



Gregory Horndeski, 'Horndeski Scalar Theory, Past, Present and Future'

# Towards Void-Lensing as a Cosmological Observable

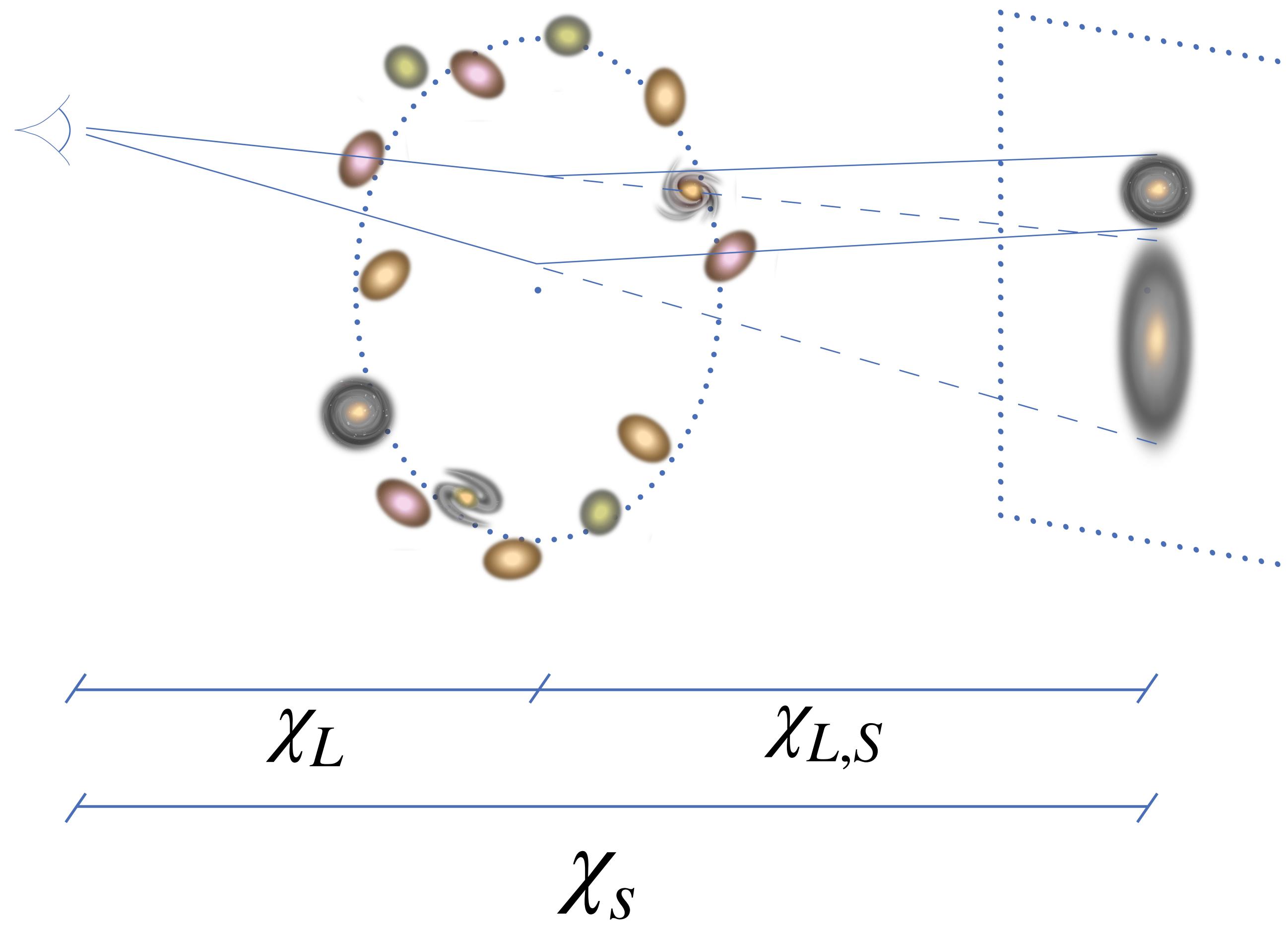
- I. How To Optimize Void-Lensing Measurements
- II. How To Interpret the Measurement

Renan Isquierdo Boschetti (Supervisors: Stephanie Escoffier and Eric Jullo)



# WL Voids

Differential surface mass density:

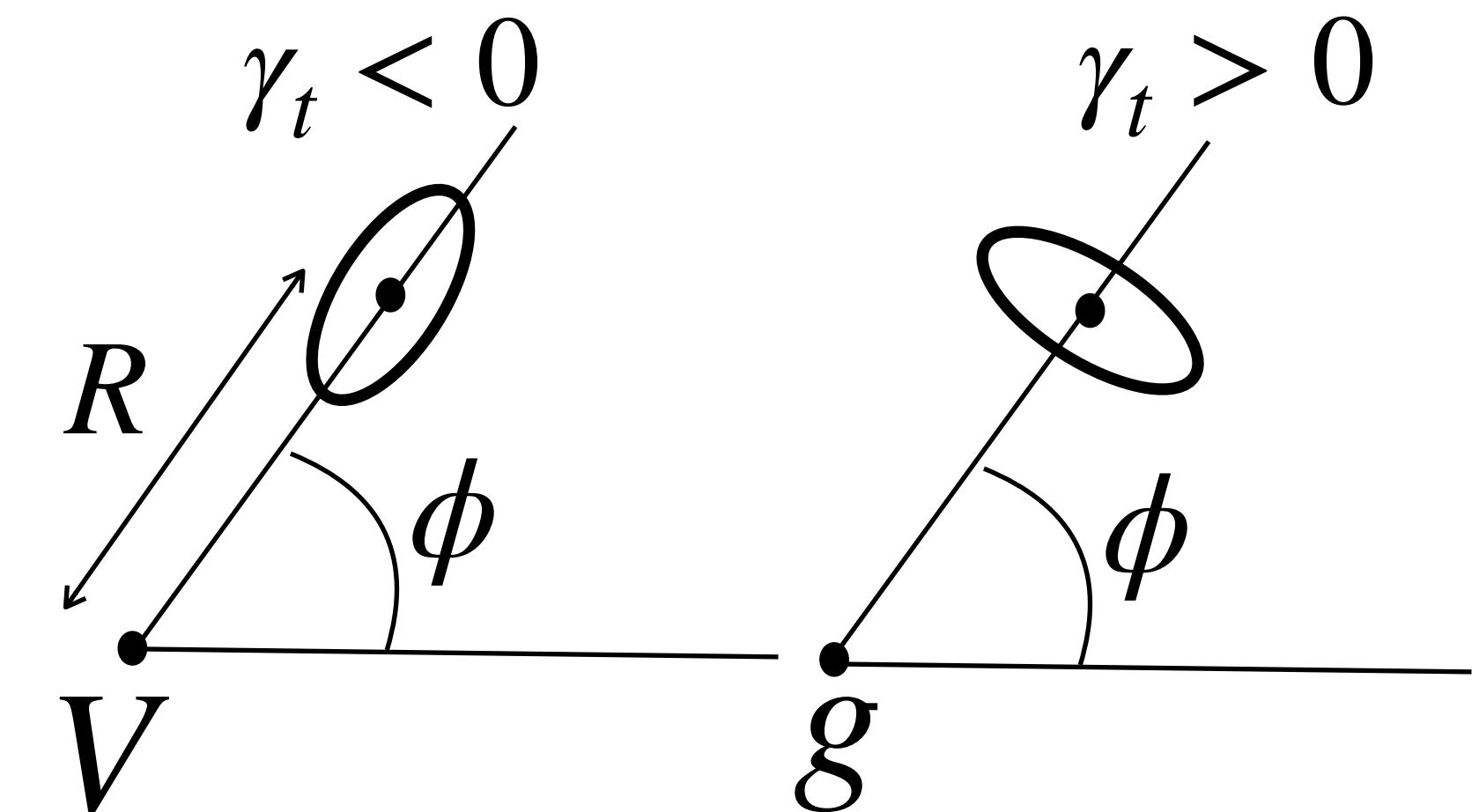


$$\Delta\Sigma(R, z_L) = \Sigma_{crit}(\bar{\kappa}( < R) - \kappa(R))$$

$$= \Sigma_{crit} \times \gamma_t(R)$$

$$\kappa(R) = \int d\chi \Sigma_{crit}^{-1} \bar{\rho} \delta(\chi, R) \simeq \Sigma_{crit}^{-1} \Sigma(R) \text{ (TL)}$$

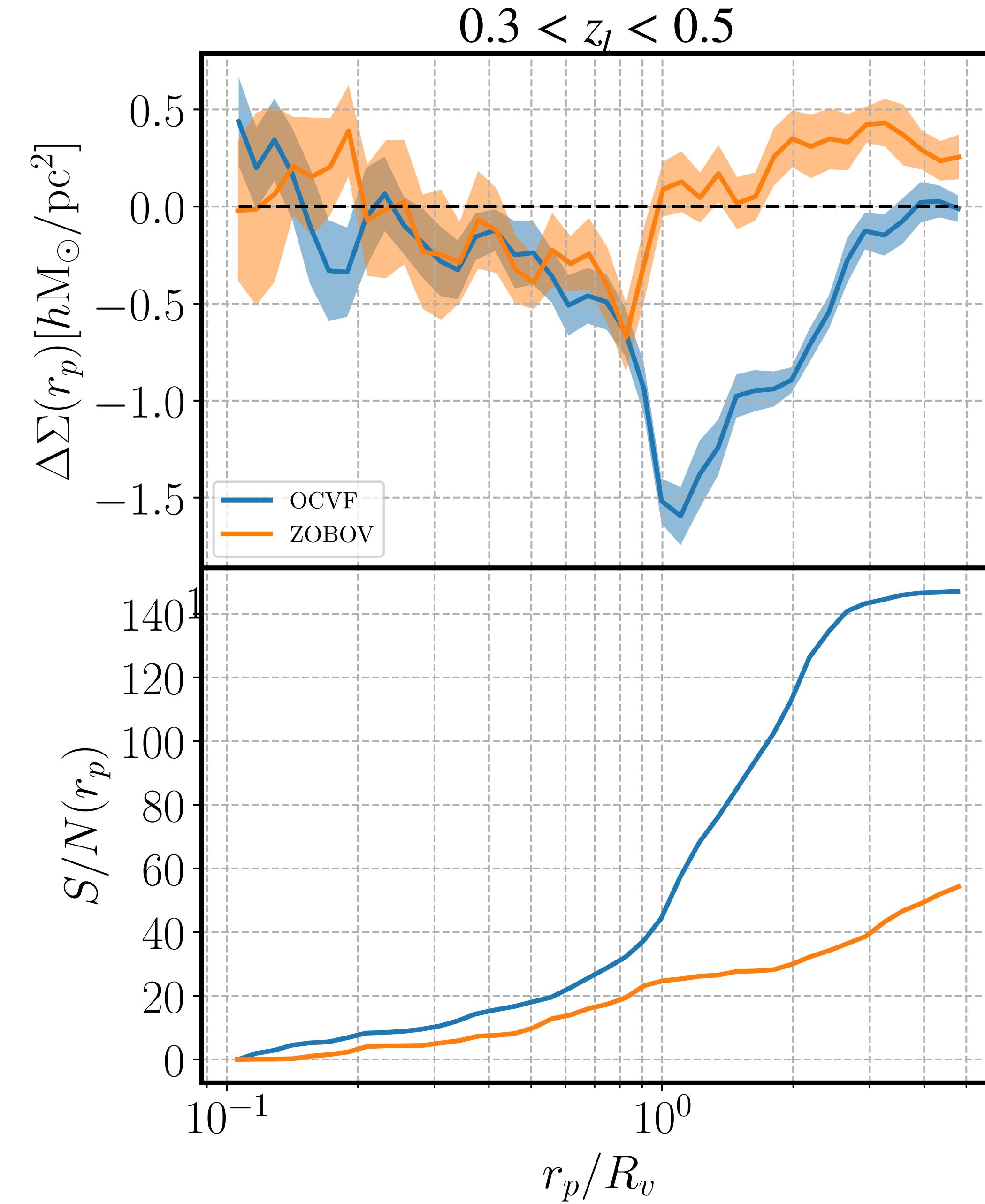
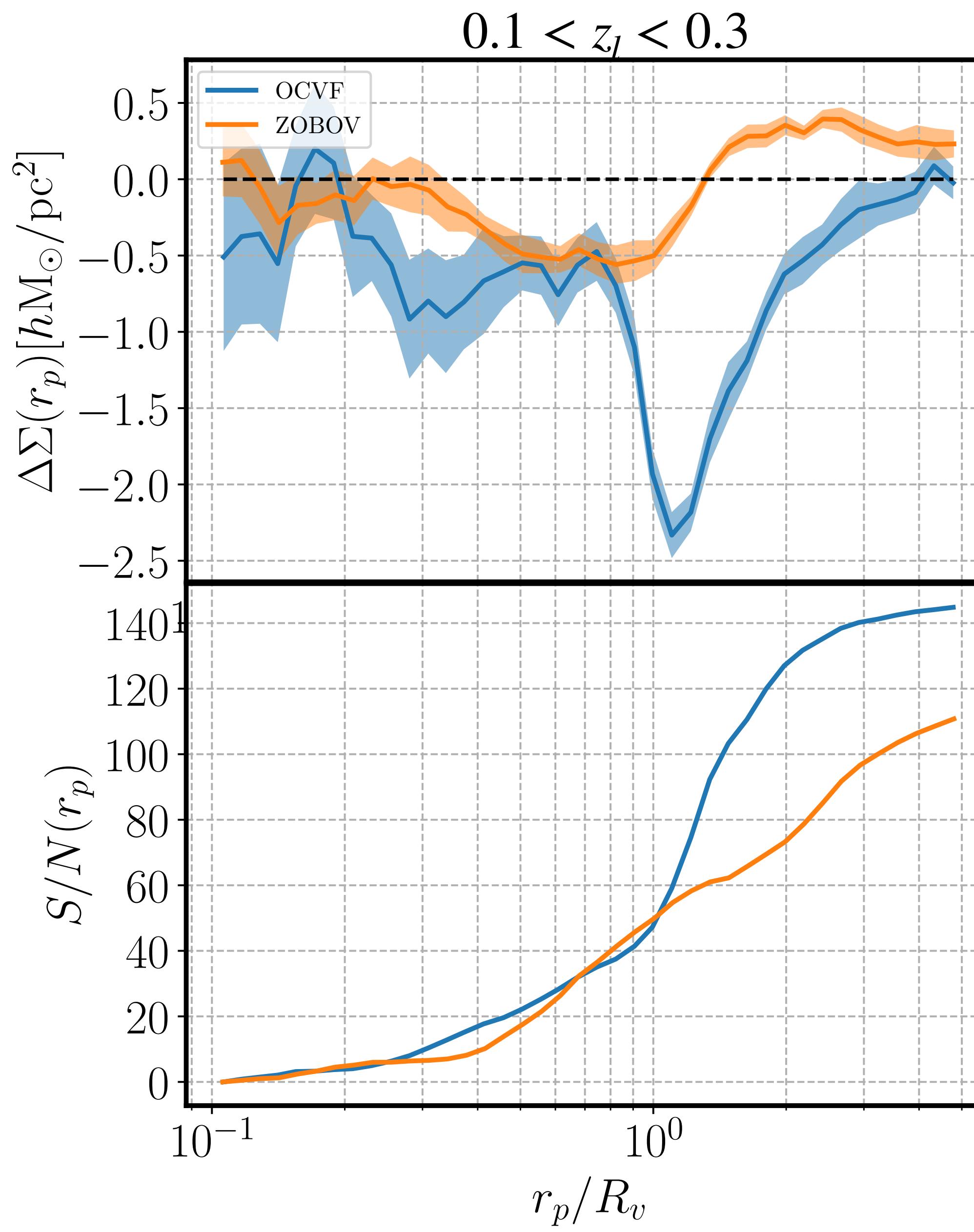
$$\Rightarrow \Delta\Sigma(R) = \bar{\Sigma}( < R) - \Sigma(R)$$



# Performance on VL

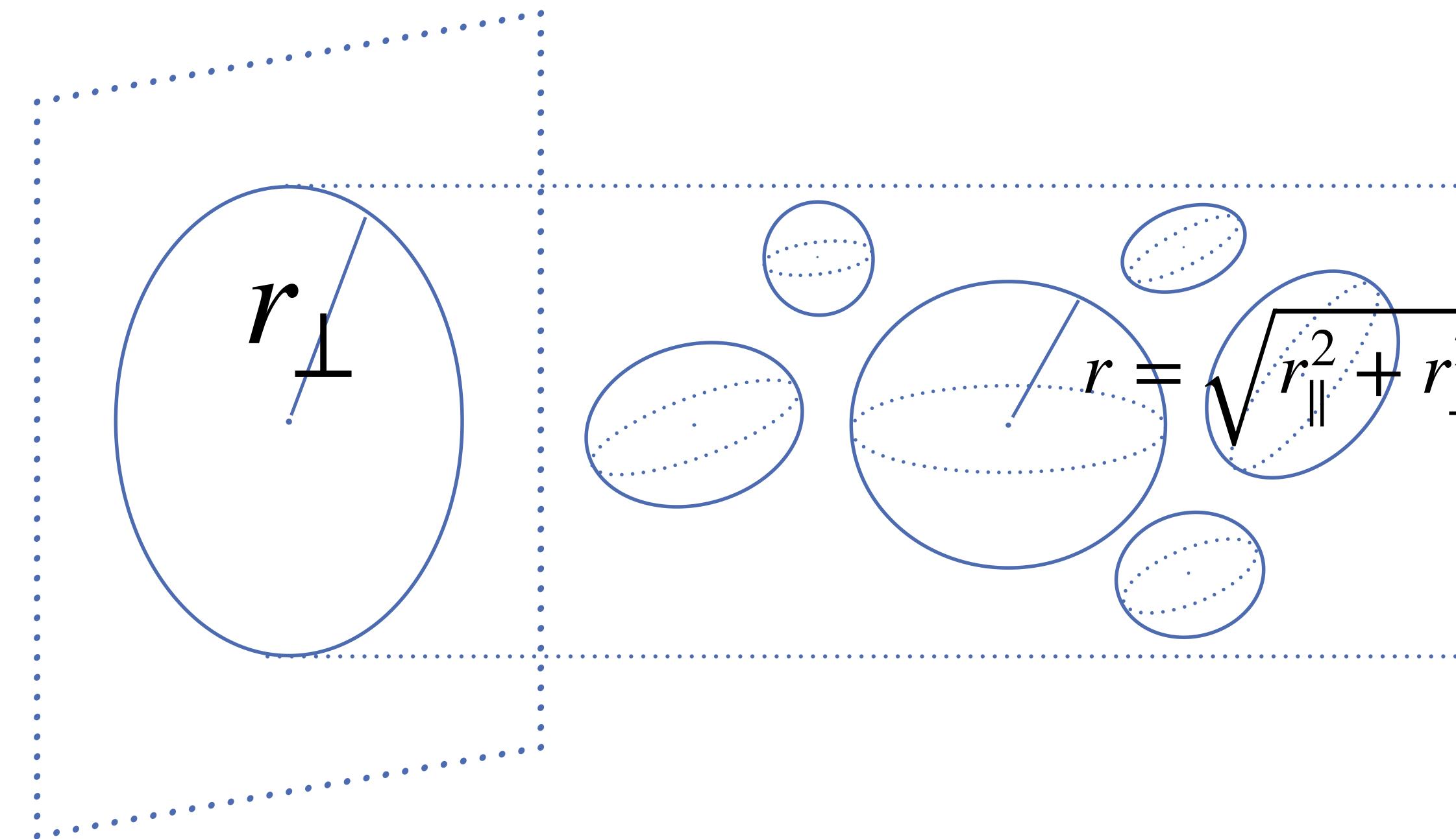
$10 < R_v < 15 [h^{-1} \text{Mpc}]$

$10^4 \text{degrees}^2$



# The Void-Lensing Model

Projected field



$$\begin{aligned}\Sigma(r_{\perp} | R_{2D}) &= \int d \ln R_{3D} \frac{dn_{\nu}}{d \ln R_{3D}} \int dx_{\perp} (1 + \xi(x_{\perp})) \int dr_{\parallel} \delta_{3D}(r_{\perp}, r_{\parallel} | \alpha, R_{3D}) \\ &= \int dr_{\parallel} \delta^{eff}(r_{\perp}, r_{\parallel} | \alpha, R_{3D}) \\ \Rightarrow \Delta\Sigma(r_{\perp}) &= \bar{\Sigma}(< r_{\perp}) - \Sigma(r_{\perp})\end{aligned}$$

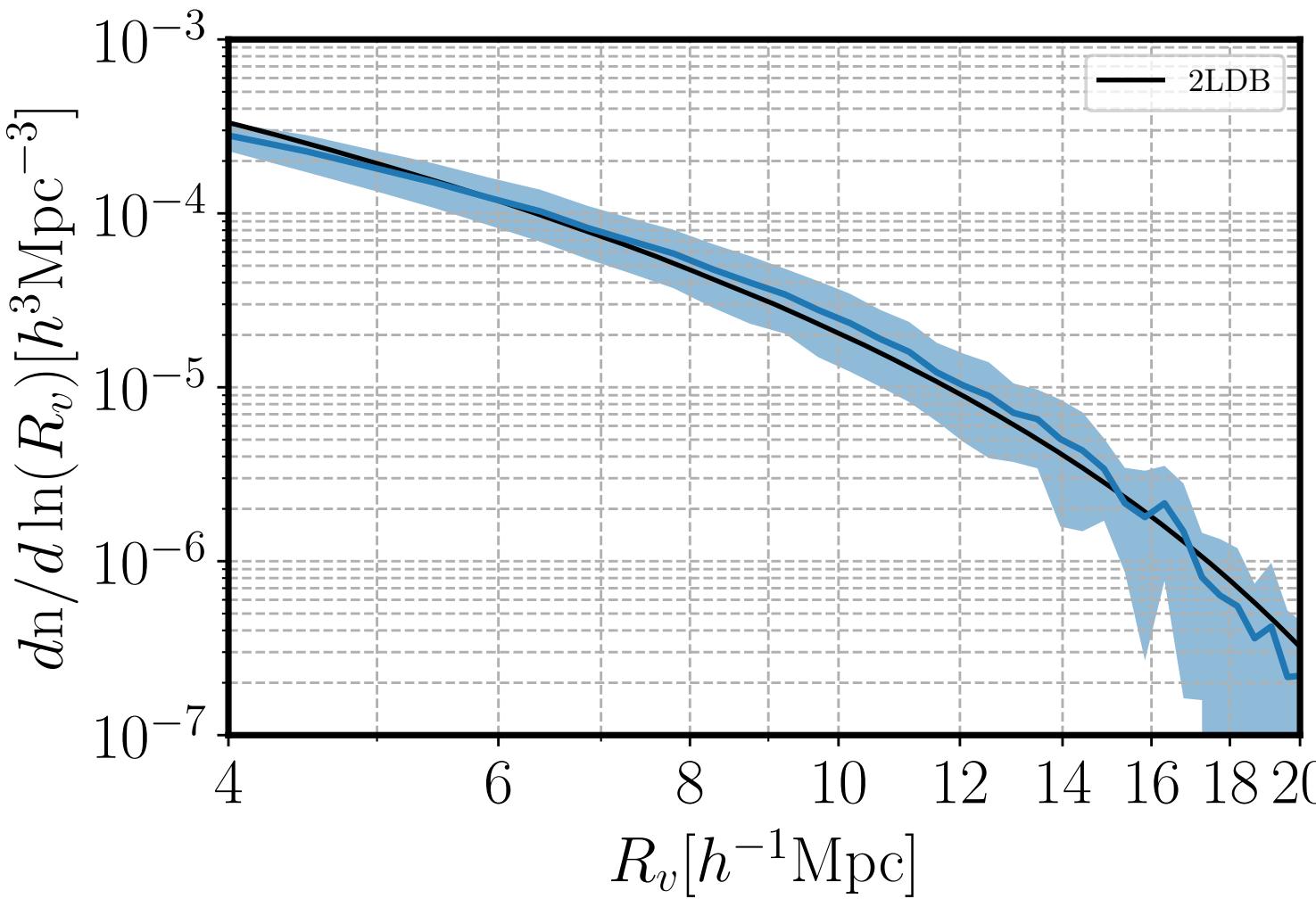
# The Void-Lensing Model

$$\Sigma(r_{\perp} | R_{2D}, \Delta_{2D}) = \int dR_{3D} \frac{dn_v}{dR_{3D}}(R_{3D} | \Delta_{3D}) \int dx_{\perp} dx_{\parallel} d\alpha P(x_{\perp}, x_{\parallel}, \alpha | R_{3D}, R_{2D}, \Delta_{3D}, \Delta_{2D}) \int dr_{\parallel} \delta_{3D}(r_{\perp} - x_{\perp}, r_{\parallel} - x_{\parallel} | \alpha, R_{3D}, \Delta_{3D})$$

$\approx$

$$\Sigma(r_{\perp} | M_{2D}) = \int d \ln R_{3D} \frac{\boxed{dn_v}}{d \ln R_{3D}} \int dx_{\perp} (1 + \xi(x_{\perp})) \int dr_{\parallel} \delta_{3D}(r_{\perp}, r_{\parallel} | \alpha, R_{3D})$$

$$\frac{dn_v}{d \ln R} = \frac{f(\sigma)}{V(R)} \frac{d \ln \sigma^{-1}}{d \ln R} \quad , \text{ where } \quad \sigma^2(R) \equiv \int \frac{dk}{2\pi^2} k^2 P_{mm}^L(k) |\tilde{W}(k | R)|^2$$



# The Void-Lensing Model

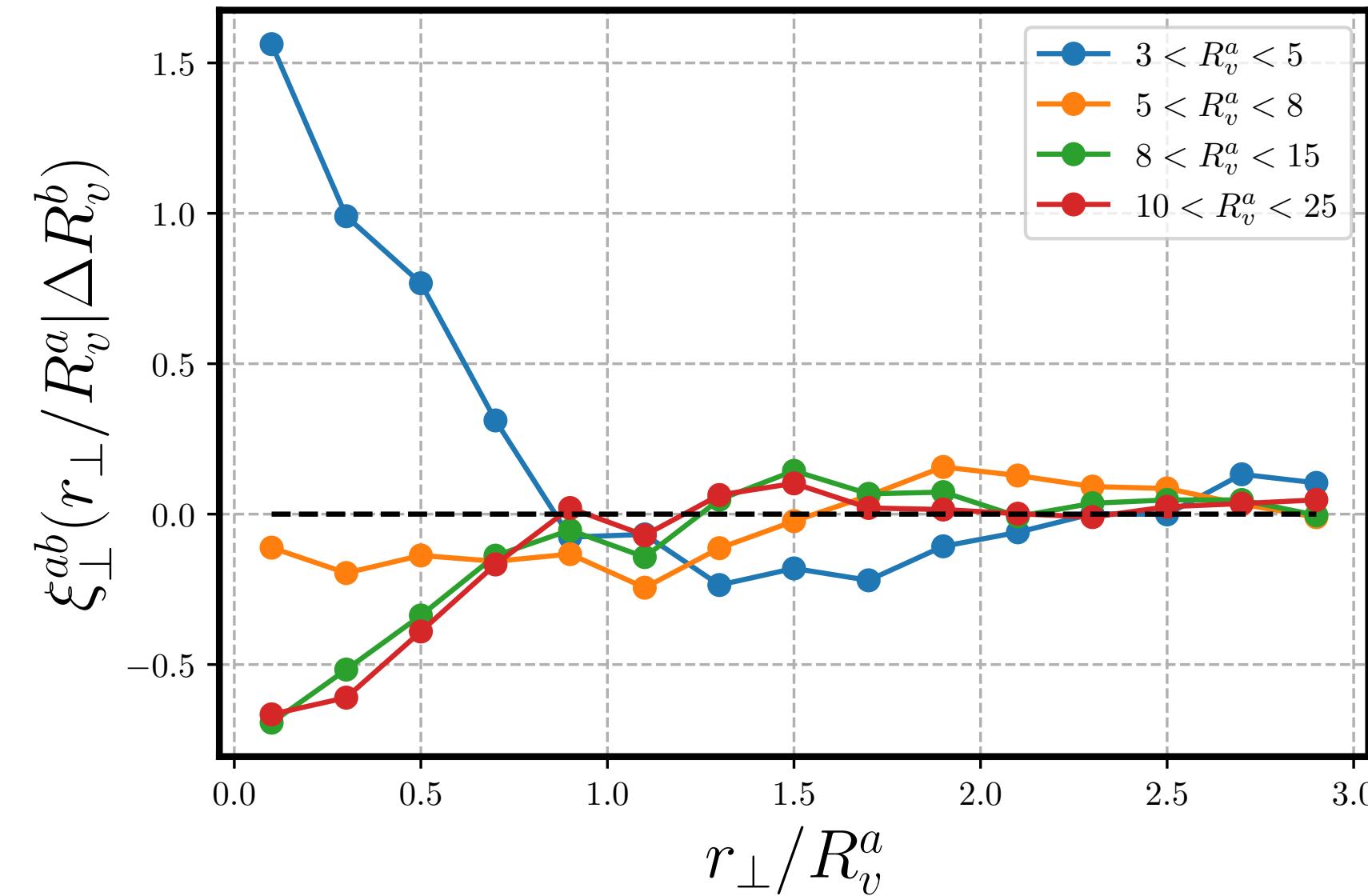
$$\Sigma(r_{\perp} | R_{2D}, \Delta_{2D}) = \int dR_{3D} \frac{dn_v}{dR_{3D}}(R_{3D} | \Delta_{3D}) \int dx_{\perp} dx_{\parallel} d\alpha P(x_{\perp}, x_{\parallel}, \alpha | R_{3D}, R_{2D}, \Delta_{3D}, \Delta_{2D}) \int dr_{\parallel} \rho_{3D}(r_{\perp} - x_{\perp}, r_{\parallel} - x_{\parallel} | \alpha, R_{3D}, \Delta_{3D})$$

$$\Sigma(r_{\perp} | R_{2D}) = \int d \ln R_{3D} \frac{dn_v}{d \ln R_{3D}} \int dx_{\perp} (1 + \xi(x_{\perp})) \int dr_{\parallel} \delta_{3D}(r_{\perp}, r_{\parallel} | \alpha, R_{3D})$$

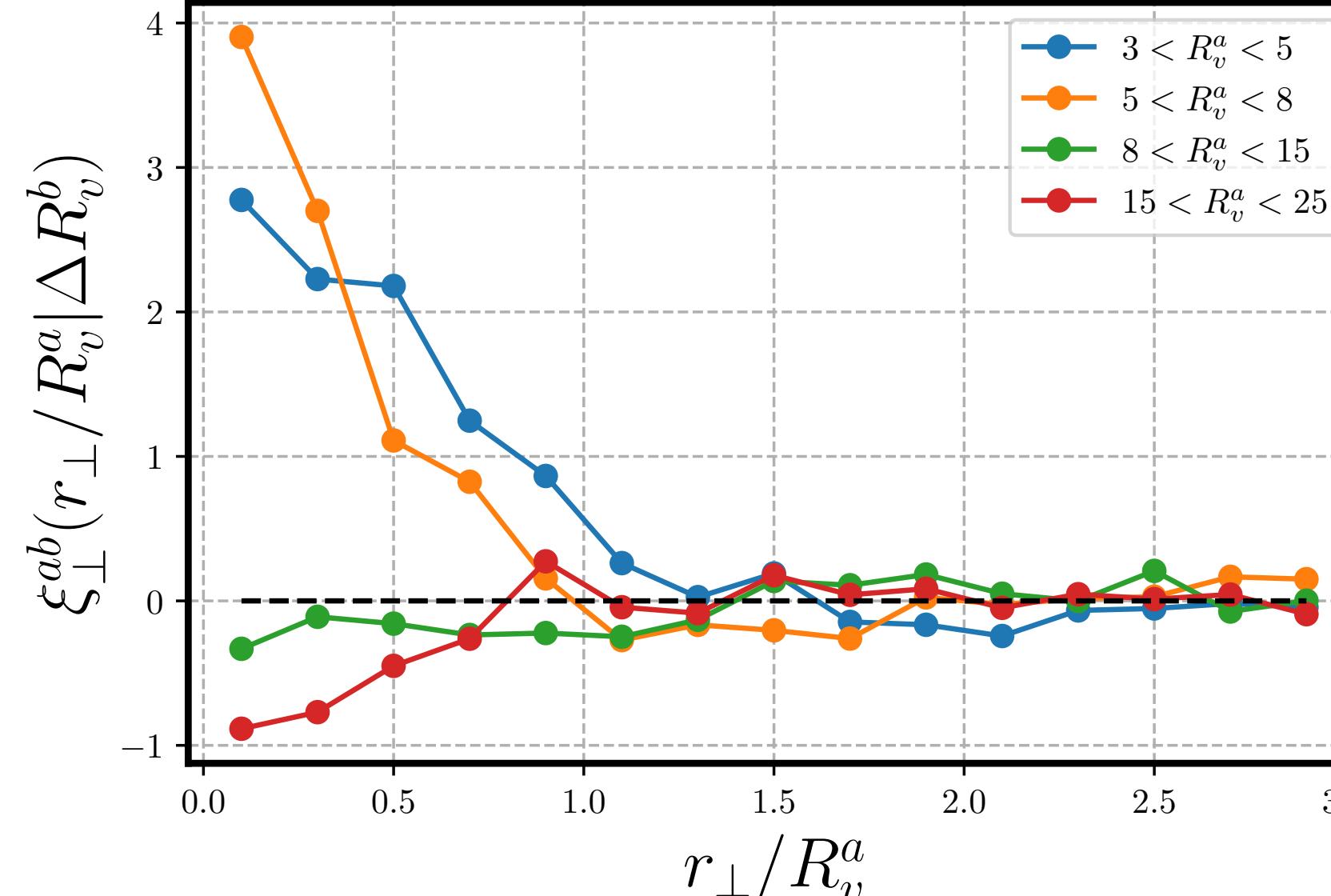
$\approx$

$$\boxed{\int dx_{\perp} (1 + \xi(x_{\perp})) \int dr_{\parallel} \delta_{3D}(r_{\perp}, r_{\parallel} | \alpha, R_{3D})}$$

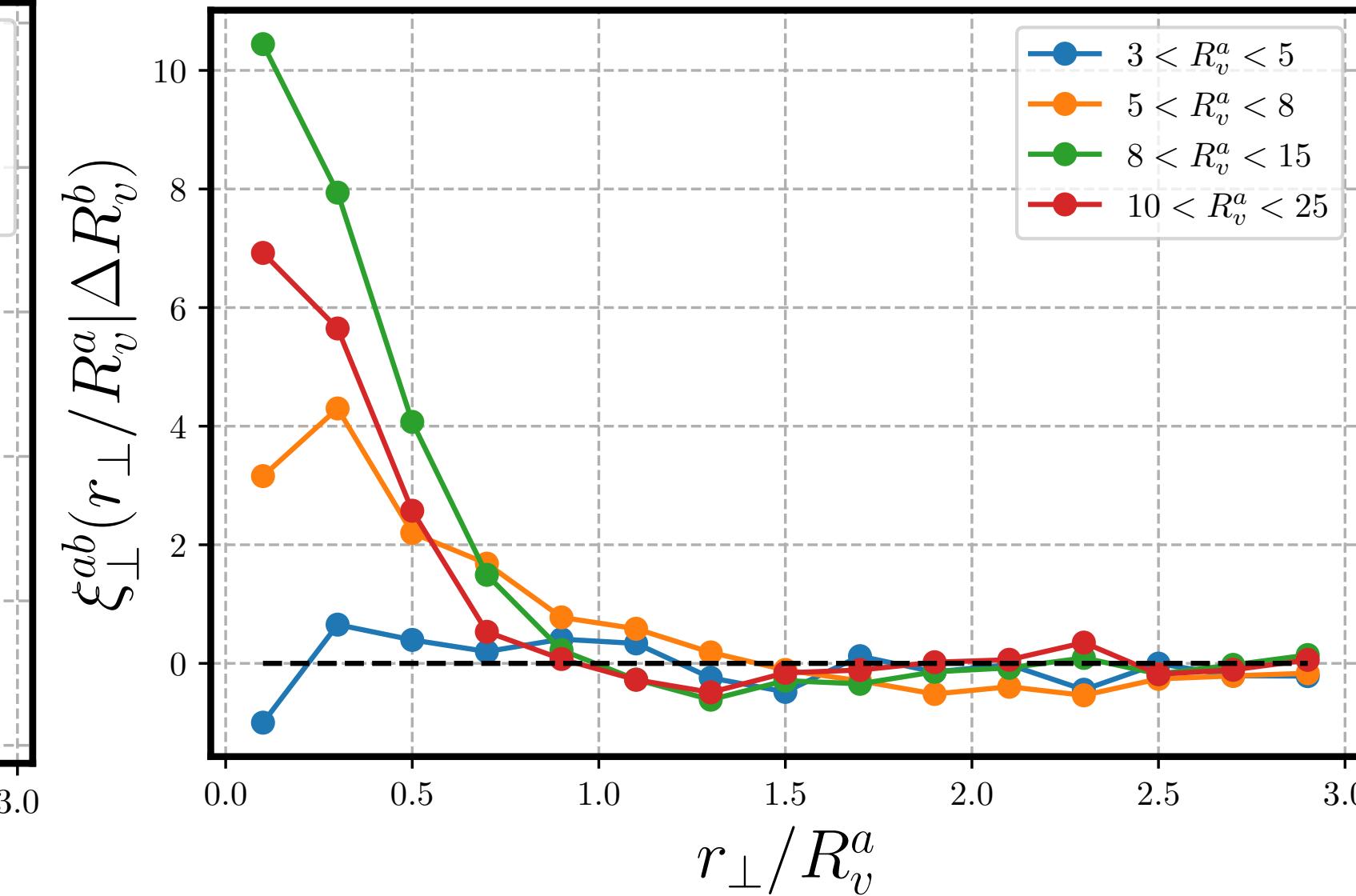
$3 < R_v^b < 5 [h^{-1}\text{Mpc}]$



$5 < R_v^b < 8 [h^{-1}\text{Mpc}]$



$8 < R_v^b < 15 [h^{-1}\text{Mpc}]$

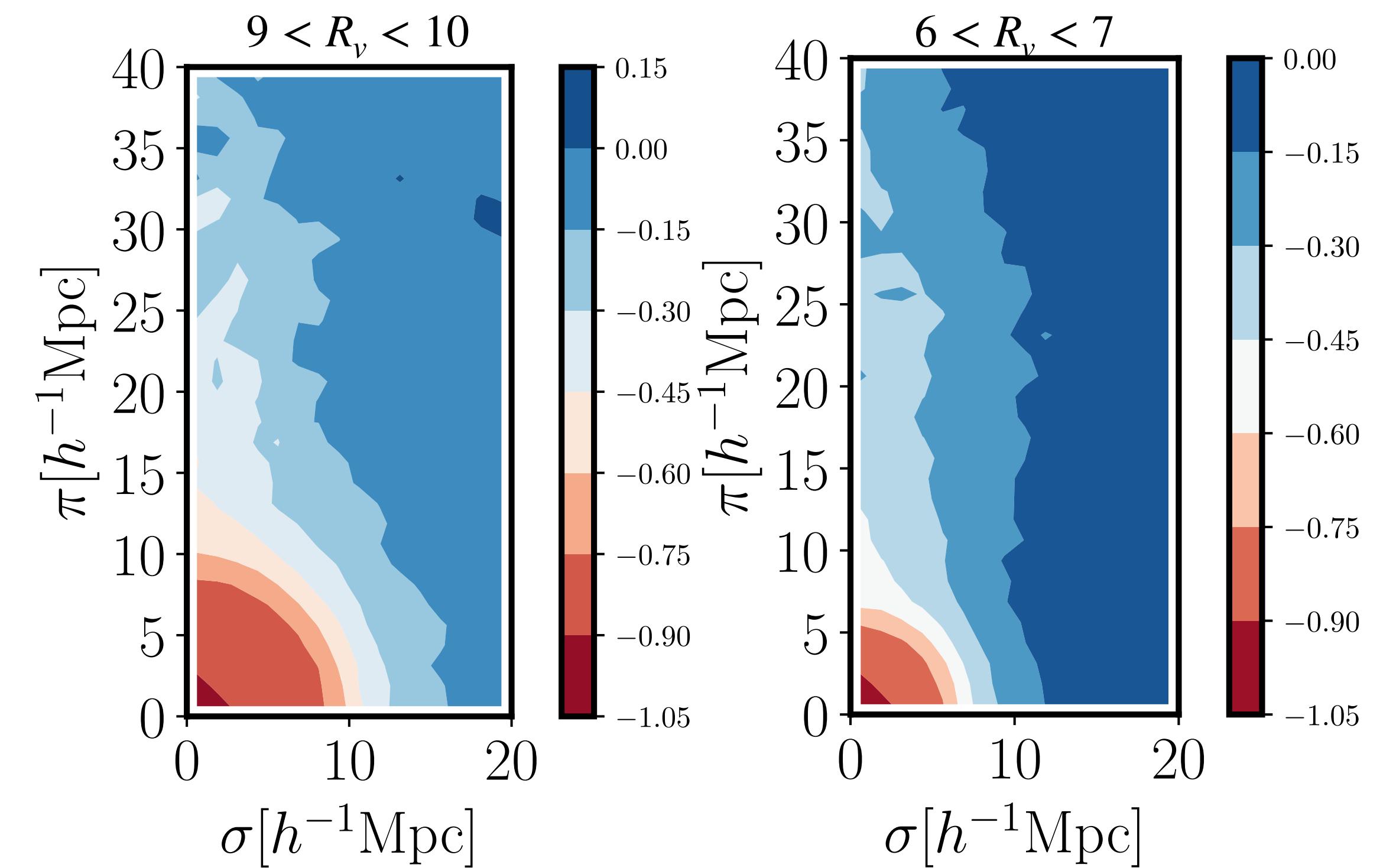
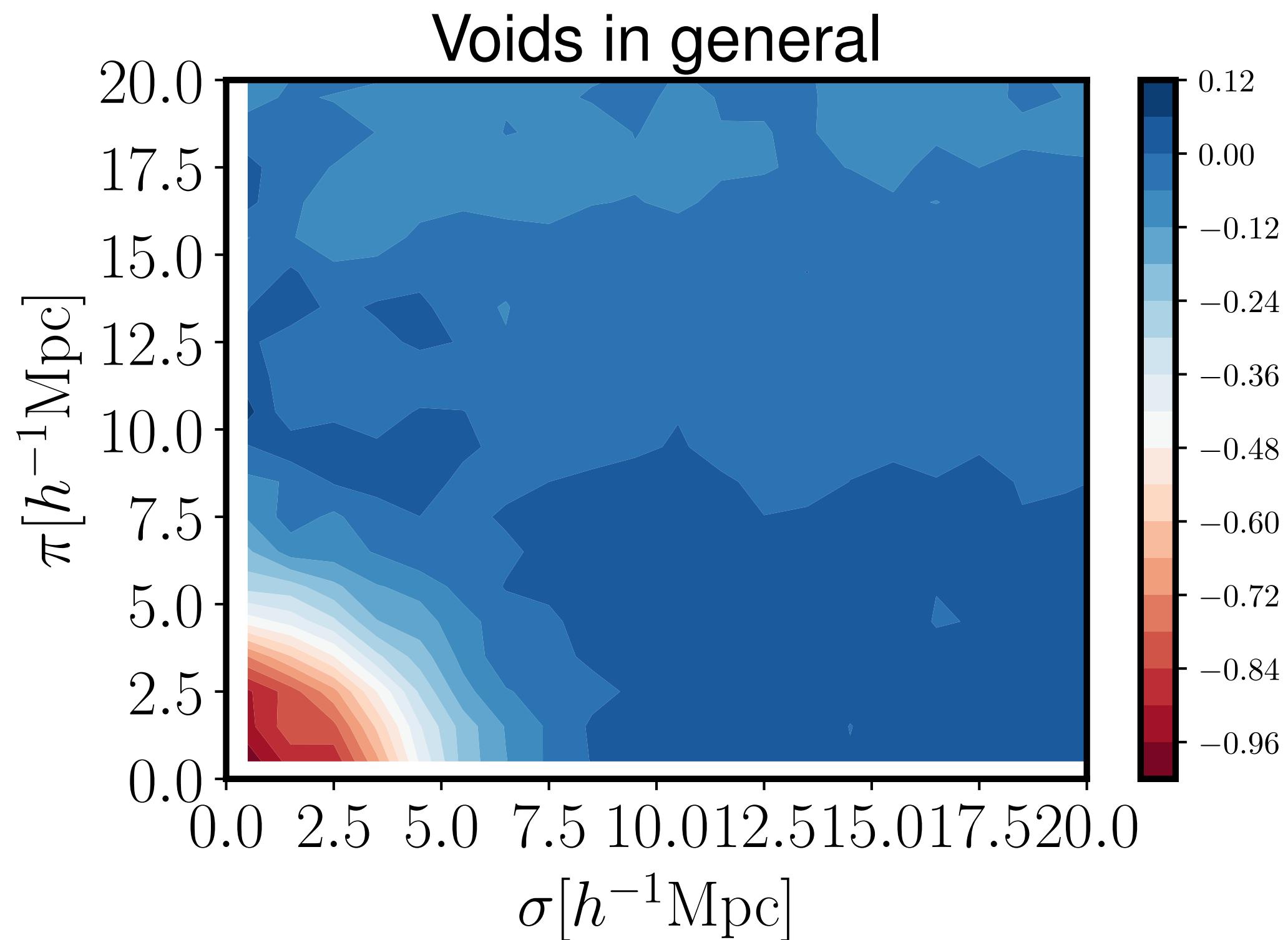


# The Void-Lensing Model

$$\Sigma(r_{\perp} | R_{2D}, \Delta_{2D}) = \int dR_{3D} \frac{dn_v}{dR_{3D}}(R_{3D} | \Delta_{3D}) \int dx_{\perp} dx_{\parallel} d\alpha P(x_{\perp}, x_{\parallel}, \alpha | R_{3D}, R_{2D}, \Delta_{3D}, \Delta_{2D}) \int dr_{\parallel} \delta_{3D}(r_{\perp} - x_{\perp}, r_{\parallel} - x_{\parallel} | \alpha, R_{3D}, \Delta_{3D})$$

$\approx$

$$\Sigma(r_{\perp} | M_{2D}) = \int d \ln R_{3D} \frac{dn_v}{d \ln R_{3D}} \int dx_{\perp} (1 + \xi(x_{\perp})) \int dr_{\parallel} \delta_{3D}(r_{\perp}, r_{\parallel} | \alpha, R_{3D})$$

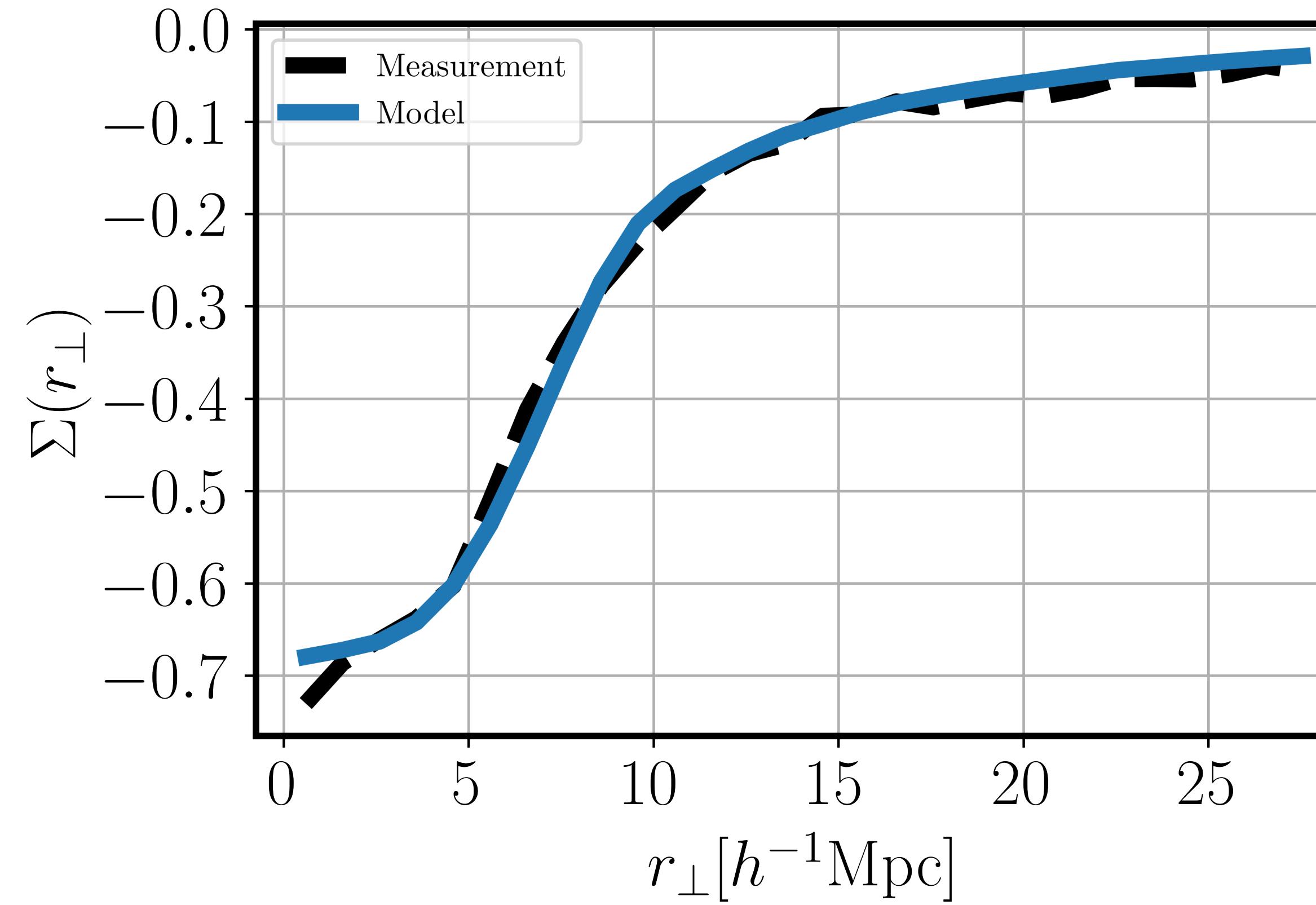


# Preliminary Result

$$\Sigma(r_{\perp} | R_{2D}, \Delta_{2D}) = \int dR_{3D} \frac{dn_{\nu}}{dR_{3D}}(R_{3D} | \Delta_{3D}) \int dx_{\perp} dx_{\parallel} d\alpha P(x_{\perp}, x_{\parallel}, \alpha | R_{3D}, R_{2D}, \Delta_{3D}, \Delta_{2D}) \int dr_{\parallel} \delta_{3D}(r_{\perp} - x_{\perp}, r_{\parallel} - x_{\parallel} | \alpha, R_{3D}, \Delta_{3D})$$

$\approx$

$$\Sigma(r_{\perp} | R_{2D}) = \int d \ln R_{3D} \frac{dn_{\nu}}{d \ln R_{3D}} \int dx_{\perp} (1 + \xi(x_{\perp})) \int dr_{\parallel} \delta_{3D}(r_{\perp}, r_{\parallel} | \alpha, R_{3D})$$

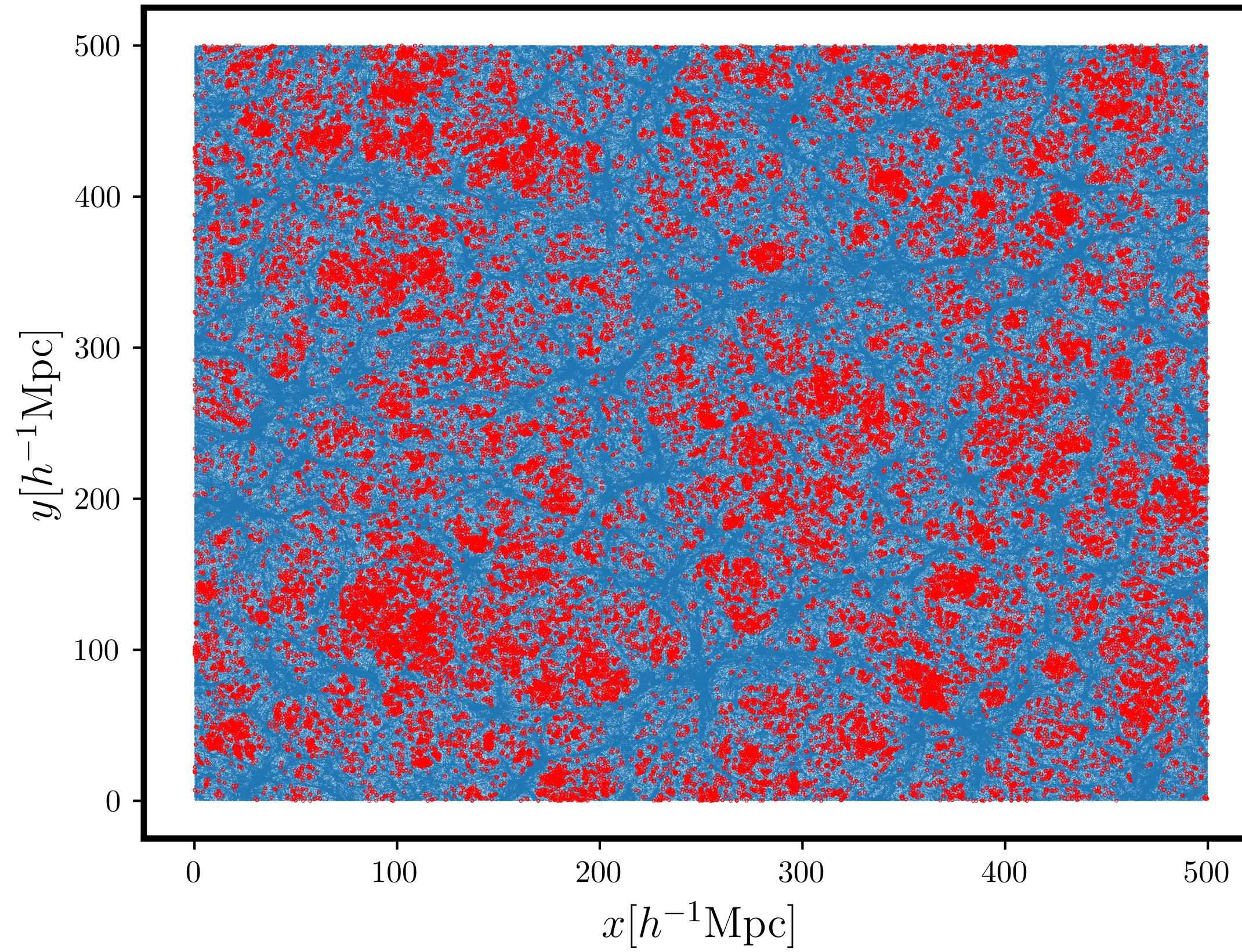


# Conclusions and Prospects

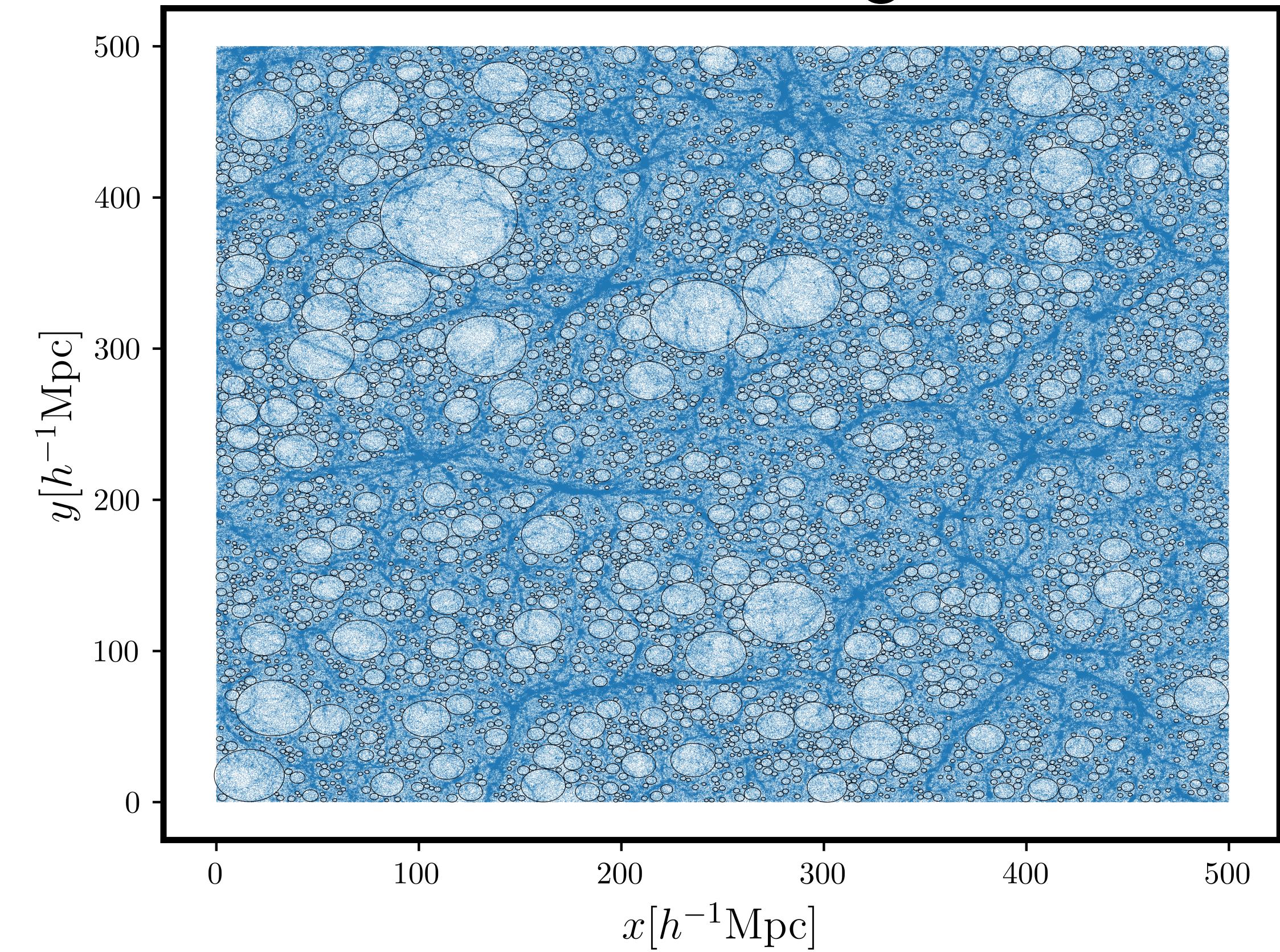
- Void-Lensing can be measured with a significant S/N
- Interesting phenomenology
- Is the Void intrinsic alignment sensitive to cosmology, modifications to gravity or neutrinos?
- What is exactly the cosmological information in Void-Lensing?

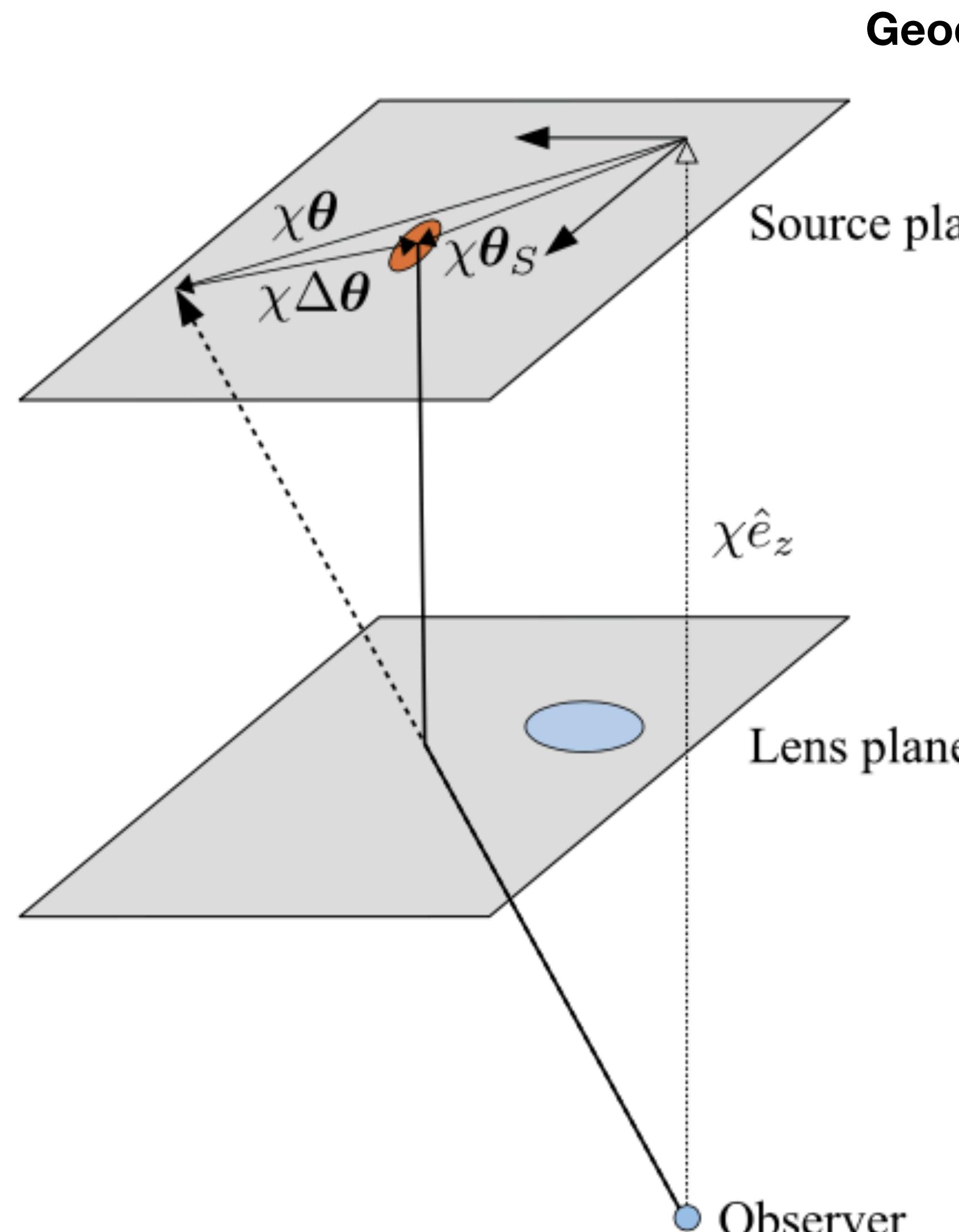
# Optimum Centering Void Finder

## Candidates



## Final Catalogue





**Geodesic equation + scalar perturbations**  $\Rightarrow$

$$\theta^i = \theta_s^i + \Delta\theta^i$$

$$\Delta\theta^i(\theta) = \frac{2}{c^2} \int_0^\chi d\chi' \Phi_{,i} \left( x(\theta, \chi') \right) \chi' \left( 1 - \frac{\chi'}{\chi} \right)$$

$$\psi_{ij} \equiv \frac{\partial \Delta\theta^i}{\partial \theta^j} = \frac{\partial^2}{\partial \theta^i \partial \theta^j} \phi_L(\theta) = \frac{2}{c^2} \int_0^\chi d\chi' \Phi_{,ij} \left( x(\theta, \chi') \right) \chi' \left( 1 - \frac{\chi'}{\chi} \right)$$

$$A_{ij} \equiv \frac{\partial \theta_S^i}{\partial \theta^j} = \begin{pmatrix} 1 - \kappa - \gamma_1 & -\gamma_2 \\ -\gamma_2 & 1 - \kappa + \gamma_1 \end{pmatrix}$$

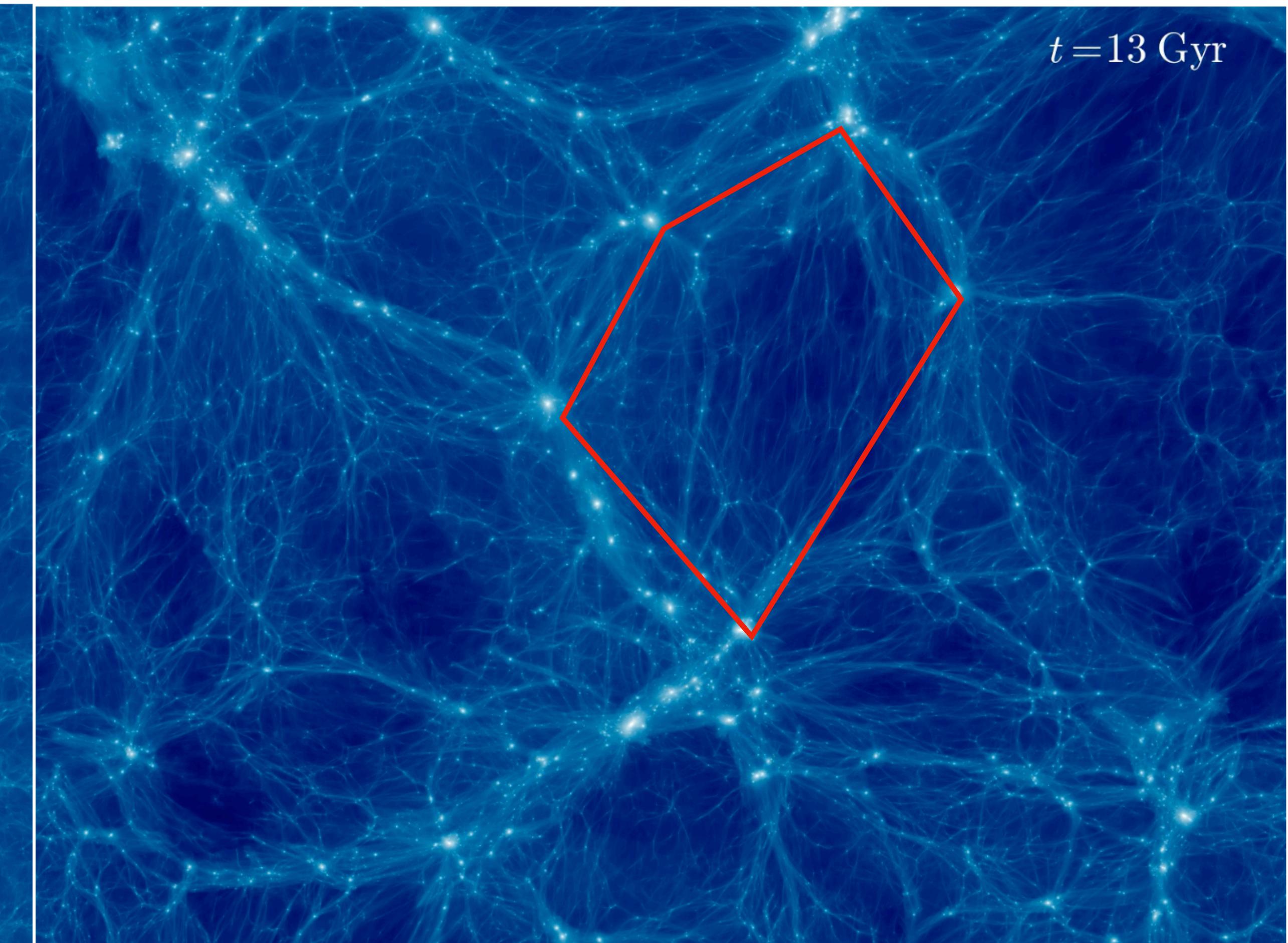
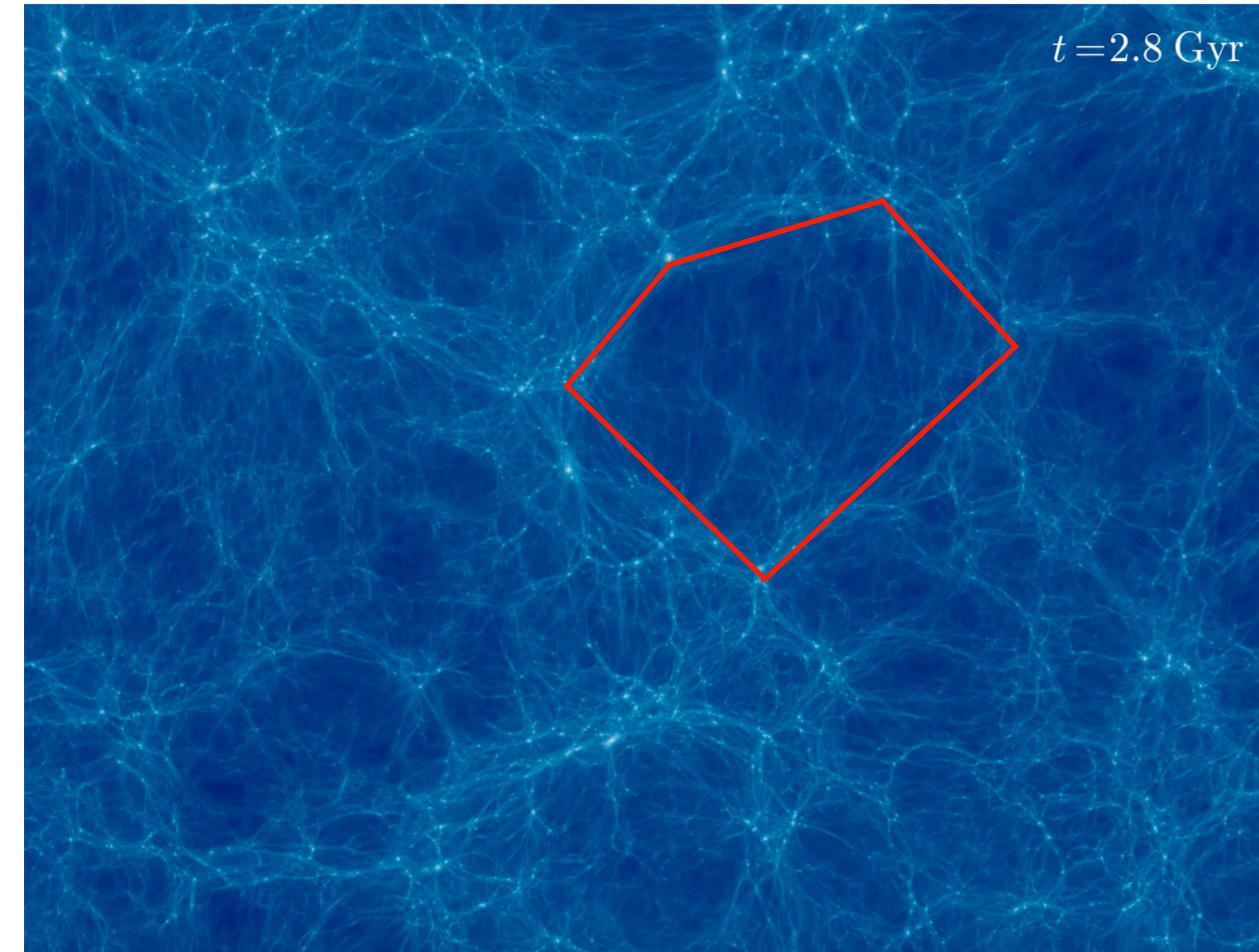
$$A_{ij} = \delta_{ij} + \psi_{ij}$$

$$\kappa = \psi_{11} + \psi_{22} = \frac{2}{c^2} \int_0^\chi d\chi' \nabla^2 \Phi \left( x(\theta, \chi') \right) \chi' \left( 1 - \frac{\chi'}{\chi} \right)$$

$$\gamma_1 = -\frac{\psi_{11} - \psi_{22}}{2}$$

$$\gamma_2 = -\psi_{12}$$

Intuition



# Motivation

- The new field act as an extra source of stress-energy (fifth force)

$$\nabla^2 \Phi = 4\pi G (\rho_M + \rho_{\text{eff}})$$

- The Bardeen potentials are not equal in general:

$$ds^2 = -(1 + 2\Phi)dt^2 + a^2(t)(1 - 2\Psi)d\mathbf{x}^2$$

$$\Phi_{len} = (\Phi + \Psi)/2 \neq \Psi$$