Inflation and f(R) Dark Energy

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Hot Topics in General Relativity and Gravitation

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History of Universe



Inflationary Universe



Linde's talk

Energy evolution...



D. Kirby, CIPANP 2015

Big Bang

- Hubble expansion, light element abundance (BBN), leftover Black body radiation (CMB)
- What preceded Big Bang ?
- BSM: DM/DE, Perturbation evolution, Inflation
- Universe is homogeneous ?
- Isotropic Universe (same in all directions) ?
- Simultaneous expansion for all parts ?
- Universe is flat
- So many particle in Universe and it is so large

Cosmic Inflation

- Inflation solves some of the problems associated with the old Big Bang Theory.
- Inflation: In fact provides an explanation for how the Universe could have been created out of matter less than one milligram.
- Solves the issues like flatness, horizon and monopole problems.
- Simply a brilliant idea and of course surprising
- Expt. verification may be around (BICEP2???)

Inflation

 The scalar field φ moves very slowly and that is why the potential energy essentially remains a constant for a fair amount of time.

$$\frac{\dot{a}}{a} = Const. = H \to a(t) = e^{Ht}$$

(this is termed as inflation)

Inflation and DE

- Inflation makes the Universe flat
- Adding a constant to the inflationary potential, one can get inflation as well as DE

$$V = \frac{1}{2}m^2\phi^2 + \Lambda$$

• (simplest model to explain Inflation and DE)

$$p = T - V(\phi) \ ; \ \rho = T + V(\phi) \ ; \ \omega = \frac{p}{\rho}$$

Challenging problem.. (DE)

• Several cosmological observations demonstrated that the Universe is expanding and is accelerating

• What is causing this acceleration?

 How can we learn more about this acceleration, the Dark Energy it implies, and the questions it raises?

• EOS only tells w=-1.

• Universe is accelerating

- Type la Supernovae observations (SNe la)
- Cosmic Microwave Background Radiation (CMBR)
- Cluster of Galaxies (Large scale structure)



 $\Omega_{\rm M}$

Dark Energy: Expansion History Constraints



 Constraints consistent with a ΛCDM cosmology (i.e., a constant dark energy equation of state, w=-1), even after allowing for a nonzero curvature (Ω_K) or evolving dark energy (w_a)

Talk by M. Vargas

CIPANP 2015

Observations

- Dark Energy: 73%
- Dark Matter: 23%
- Baryons: 4%
- Massive neutrinos : 0.1%



$$\begin{split} \Omega_{\rm M} &= \rho_{\rm M} / \rho_{\rm c} \\ \Omega_{\Lambda} &= \rho_{\Lambda} / \rho_{\rm c} \\ \rho_{\rm c} &= 3 {\rm H}^2 / 8 \pi \\ {\rm H} &= {\rm Hubble \ Const.} \end{split}$$

Dark Energy

- Dark Energy: Most embarrassing observation in Physics – A. Einstein
- Is it Cosmological Constant?
- Is it a Failure of GR?
- Quintessence?
- Novel property of matter?
- Many ideas have been proposed

Einstein's Eqn.

- Einstein Equation: $G_{\mu\nu} = 8\pi G T_{\mu\nu}$ (Testable theory of the Universe)
- where R $_{\mu\nu}$ ½ R g $_{\mu\nu}$ = G $_{\mu\nu}$
- and R = $g_{\mu\nu}R^{\mu\nu}$ (Ricci scalar)
- * GR is well tested, but not unique.

Is there any alternate option?



f(R) gravity

- Inflation and Dark Energy (Cosmic acceleration but different energy scales) (energy density differ by $\sim 10^{120}$) Modify the gravity sector \rightarrow **modify** $G_{\mu\nu}$ (f(R) gravity model..) OR Modify the matter sector -> modify T_{uv} (scalar field model..)
- If one includes Cosmological constant (Einstein):

$$G_{\mu\nu} + \Lambda g_{\mu\nu} = 8\pi G T_{\mu\nu}$$

f(R)

• In the simplest generalization of General Relativity one can write the action:

$$S = \frac{1}{16\pi G} \int d^4x \sqrt{-g} f(R) + S_M$$

In GR f(R) = R so df/dR =1)

- In the modified gravity scenario: $\frac{df}{dR} \neq 1$
- Let us consider f(R)= a R²
- Since the de Sitter solution in f(R) gravity gives
 (df/dR)R 2 f =0 it so happens that f(R)= aR² gives
 rise to de Sitter expansion. (Starobinsky 1980)
- * Disappearing Λ in f(R) gravity: (Starobinsky 2007)

Dark Energy and Modified Gravity

- Dark Energy: About 70% of the energy density today consists of Dark Energy, which is responsible for Cosmic acceleration.
- The simplest one is the Cosmological Constant (w=p/p=-1)
- => If the cosmological constant originates from a vacuum energy then it is in fact much more larger than the scale of the Dark Energy

- Other dynamical DE models, where w \neq -1
- i) Modification of the matter sector: Quintessence, k-essence..
 - ii) Modification of gravity:
 - f(R) gravity model, scalar-tensor theory..

Here we will consider the simplest one: f(R) model of gravity for Dark Energy

Starobinsky (1980, 2007), De Felice-Tsujikawa (2010), Artymowski-Lalak (2014), Takahasi-Yokoyama(2015)...

Modified Gravity for DE

- Modification of Gravity can give rise to observational signatures, DE equation of state, impact of LSS, CMB etc., which one can see on large scales.
- In small scales, the modification may not be significant and may be very close to the GR predictions (with small corrections) in case of Solar system experiments.

f(R) Inflation

- An example is the Starobinsky model of Inflation, with the account of a correction quadratic in the Ricci scalar in the modified framework, and of an exponential potential in the scalar field framework.
- Where $f(R) = R + R^2/6M^2$
- (during the inflation the R² term dominates, which actually give de Sitter like expansion)

Starobinsky model

- Since we have introduced the model, let us see;
- A) when R²/ (6 M²) >> R: Inflationary expansion
- B) when $R^2/(6 M^2) \sim R$: End of Inflation
- C) when R²/ (6 M²) << R: This is called the Reheating stage, where the scalar R oscillates around the minimum value of R=0.
- One can then discuss the inflation and reheating scenarios.

$f(R) = R + a R^m + b R^n$

- Dark Energy models with f(R) have been considered:
- (Alternative cosmologically viable f(R) model exists by Amendola et al, Amendola-Tsujikawa, Hu-Sawicki, Starobinsky)
- $f(R) = R + \alpha R^n \beta R^{2-n}$ (Artymowski+Lalak)
- (α and β are positive constants)
- Let us consider $f(R) = R + \alpha R^n$, and to obtain Inflation one must satisfy:

$$n \in \left[\frac{1}{2}(1+\sqrt{3}), 2\right]$$

$f(R) = R + \alpha R^n - \beta R^{2-n}$

- Let us consider $\alpha \gg 1$, $\beta \ll 1$ and $\alpha\beta << 1$ This means that $\alpha R^n >> R >> \beta R^{2-n}$ during inflation.
- The last term will not affect inflation
- The Einstein frame scalar potential has a minimum

$$R_{min} = \left(\frac{\sqrt{1+4(2-n)n\alpha\beta} - 1}{2(2-n)\alpha}\right)^{\frac{1}{n-1}} \simeq (n\beta)^{\frac{1}{n-1}} \left(1 - \frac{(2-n)n\alpha\beta}{n-1}\right)$$

• The value of V at the minimum for small β :

$$V(\varphi_{min}) \simeq \frac{n}{8(n-1)^2} (n\beta)^{\frac{1}{n-1}} \left(n-1-n^2\alpha\beta\right) \sim \frac{1}{2}\beta^{\frac{1}{n-1}}$$

- The energy density for DE ~ $\beta^{\frac{1}{n-1}}$ ($\beta <<<1$)
- The existence of stable minimum is the key point.

f(R) screening

* In solar system experiments as well as pulsar timing measurements the GR is tested to high accuracy

* In largest scales gravity is modified so as to have an accelerating Universe without cosmological constant.

 At small scales the screening mechanism helps recover the GR (Chameleon mechanism: Khoury & Weltman).The fifth force is blind to small scales and becomes noticeable at larger scales

OUTLOOK

- Standard Model of Particle Physics complete
- No trace of BSM, DARK Matter
- Flavor Connection? LHC input?
- Cosmology? Centenary year of GR ...
- Gravitational Waves? Gravitons? Q Gravity?
- Lessons from INFLATION
- DARK ENERGY/ MODIFIED GRAVITY???
- In my opinion, exciting time ahead !!!!!

Comparison of Cold Dark Matter (CDM) and sterile neutrino simulations of Milky Way-like dark matter haloes (the invisible "skeleton" within which the galaxy will actually form). Credit: M Lovell/ICC Durham. /RAS meeting 7 July, 2015



the end