

Need for global

estimates of

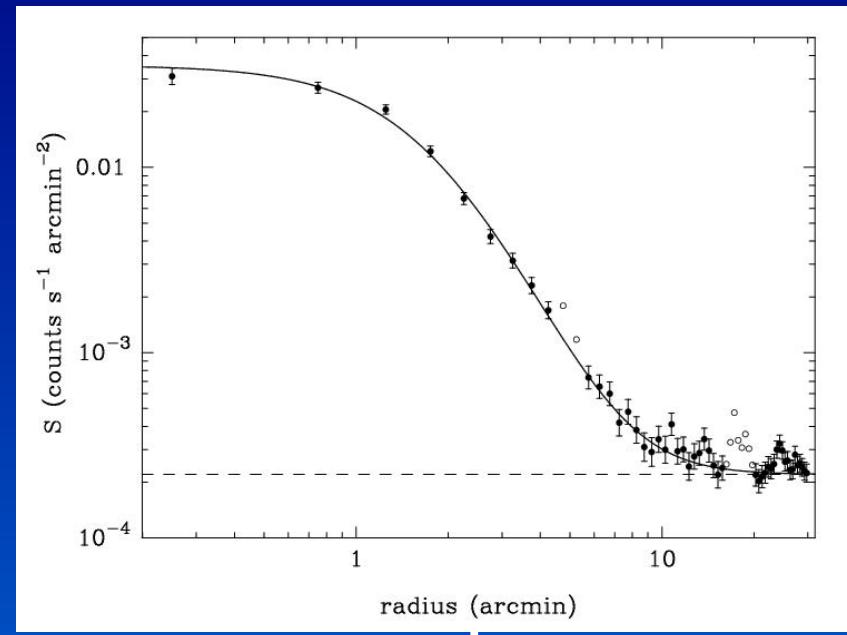
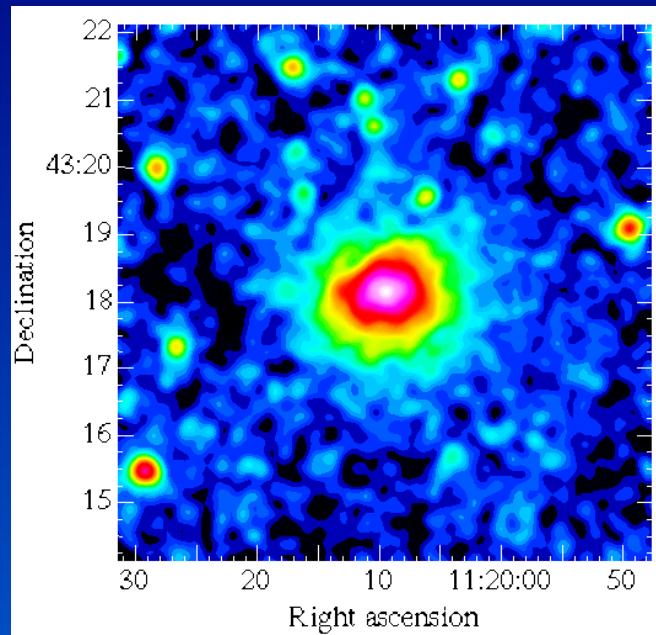
Ω_m !!!

$$\Omega_m$$

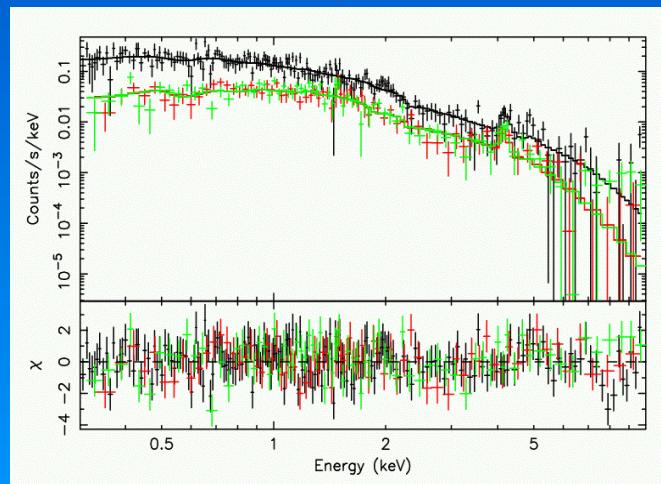
From X-ray Clusters

Baryon Fraction

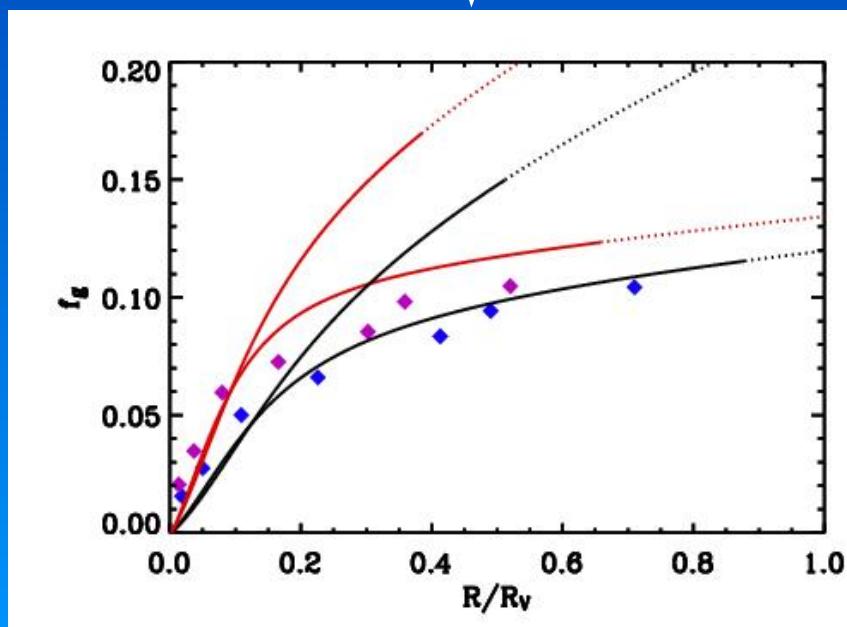
What do you do with a cluster?



X-ray spectrum



$M(r)$



Gas mass $M_g(r)$

Method :

Ratio :

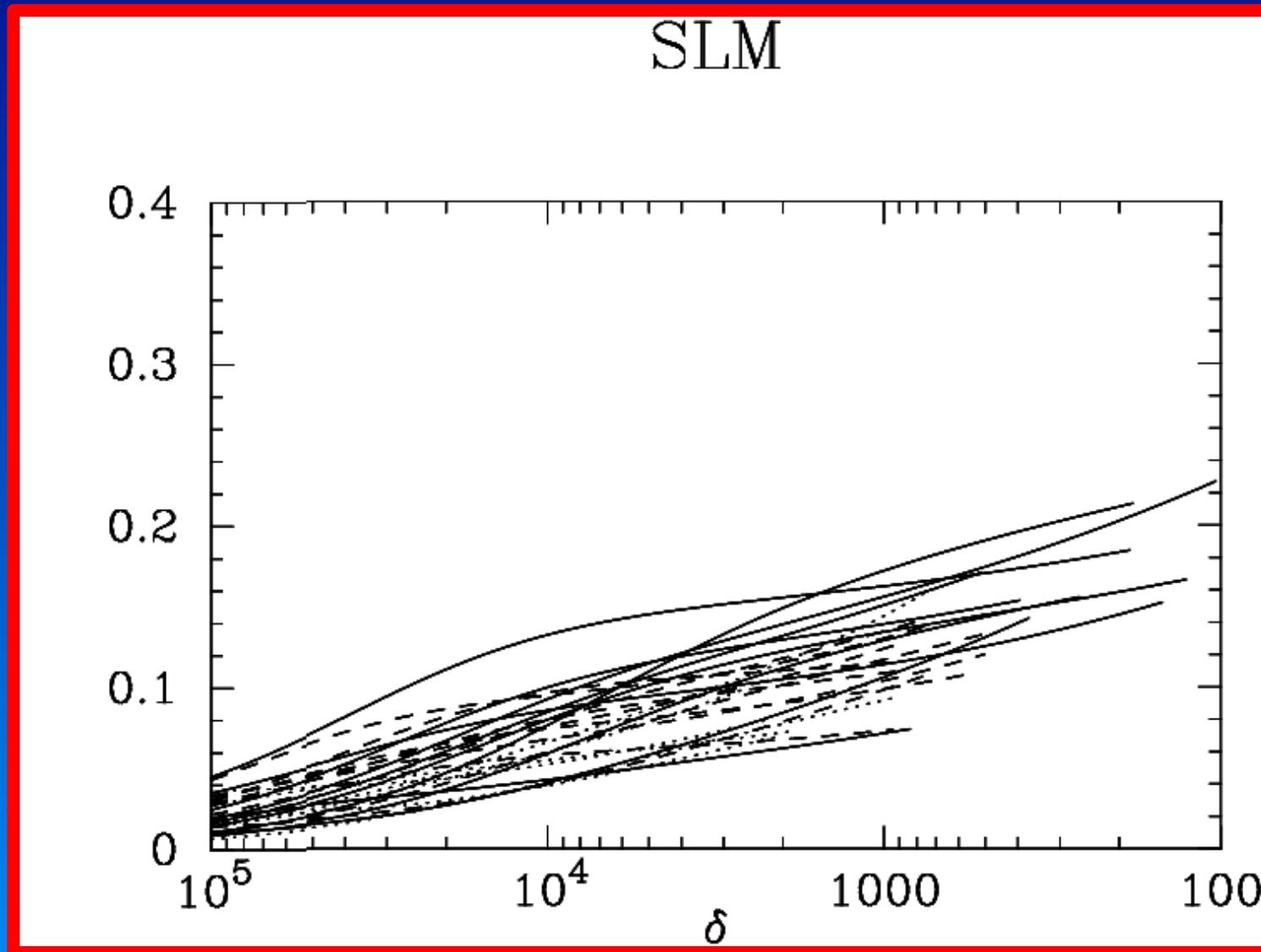
$$f_b = M_b / M_t$$

Observations $\Rightarrow M_g, T_x \square M_t$

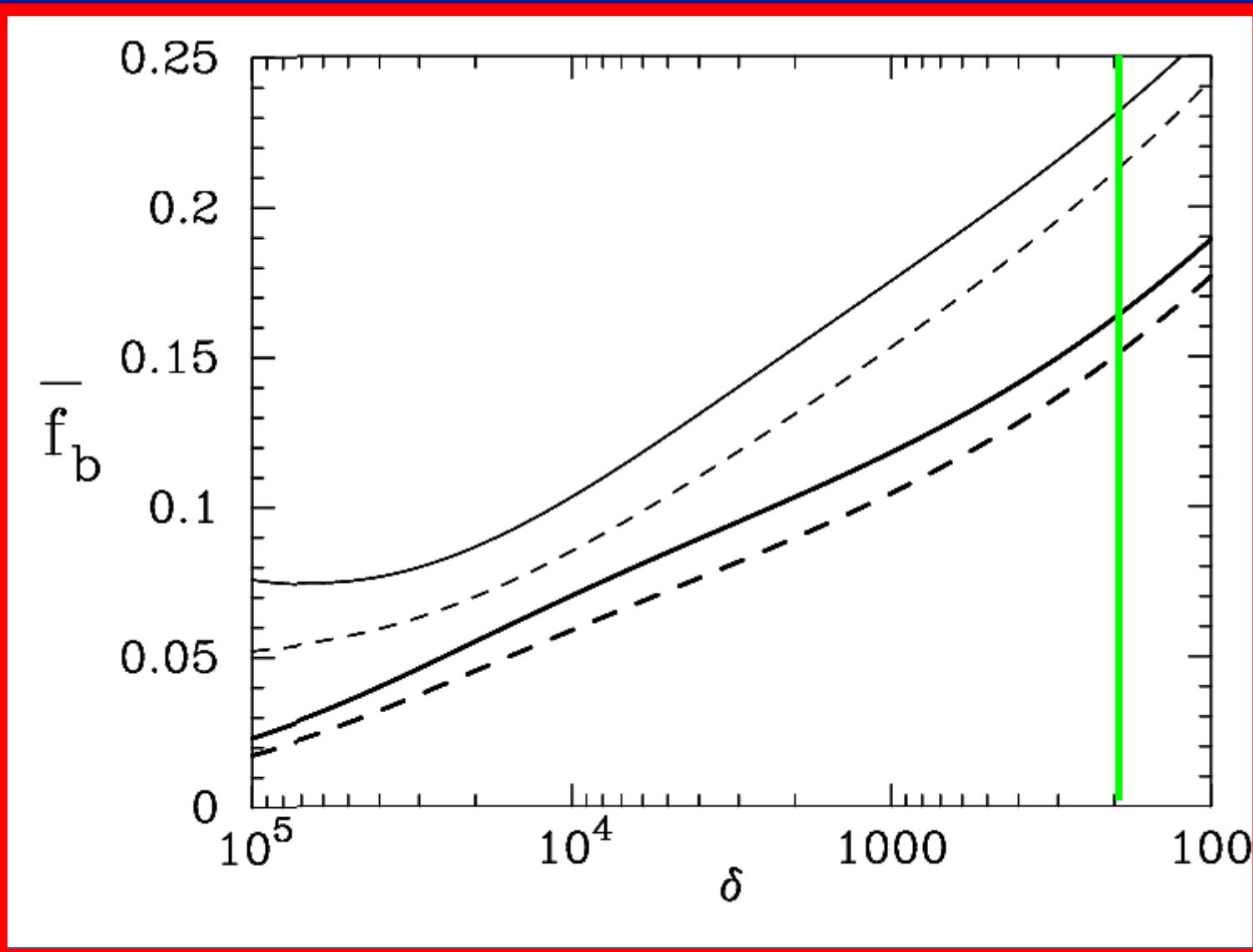
i.e. : $f_b \approx 15.-20. h_{50}^{-3/2} \%$

Cosmology : $f_b = \Omega_{bbn} / \Omega_0$

Scaling of baryon fractions :



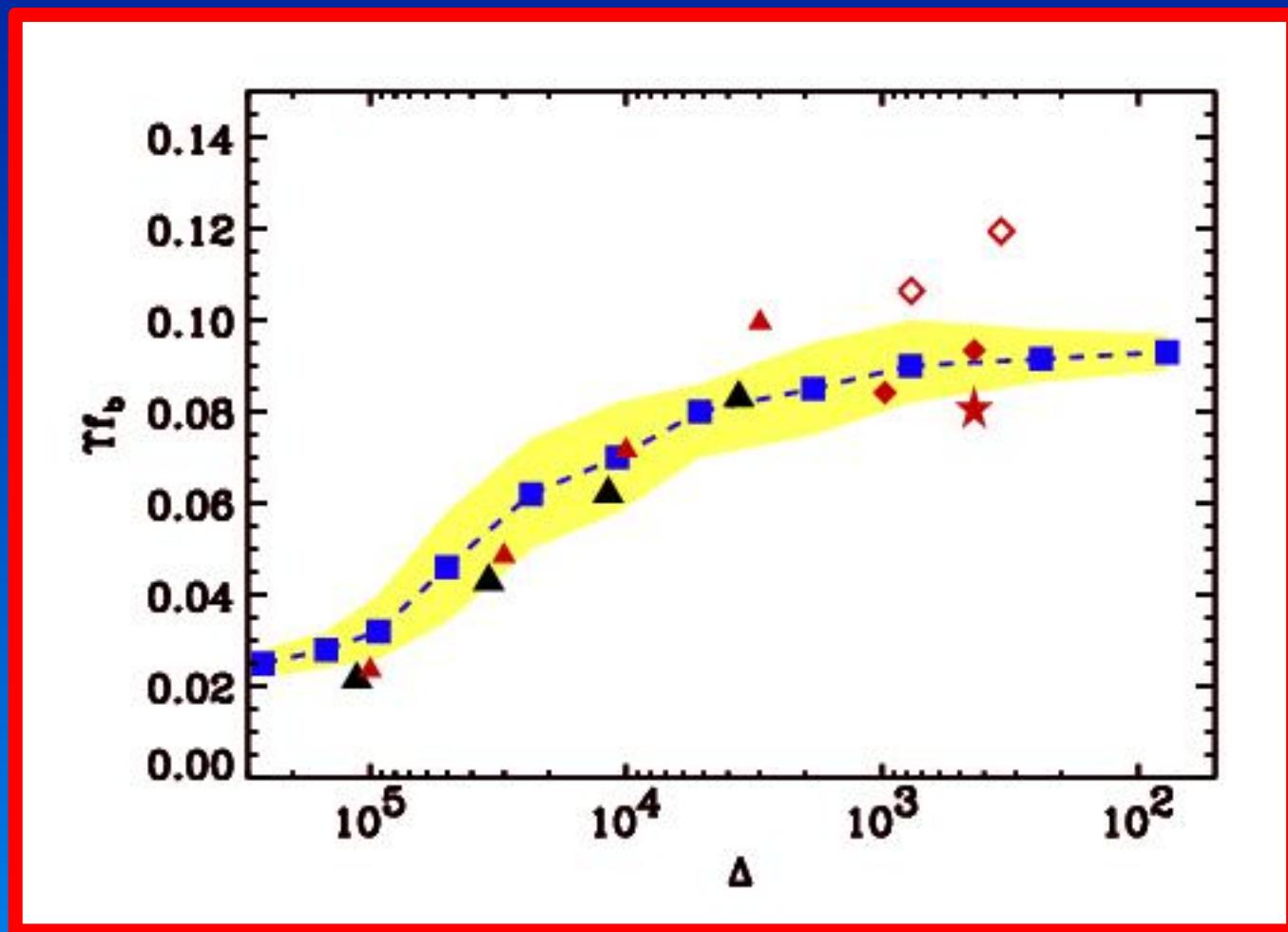
Average baryon fraction :



Three correcting factors :

- ◆ Mass estimator
- ◆ Clumping of the gas
- ◆ Outer emission

Baryon Fraction @ z = 0



R_{2000} & R_{1000} in Vikhlinin, Forman, Jones 1999 ($\sim 35\%$ & 50% Rv)

Conclusion

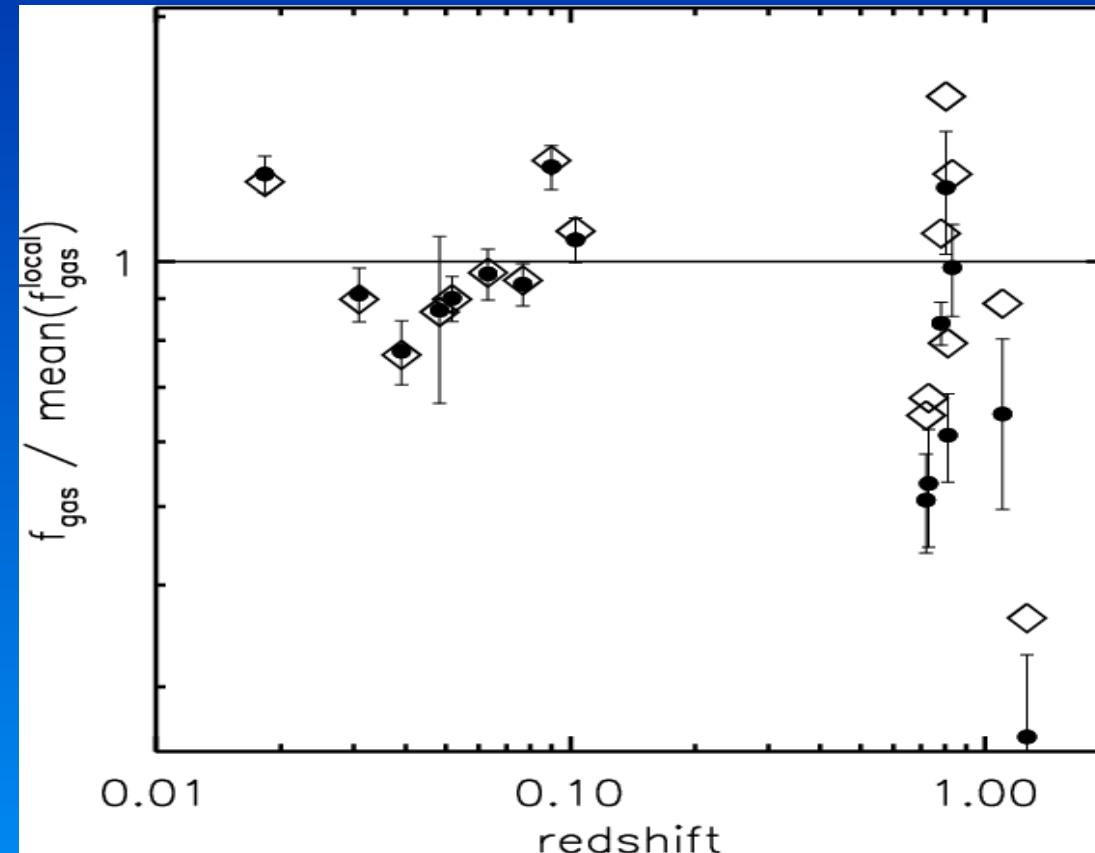
A baryon fraction of the order of $10 \cdot h_{50}^{-3/2} \%$
or less could be consistent with data...

$$\Omega_m$$

From X-ray Clusters

Baryon Fraction evolution

Baryon Fraction (non)evolution as a test of Ω_m



Chandra

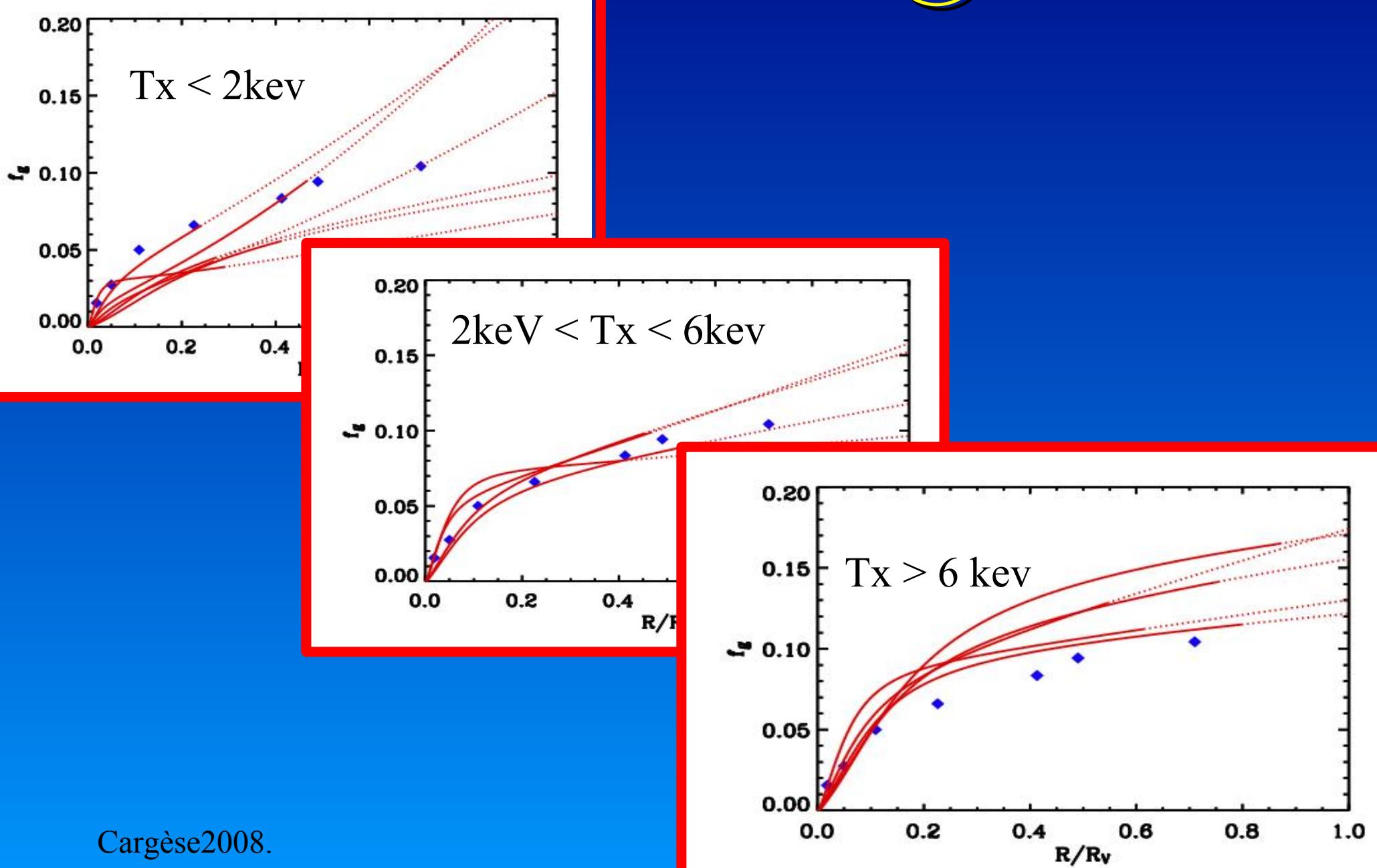
Ω_m

From X-ray Clusters

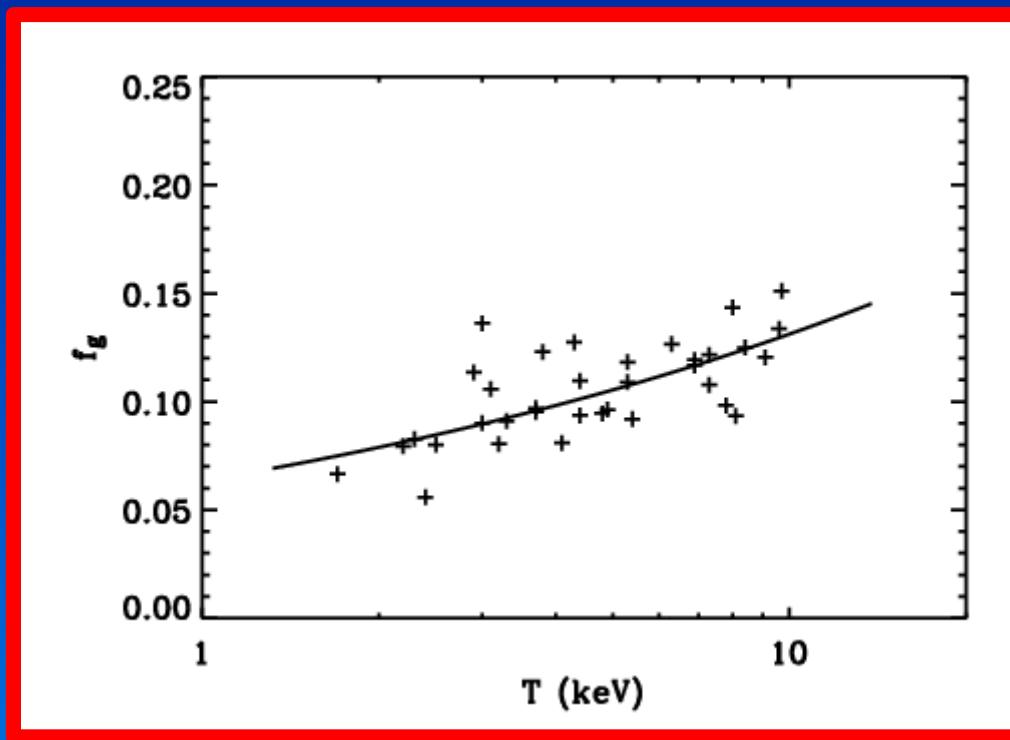
Baryon Fraction evolution
in the XMM Ω -project

(Sadat et al., 2005)

Barvon Fraction @ z = 0

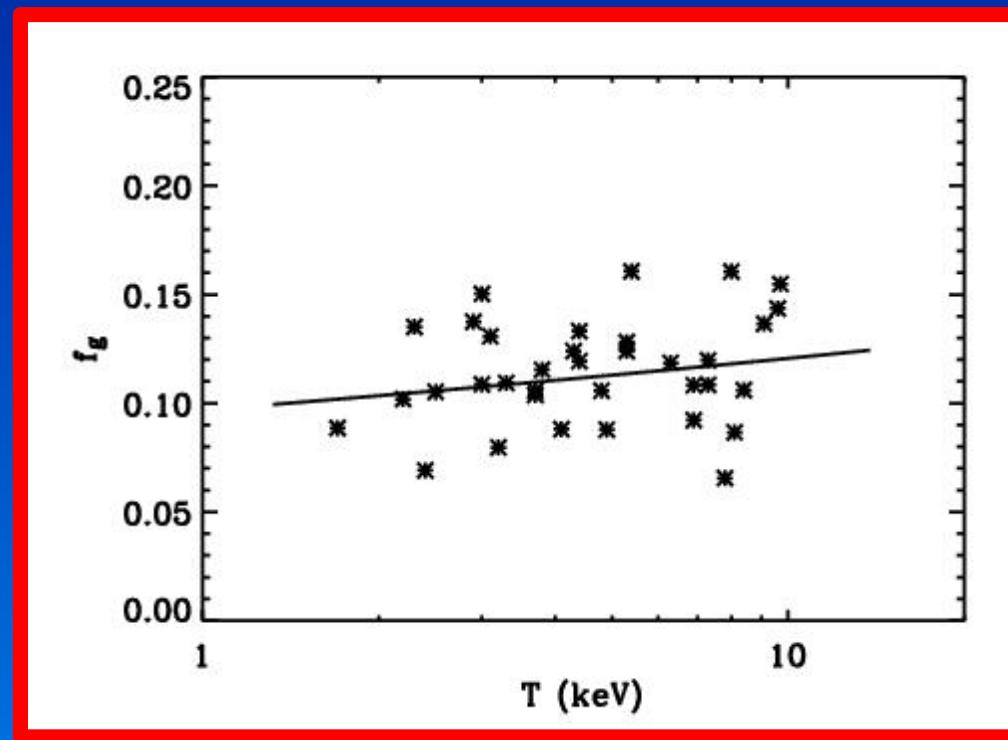


Baryon Fraction @ z = 0



R_{2000} in Vikhlinin, Forman, Jones 1999 ($\sim 35\text{-}45\%$ R_V)

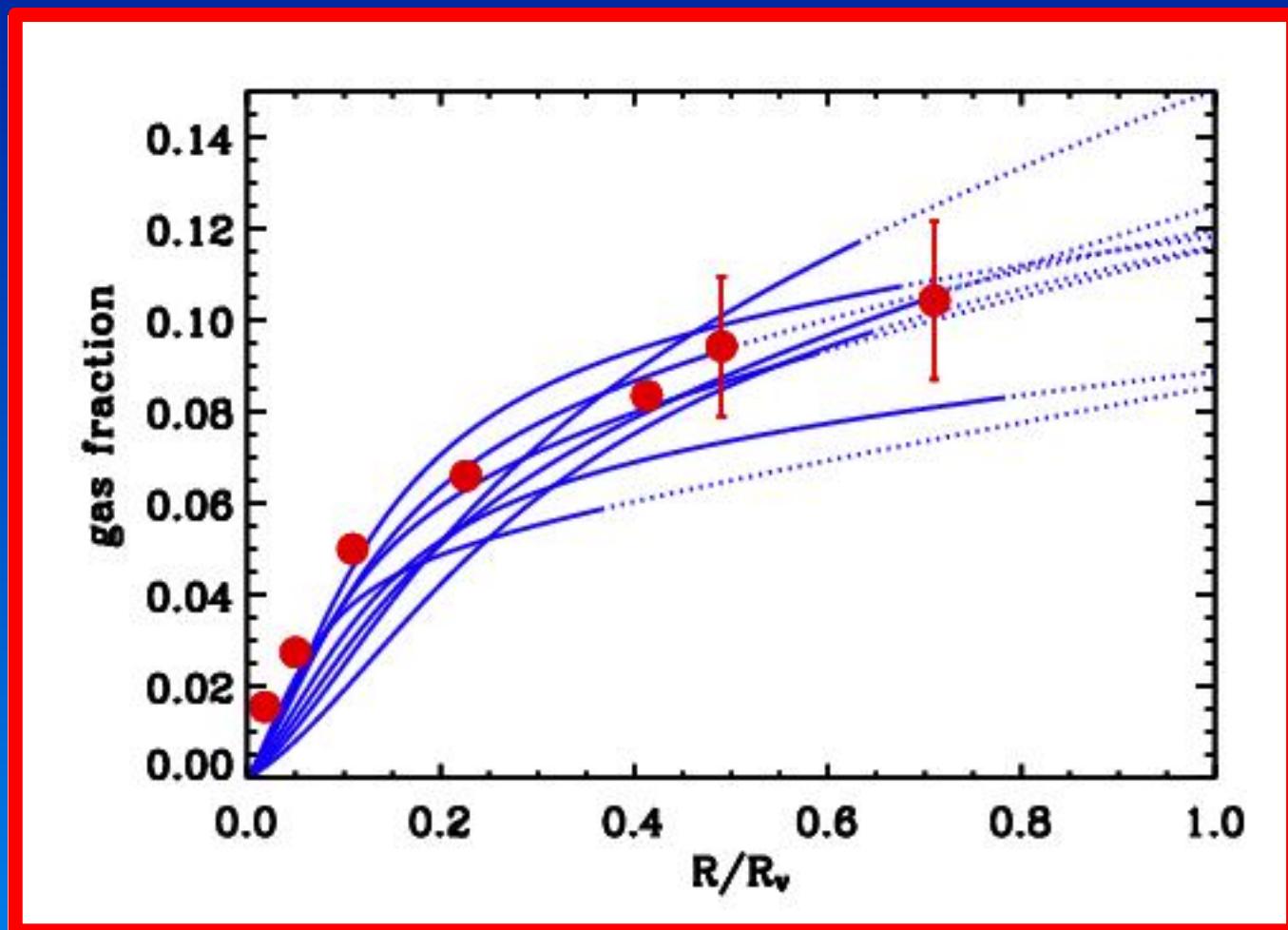
Baryon Fraction @ z = 0



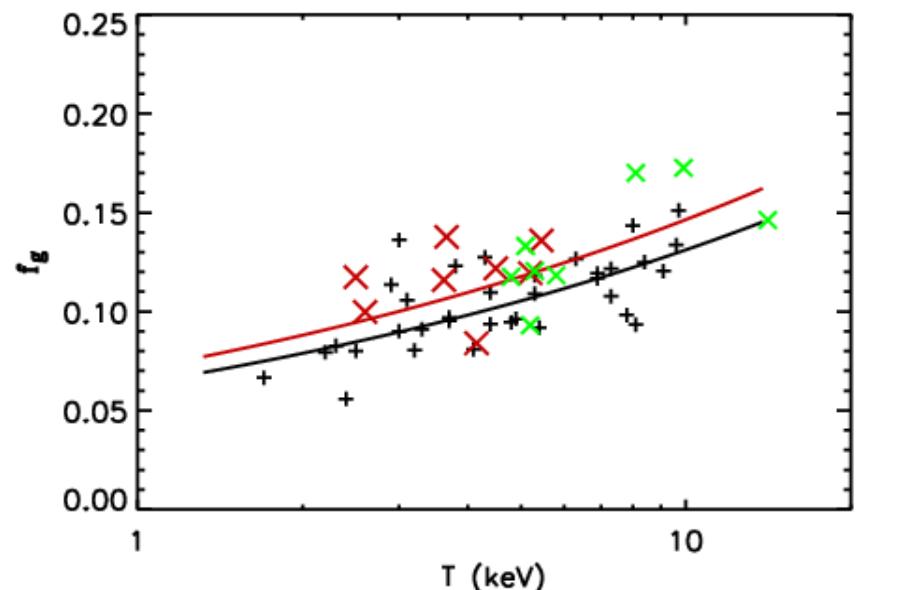
R_v in Vikhlinin, Forman, Jones 1999

I Evidencing (non-)scaling relations of X-ray clusters in the local universe

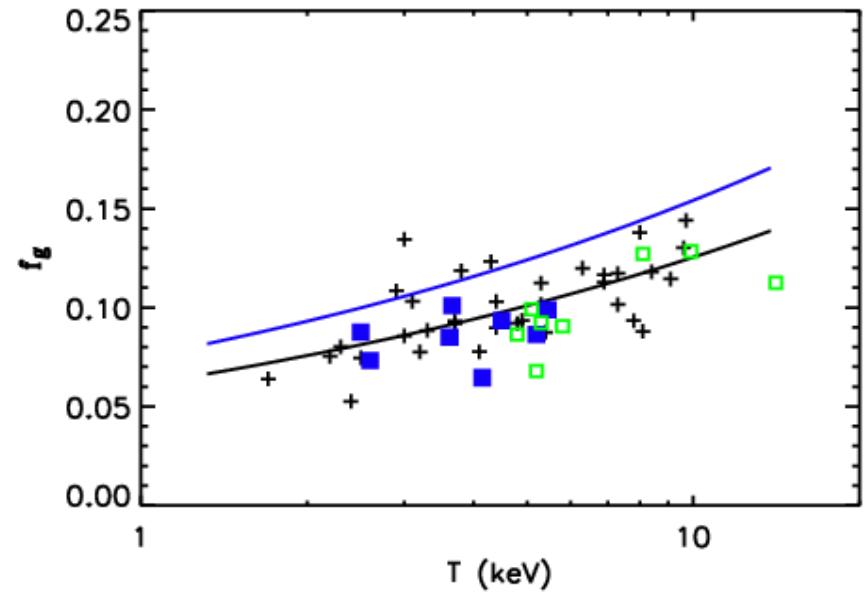
Baryon Fraction @ z = 0.6



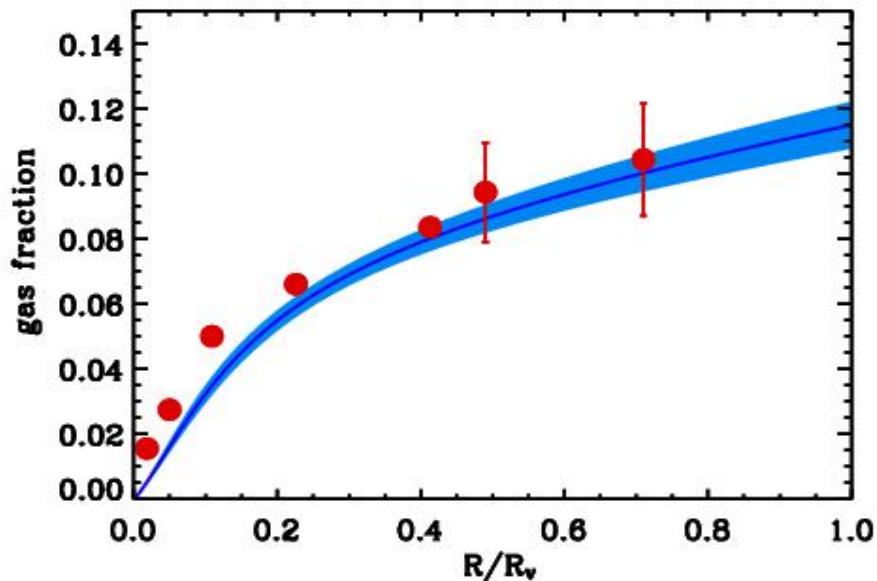
Baryon Fraction @ $z = 0.6$



$\Delta = 2000$

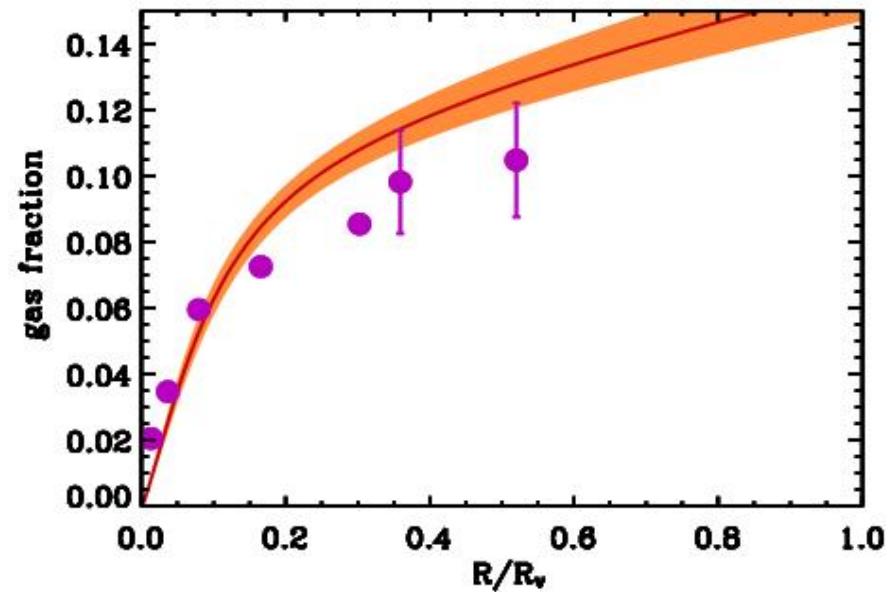


Baryon Fraction @ $z = 0.6$

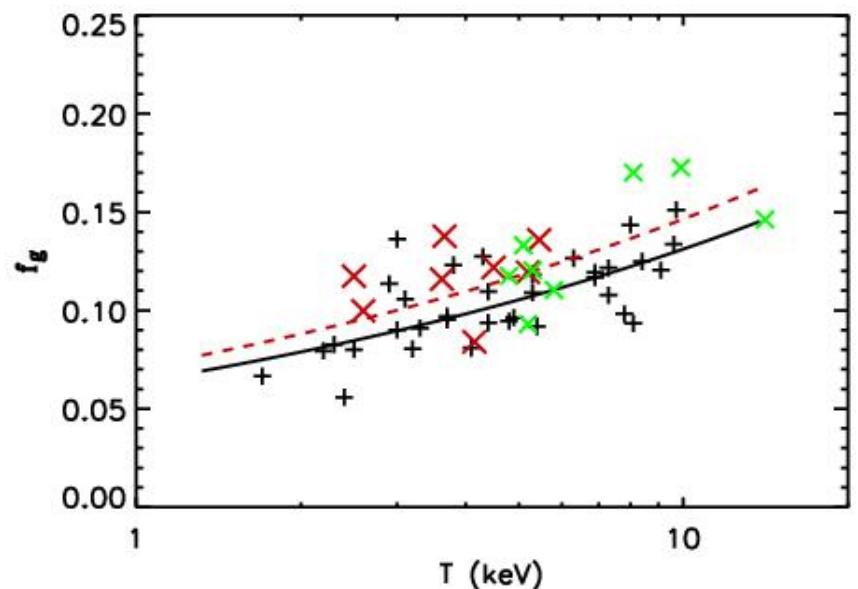


Internal structure

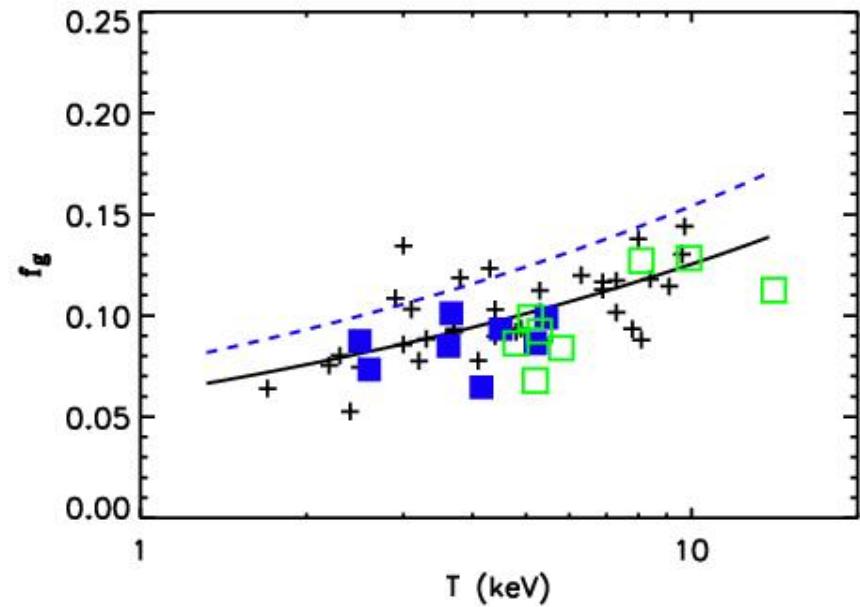
is complex...



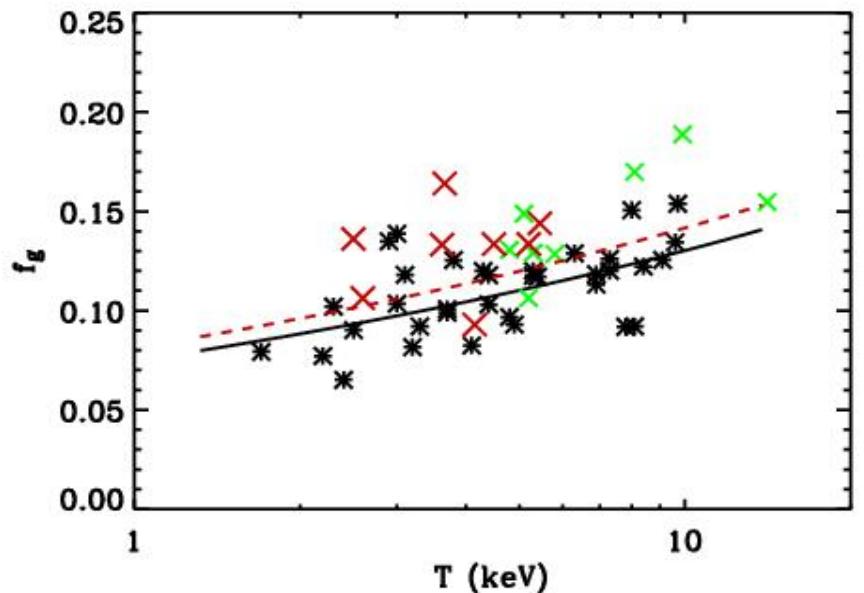
Baryon Fraction @ $z = 0.6$



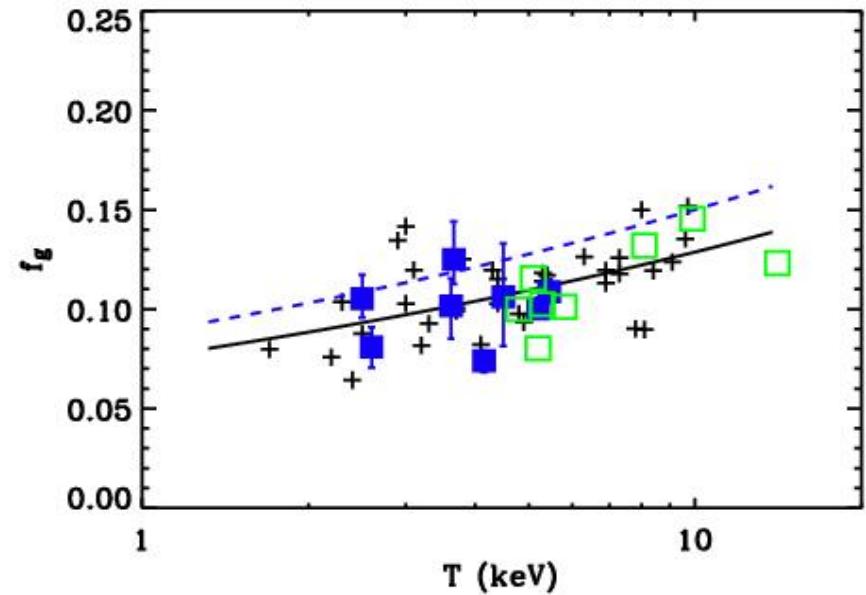
$\Delta = 2000$



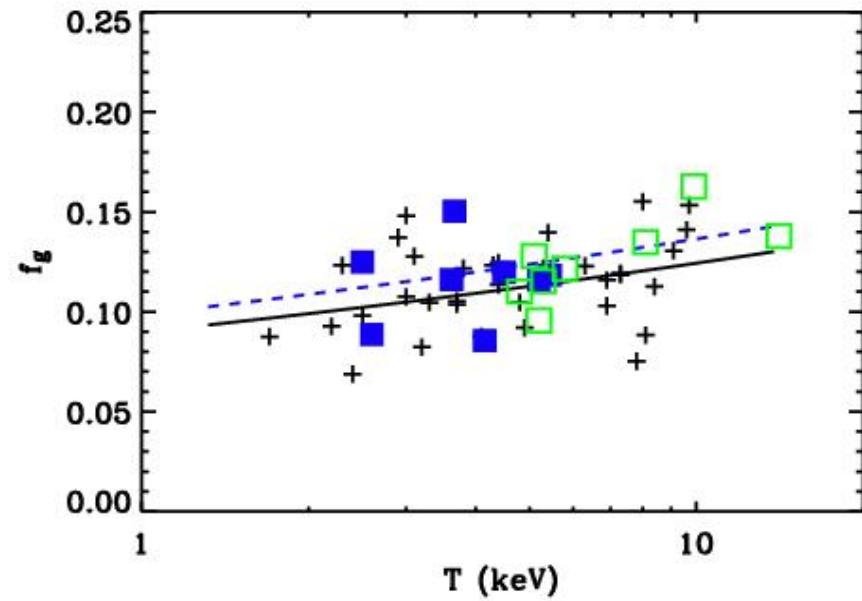
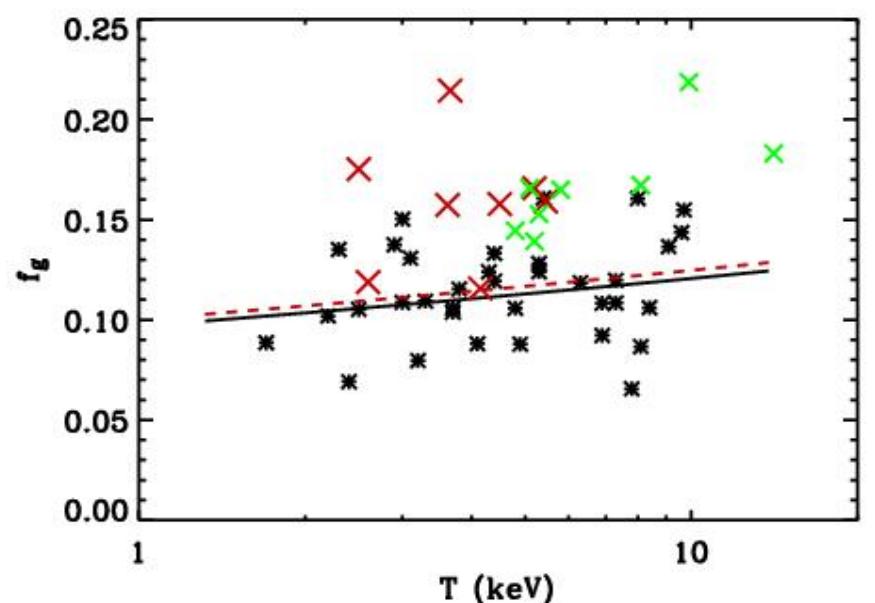
Baryon Fraction @ z = 0.6



$\Delta = 1000$

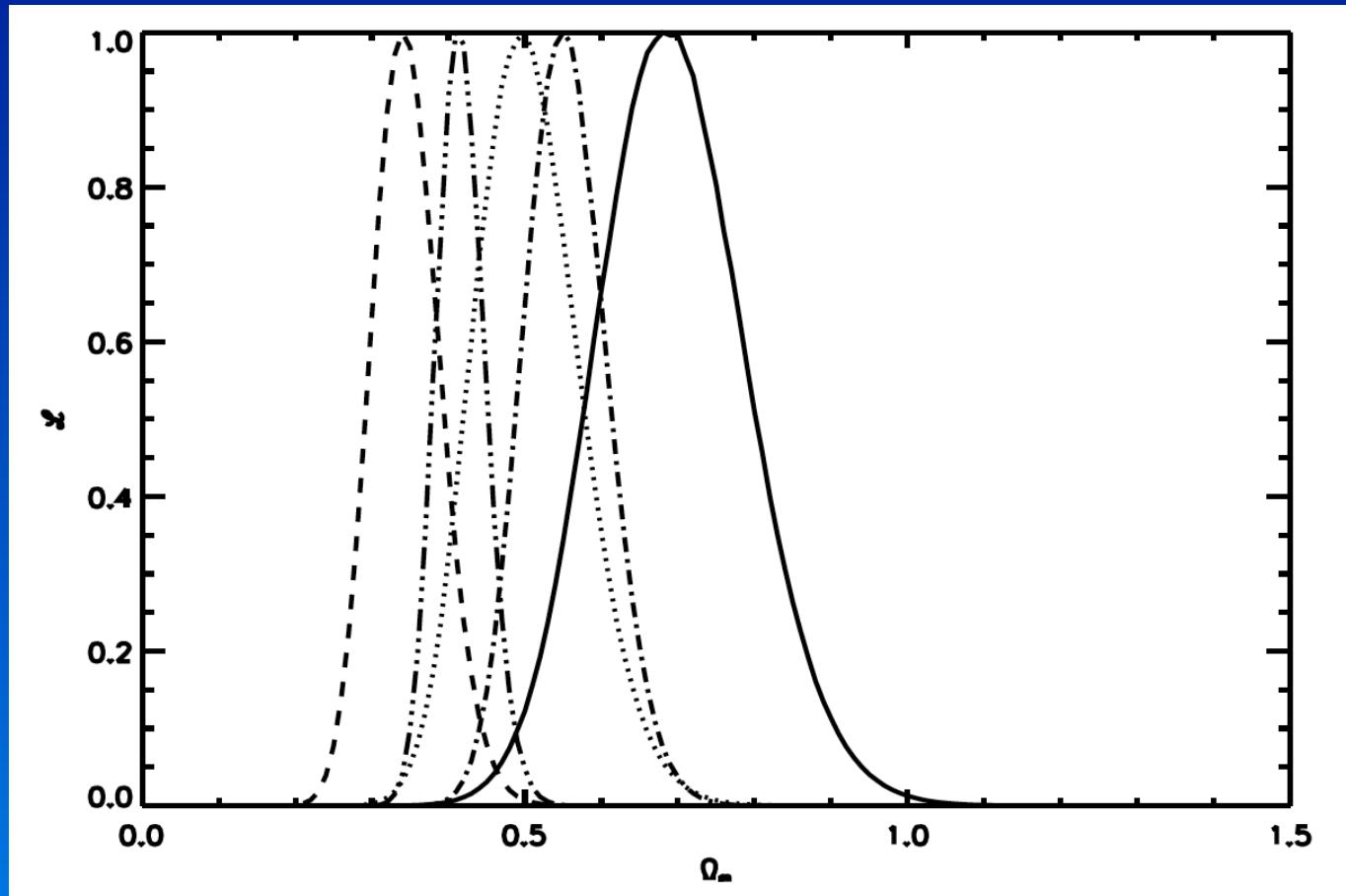


Baryon Fraction @ $z = 0.6$



$$\Delta_V$$

Likelihood analysis:



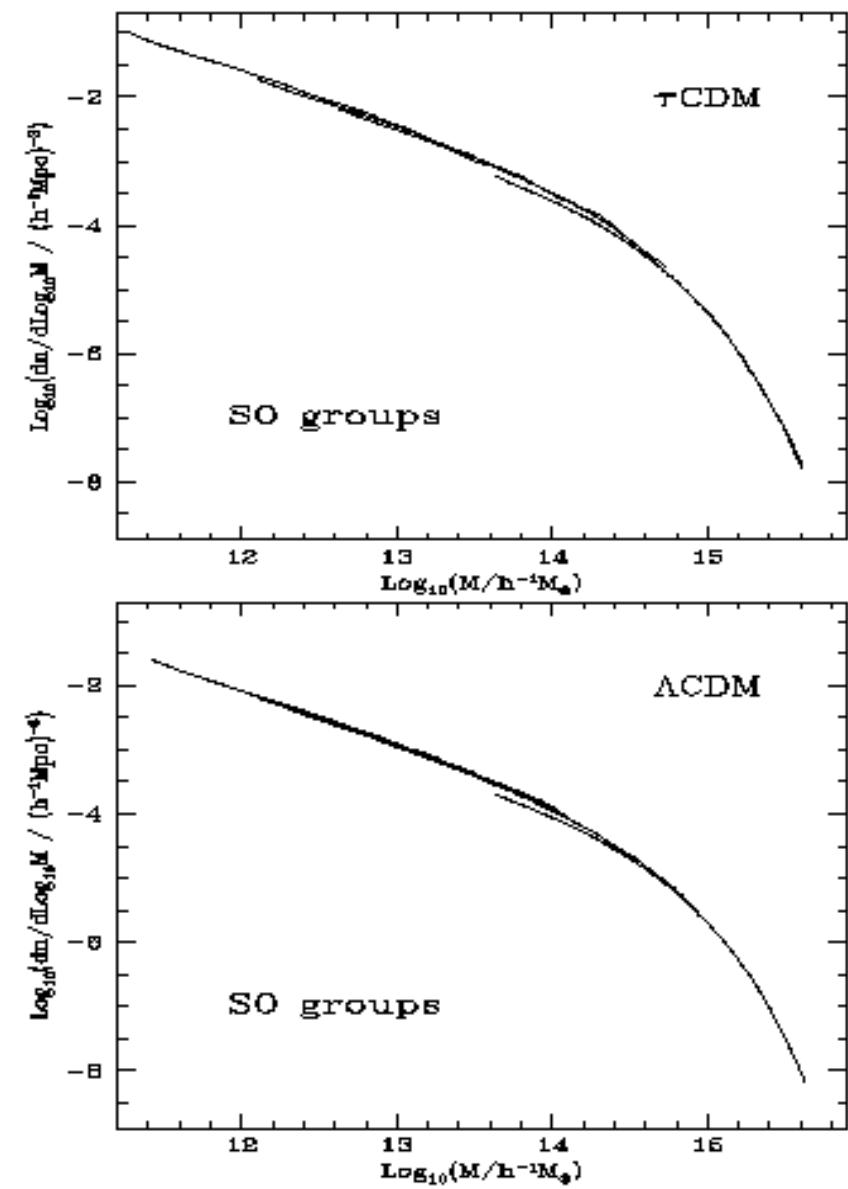
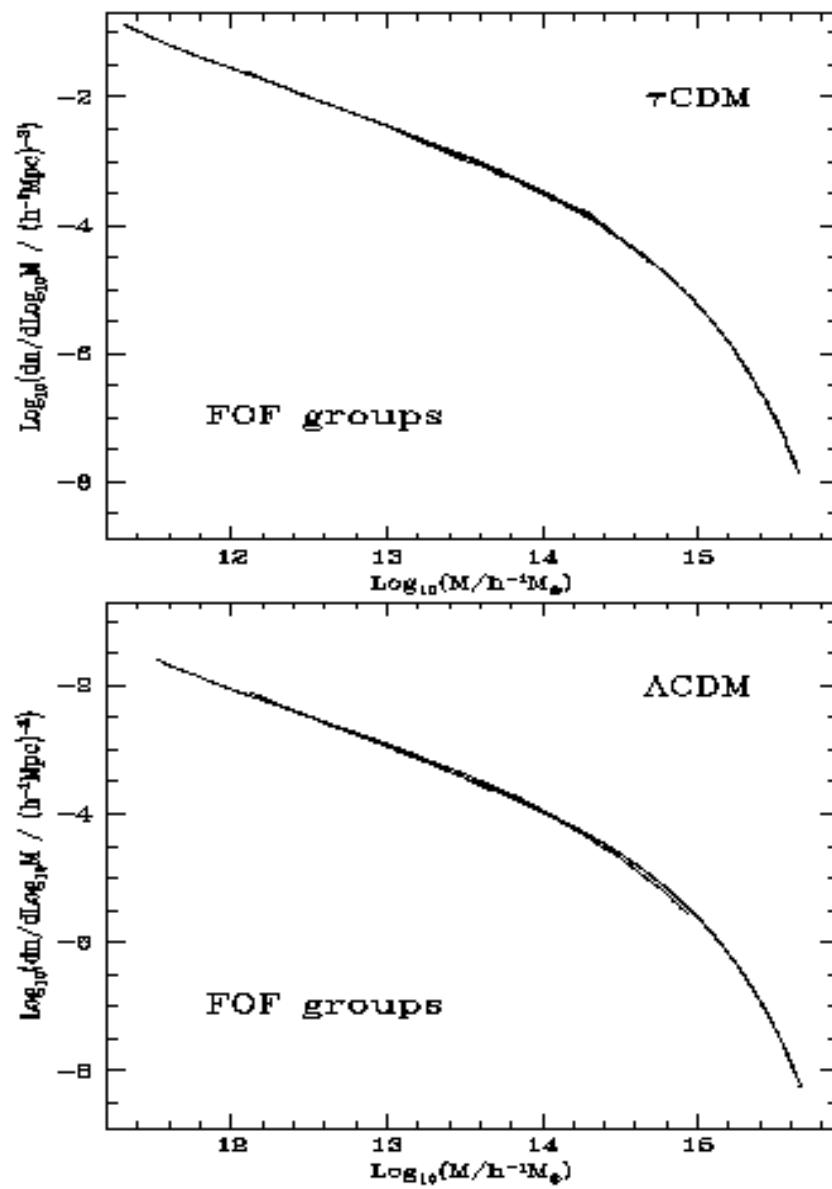
(Ferramacho, L. & B.A., 2007)

$$\Omega_m$$

From X-ray Clusters

Abundance evolution

Theory of the mass function



Basics

Matter = random field:

$$\rho(x) = \bar{\rho}(1 + \delta(x))$$

δ mathematically ill-behaved...

1. The field is smoothed = ρ is convolved:

$$\tilde{\delta} = \delta * W_R$$

with a window function:

$$\int W_R(u)du = 1$$

the smoothed field:

$$\tilde{\delta}(x) = \int \delta(x + u)W_R(u)du$$

Variance of the field :

$$\overline{\tilde{\delta}^2(x)} = \sigma^2(R)$$

Ex: top-hat window:

$$W_R(u) = \begin{cases} 1/V & \text{for } |u| < R \\ 0. & \text{for } |u| \geq R \end{cases}$$

Mass associated:

$$M(R) = \frac{4\pi}{3} R^3 \bar{\rho}$$

2. Nonlinear model

- linear overdensity

$$\tilde{\delta}(x) \sim 1$$

Ex: spherical model $\delta_{\text{NL}}(z, \Omega_m, \Omega_\lambda, \dots)$

3. Mass function:

- trivially (!): dV will be in an object with mass $> M$ if included in a NL fluctuation of $\tilde{\delta}_R$ with radius $> R$

$$\int_M^{+\infty} mn(m) dm = \bar{\rho} \int \mathcal{F}_\delta(\delta) s(\delta) d\delta \sim \bar{\rho} \int_{\delta_{NL}}^{+\infty} \mathcal{F}_\delta(\delta) d\delta$$

or (sharp threshold):

$$\int_M^{+\infty} mn(m)dm = \bar{\rho} \int_{\delta_{NL}}^{+\infty} \mathcal{F}_\delta(\delta)d\delta = \bar{\rho} \int_{\nu_{NL}}^{+\infty} \mathcal{F}(\nu)d\nu$$

with:

$$\delta = \nu\sigma(R) = \nu\sigma(M)$$

$$\text{and} \quad \nu_{NL} = \frac{\delta_{NL}}{\sigma(M)}$$

and just take the derivative...

the mass function:

$$N(M) = -\frac{\bar{\rho}}{M^2 \sigma(M)} \delta_{NL} \frac{d \ln \sigma}{d \ln M} \mathcal{F}(\nu_{NL})$$

normalization condition:

$$\frac{1}{\bar{\rho}} \int_0^{+\infty} m n(m) dm = \int_0^{+\infty} \mathcal{F}(\nu) d\nu = 1$$

Press and Schechter (1974) used:

$$\mathcal{F}(\nu) = \sqrt{\frac{2}{\pi}} \exp\left(-\frac{\nu^2}{2}\right)$$

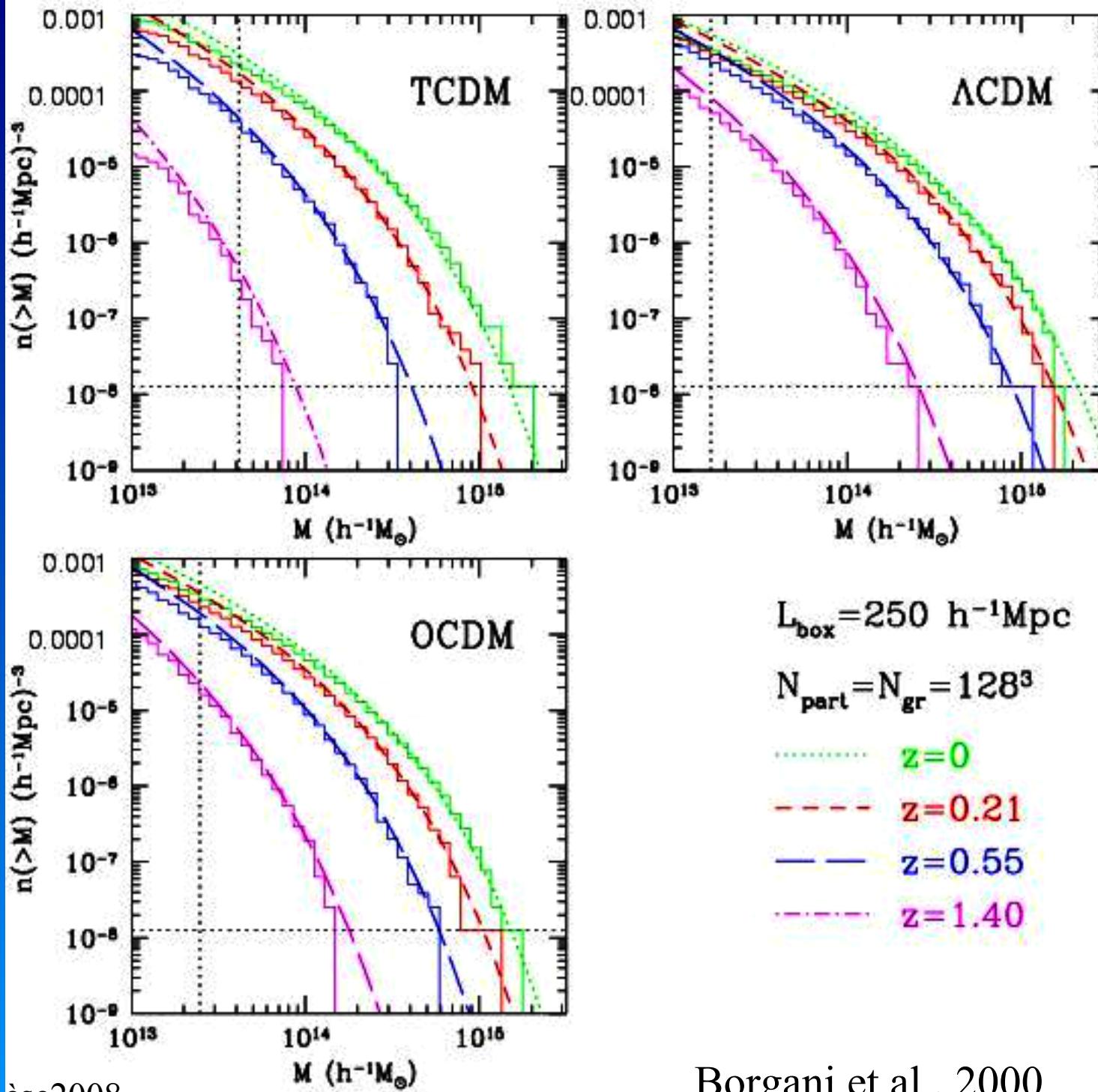
major recent improvements:

$$\mathcal{F}(\nu) = \sqrt{\frac{2A}{\pi}} C \exp(-0.5A\nu^2)(1. + (A\nu)^2)^Q$$

with

$$A = 0.707 \quad C = 0.3222 \quad Q = 0.3$$

TESTING THE MASS FUNCTION



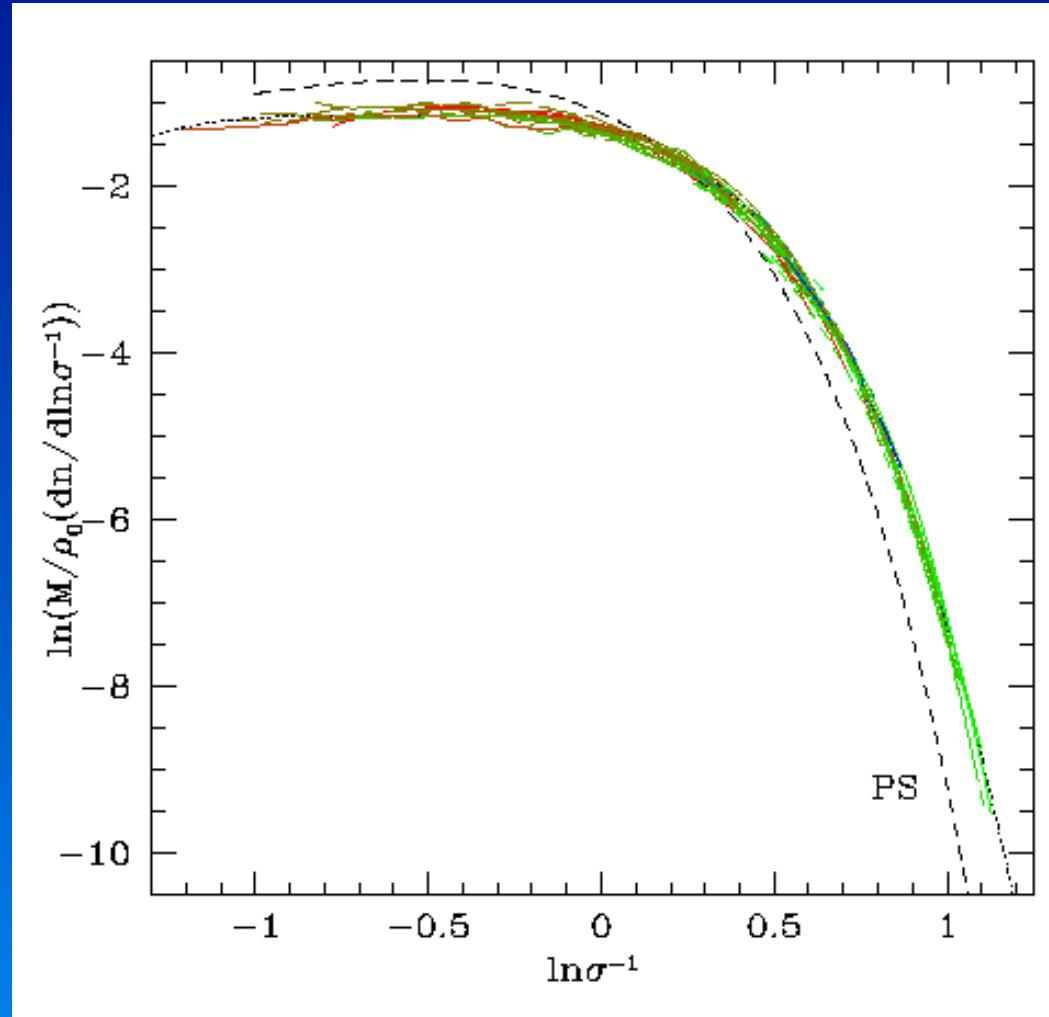
Cargèse 2008.

Borgani et al., 2000

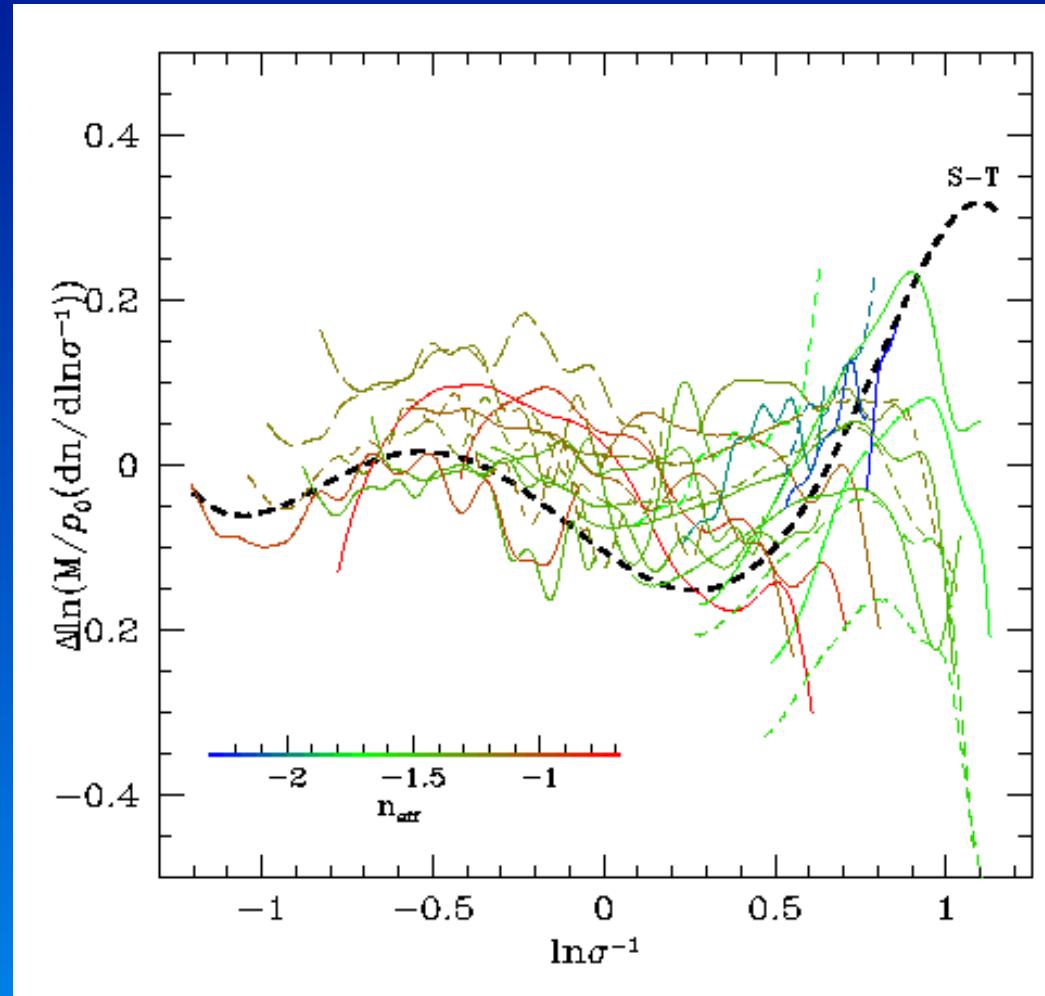
M
A
S
S

F
U
N
C
T
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O
N

Checking $N(M)$



Checking N(M) (2)



Conclusion

Reasonable description
of the mass function in
numerical simulations...