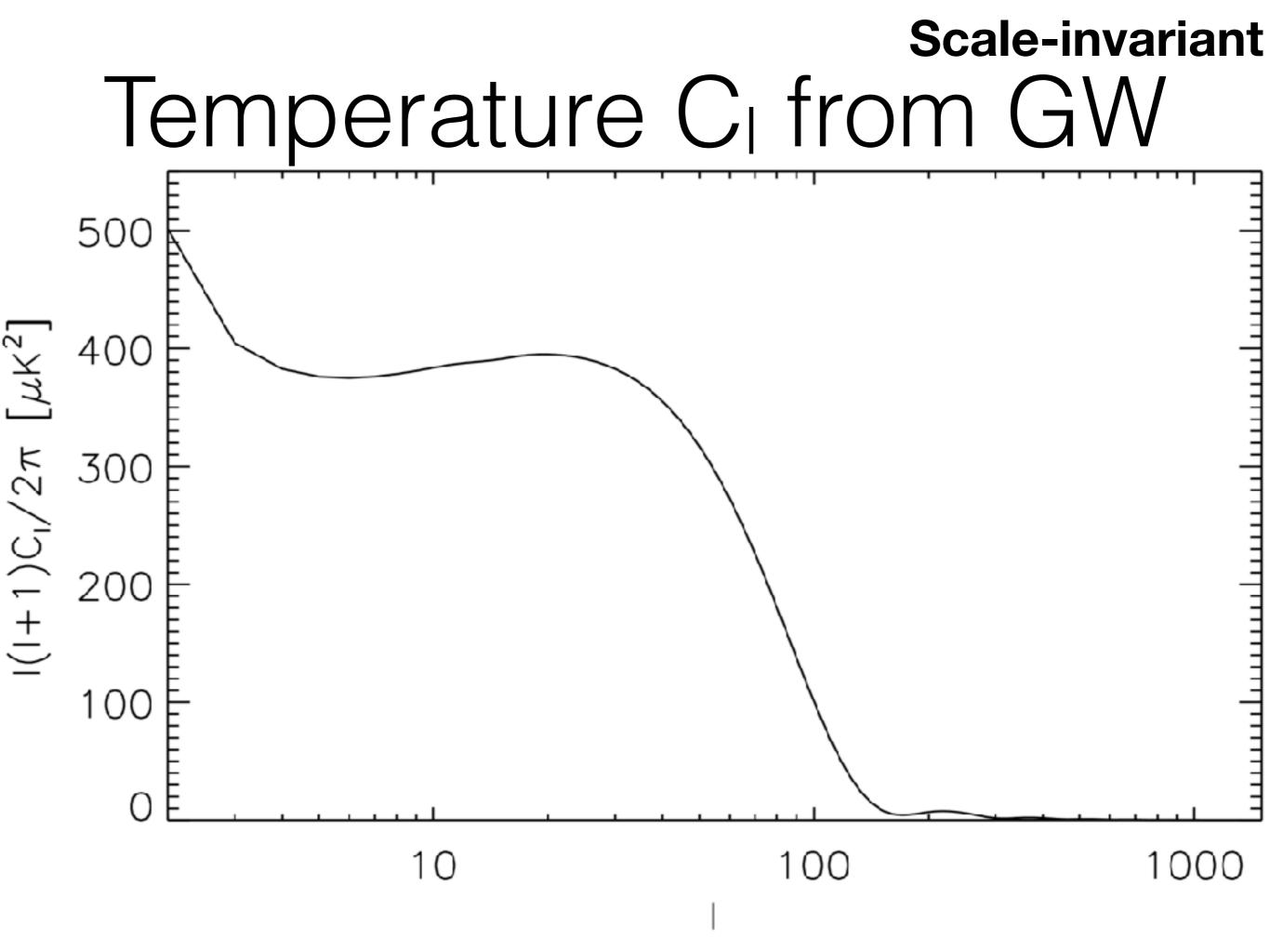


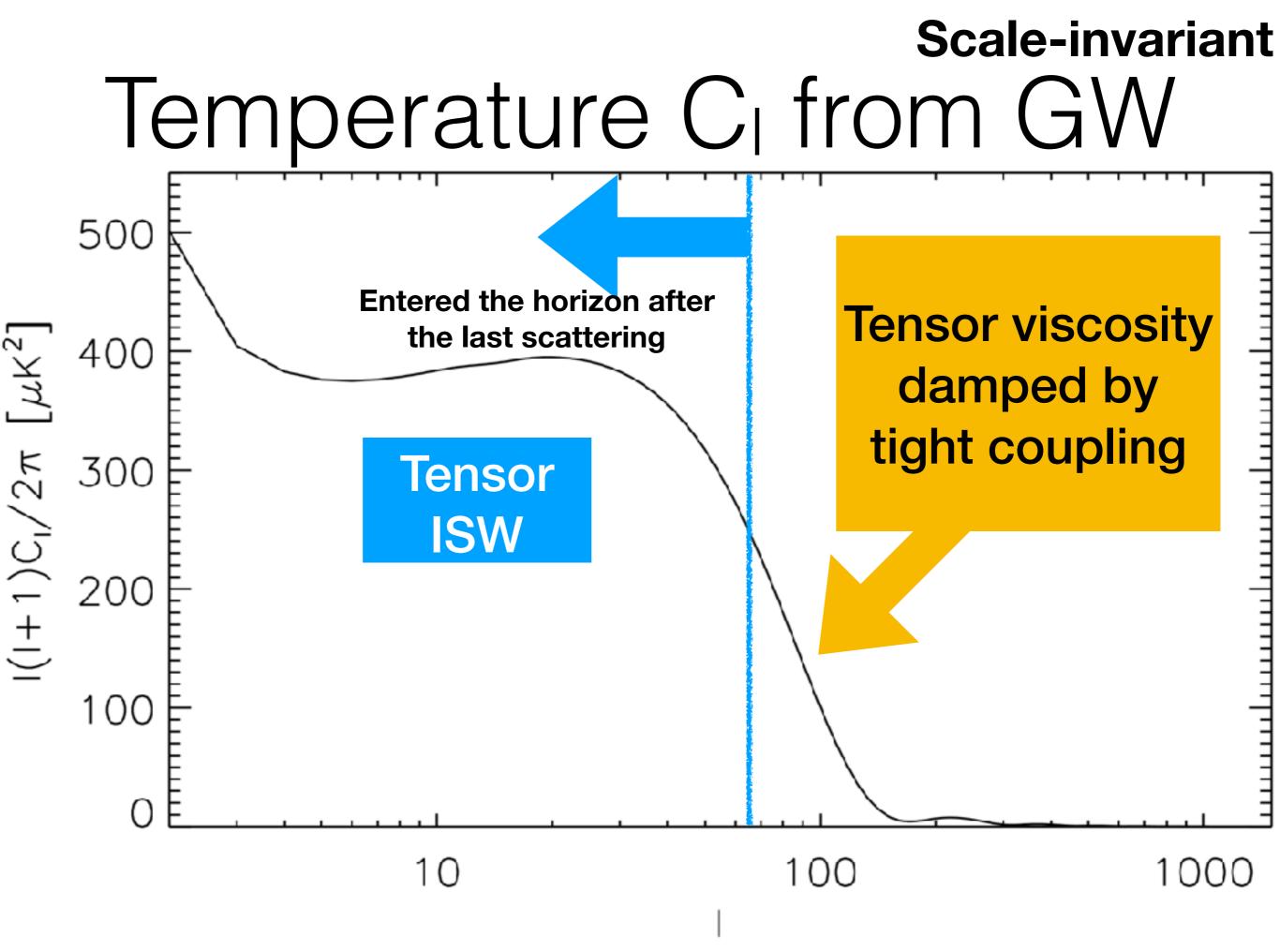
# Detecting GW by CMB



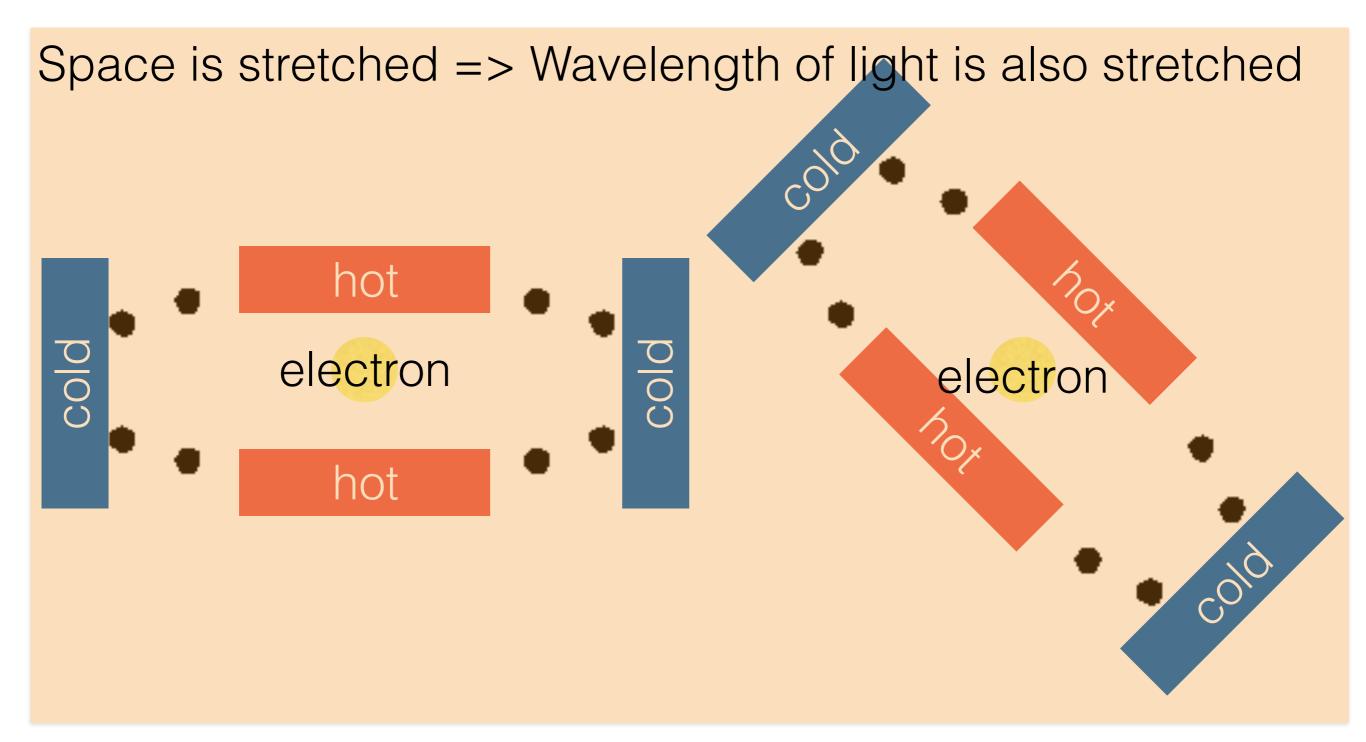
# Generation and erasure of tensor quadrupole (viscosity)

- Gravitational waves create quadrupole temperature anisotropy [i.e., tensor viscosity of a photonbaryon fluid] gravitationally, without velocity potential
- Still, tight-coupling between photons and baryons erases the tensor viscosity exponentially before the last scattering

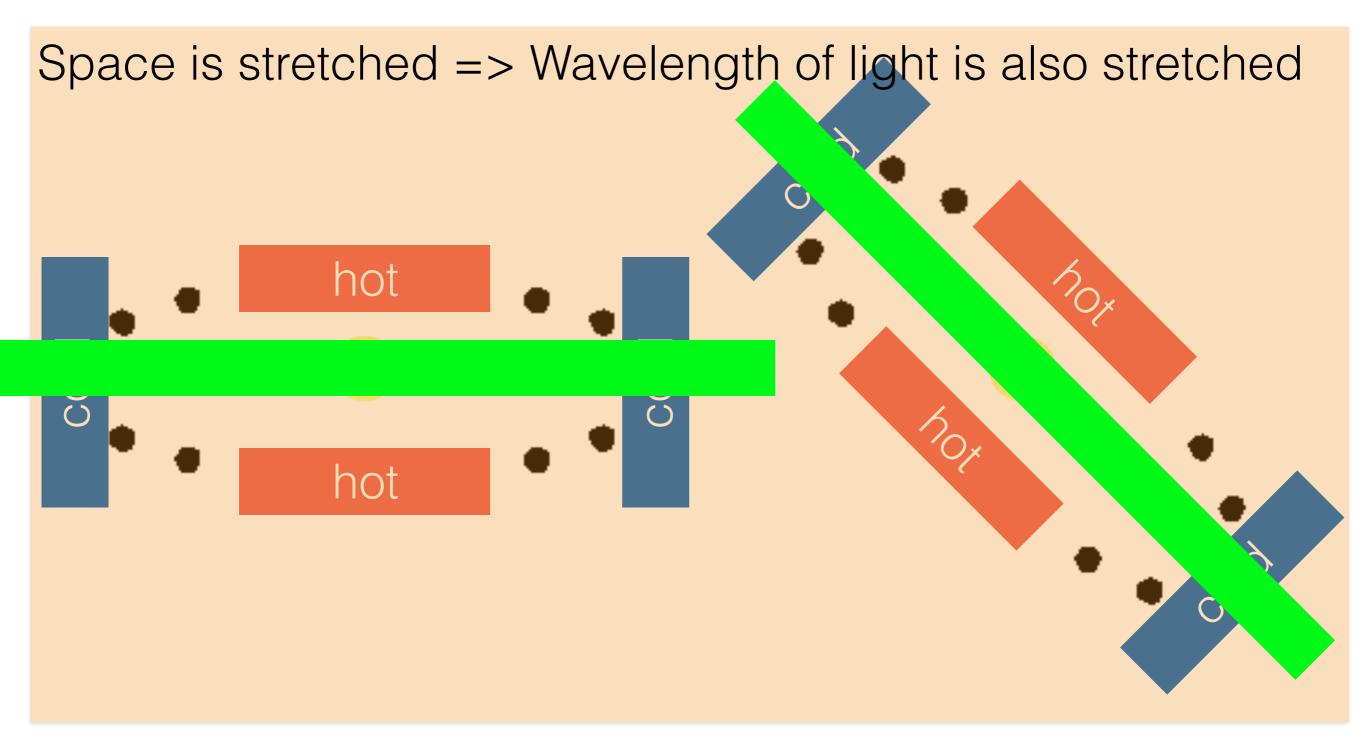


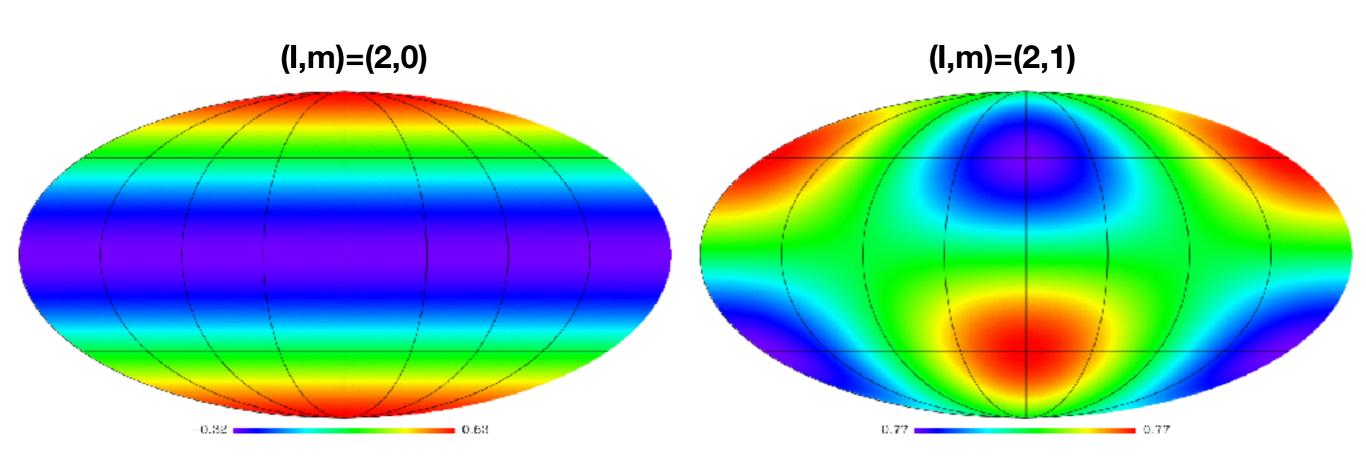


#### Detecting GW by CMB Polarisation

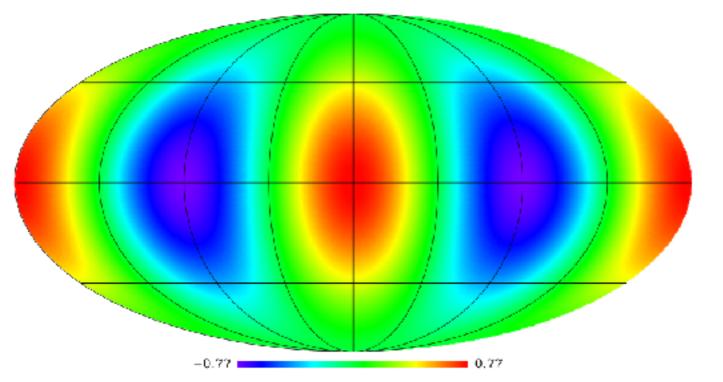


#### Detecting GW by CMB Polarisation

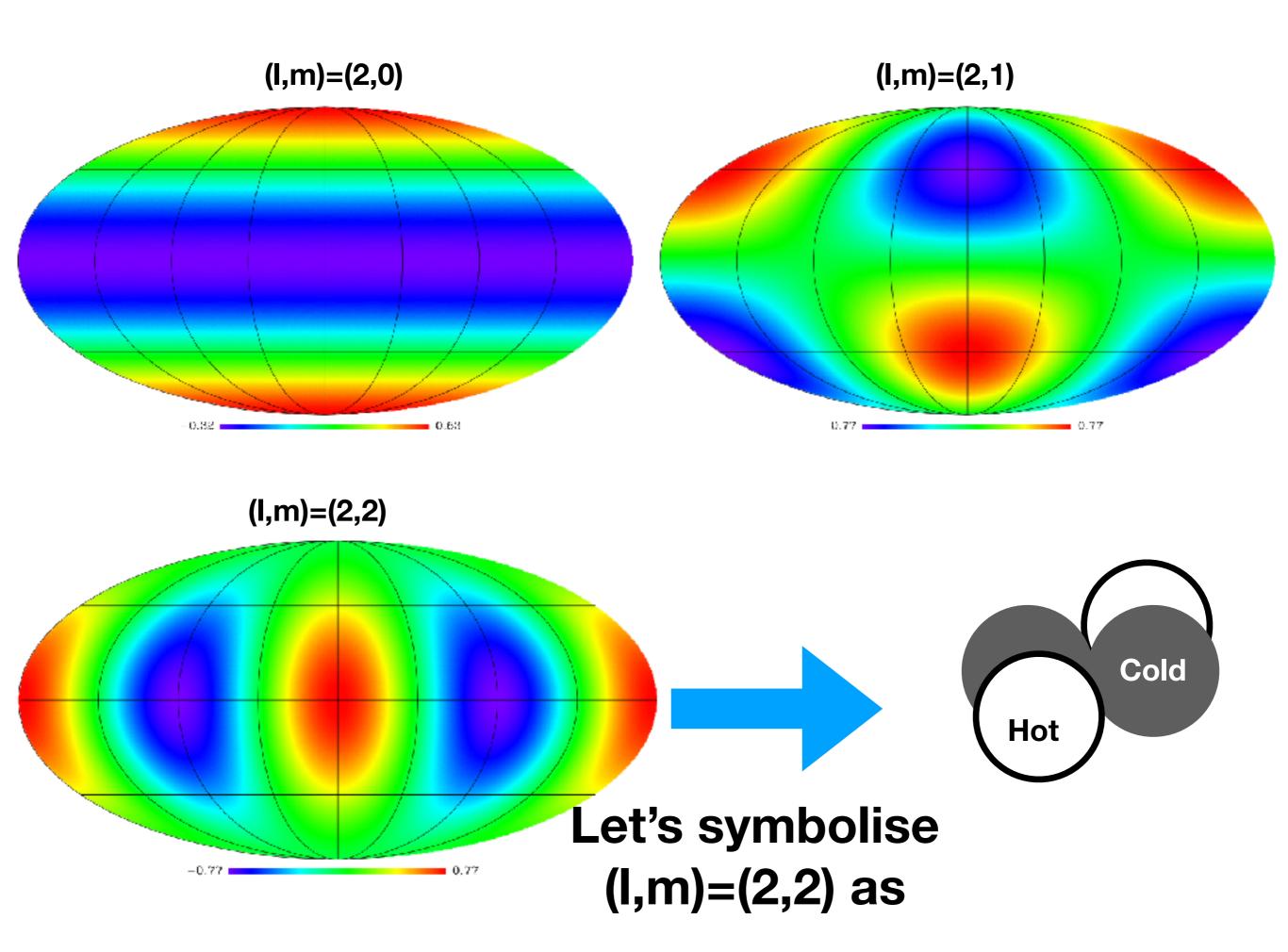


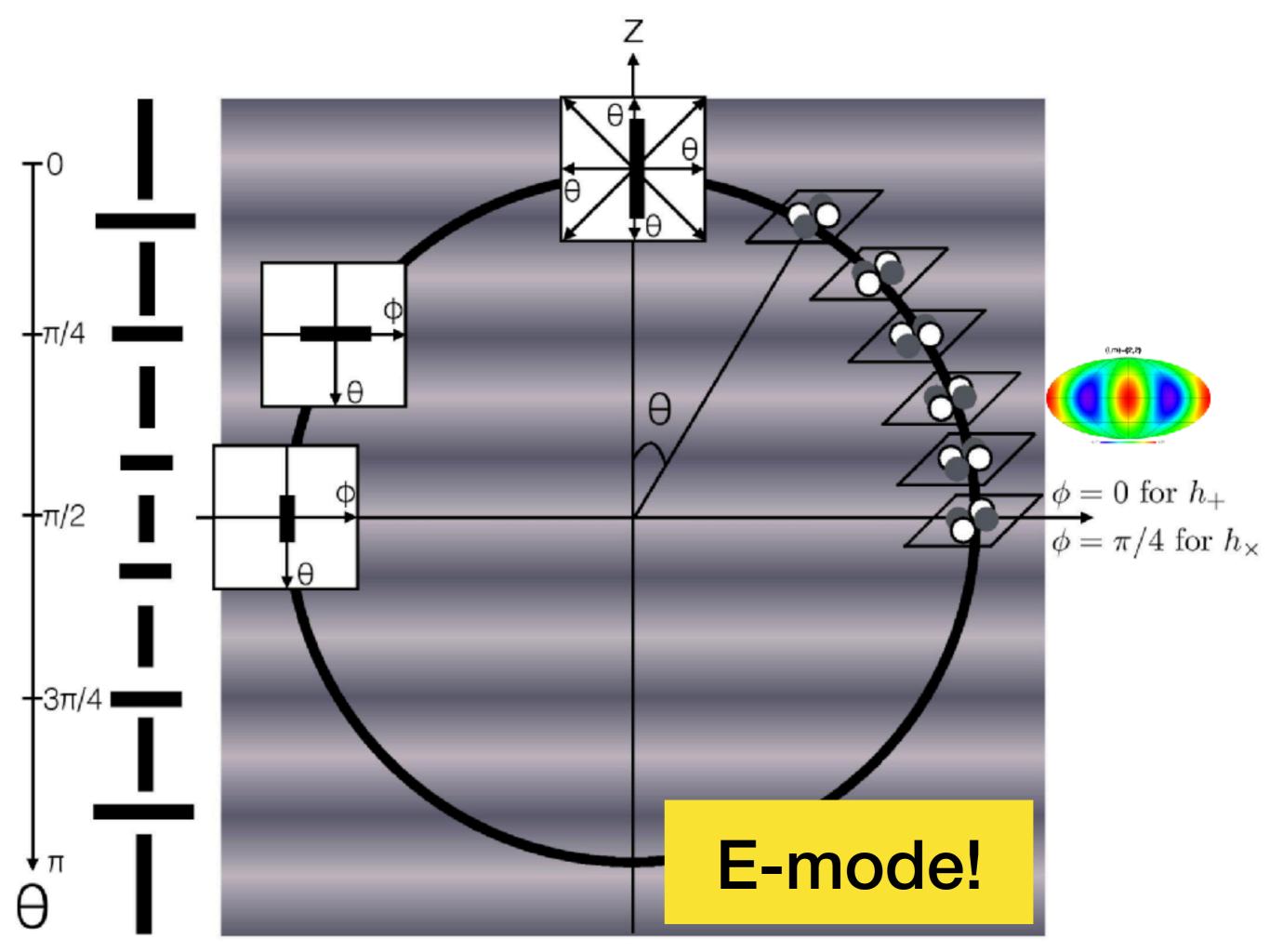


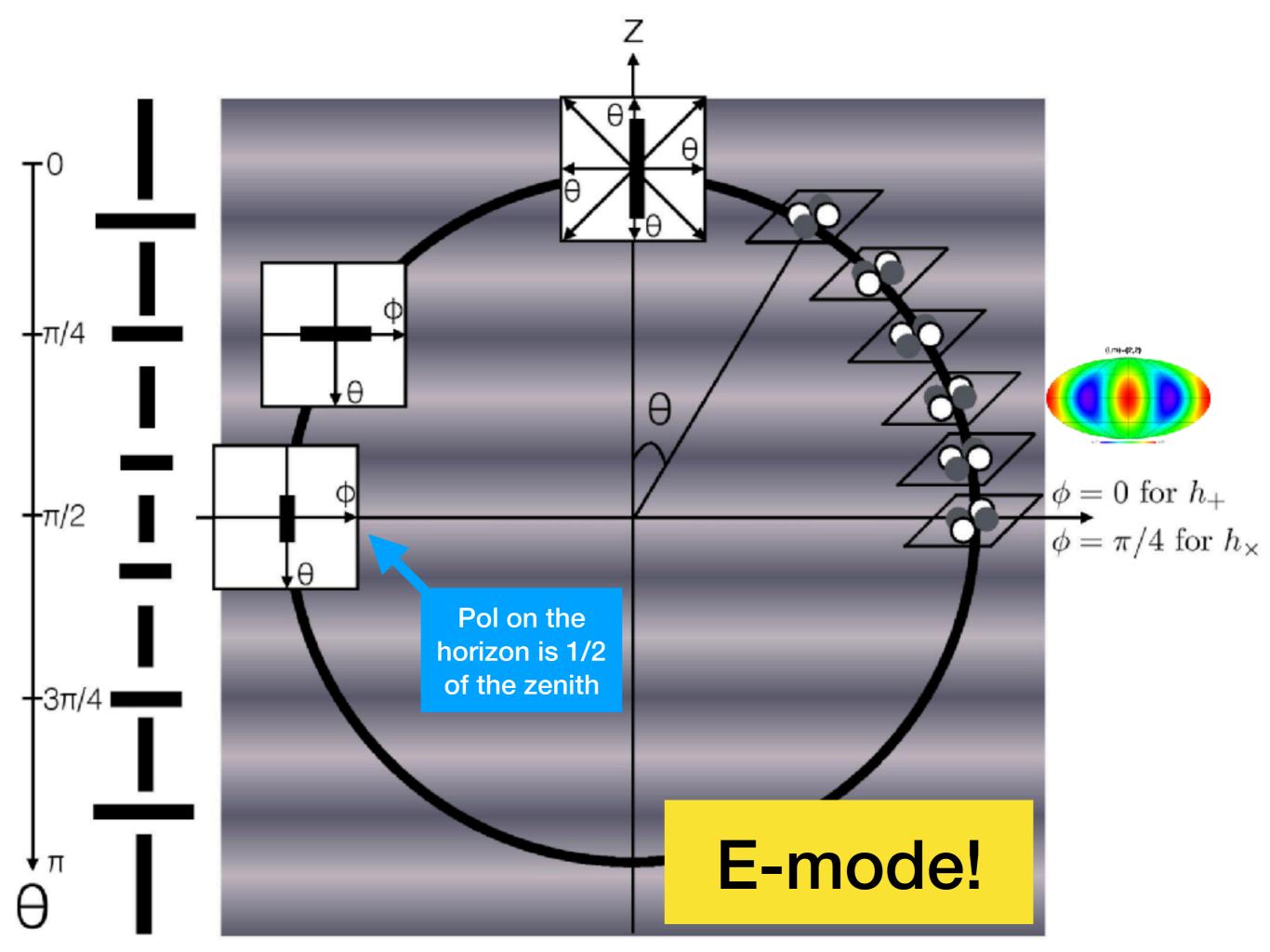
(l,m)=(2,2)

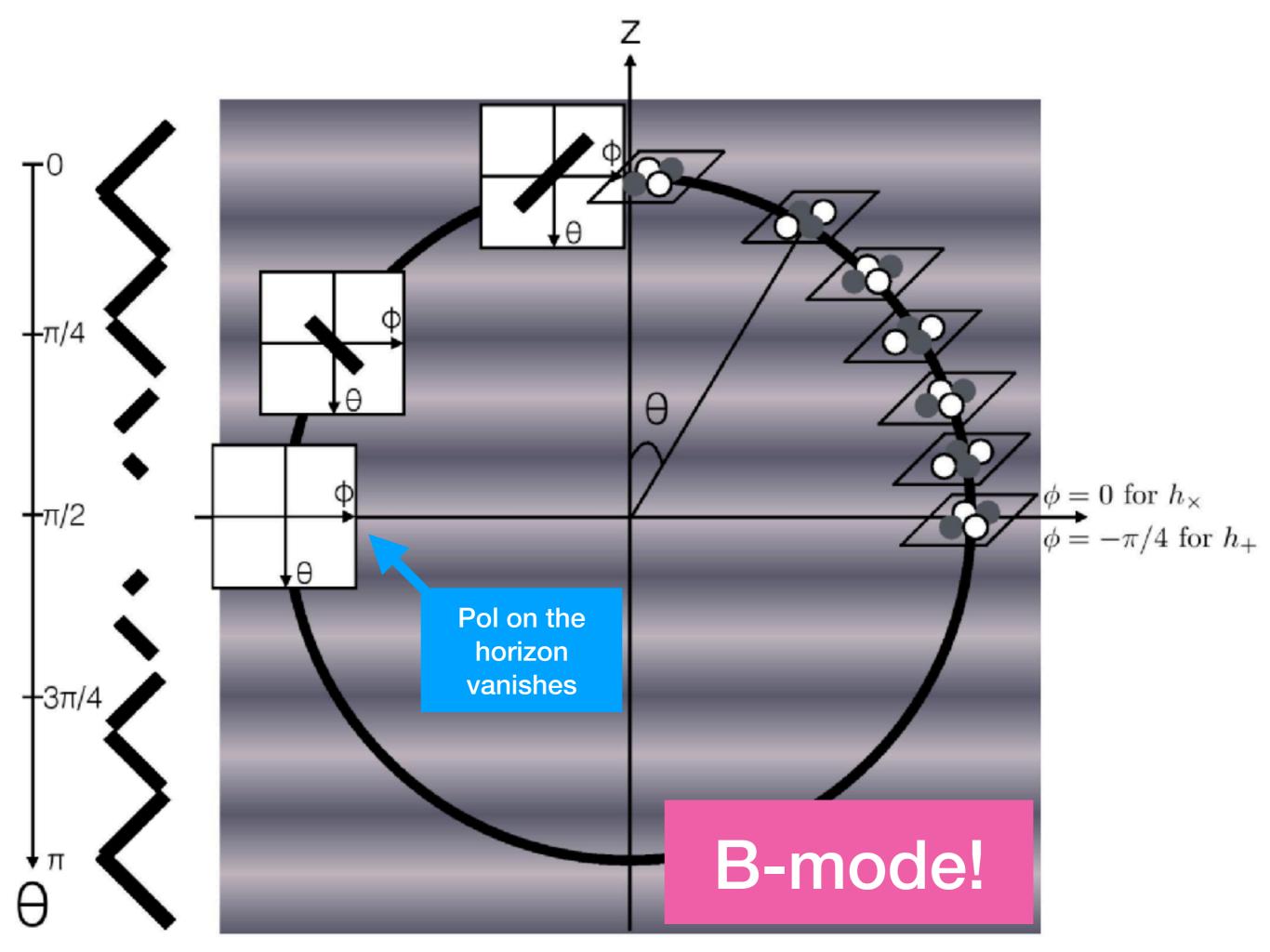


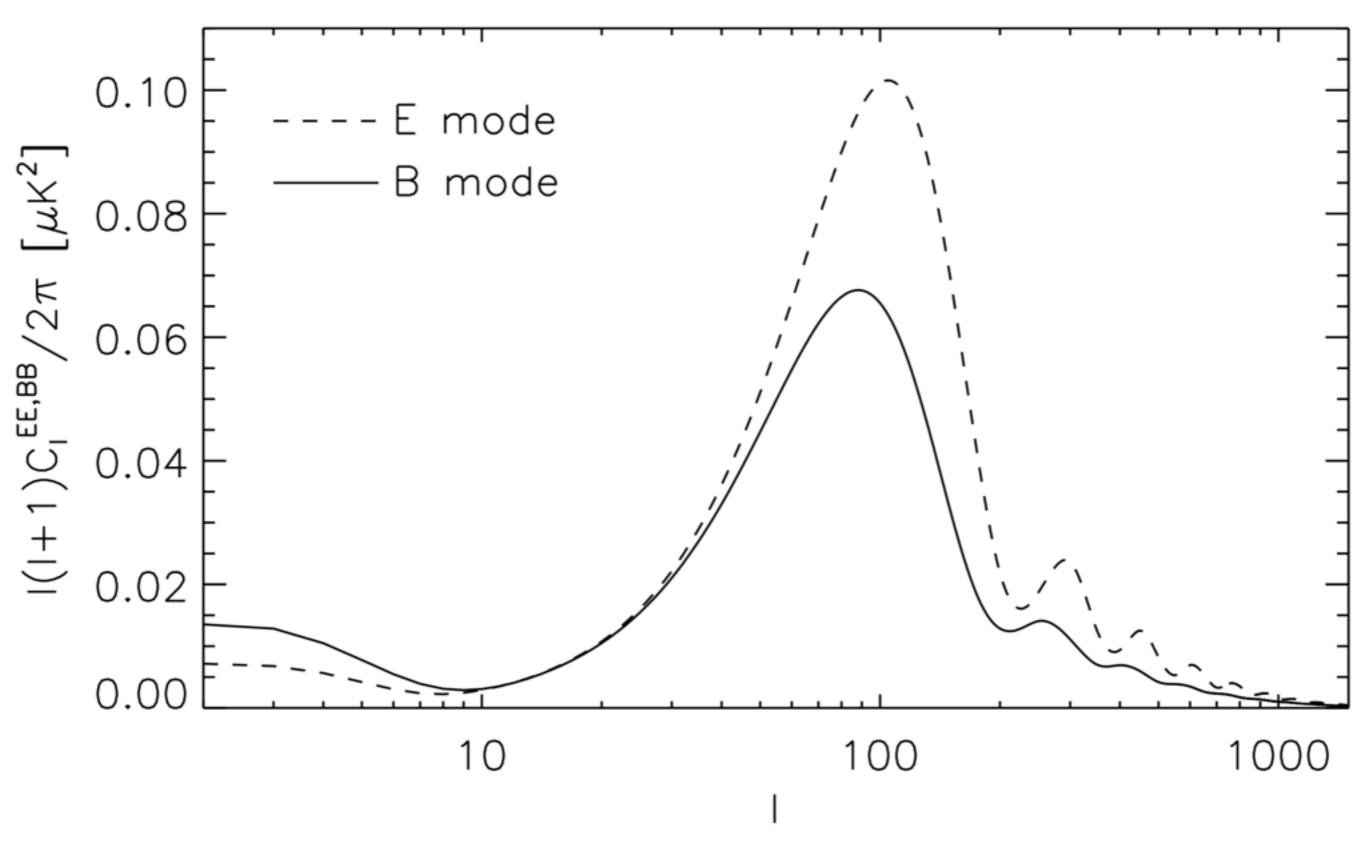
Local quadrupole temperature anisotropy seen from an electron











 E and B modes are produced nearly equally, but on small scales B is smaller than E because B vanishes on the horizon

