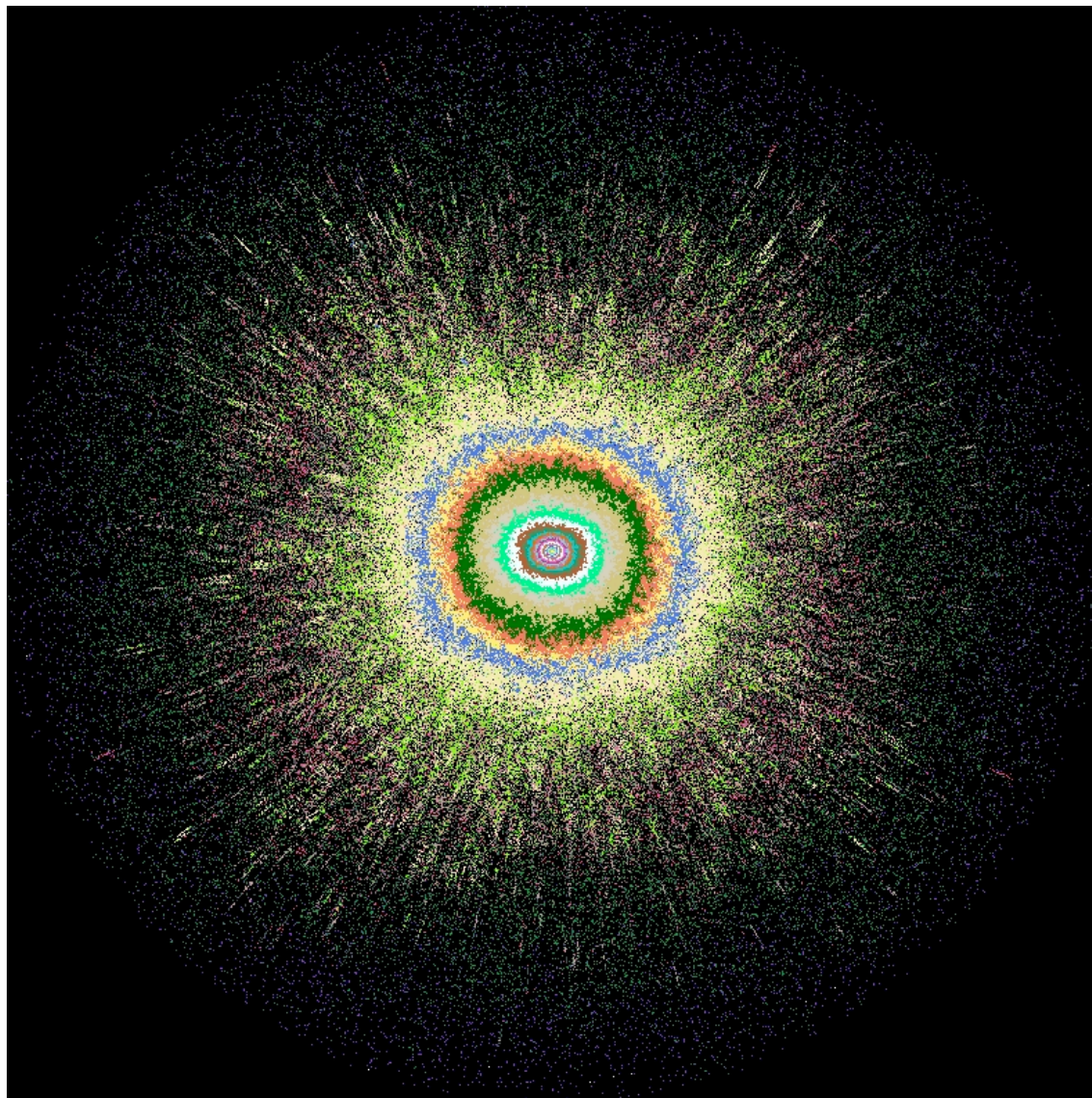
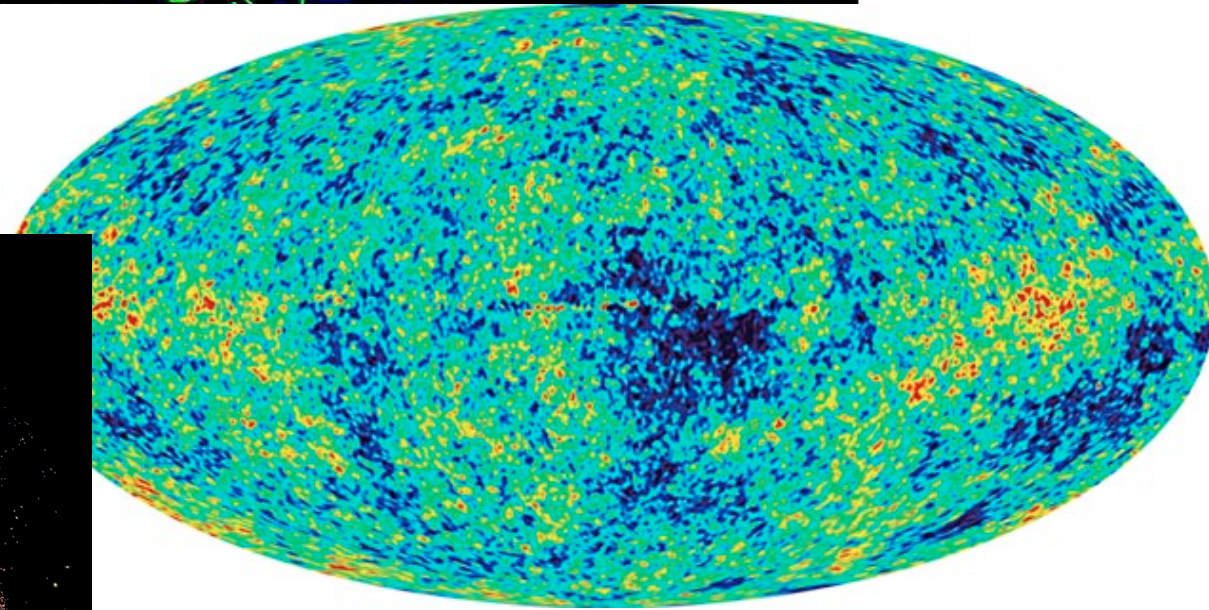
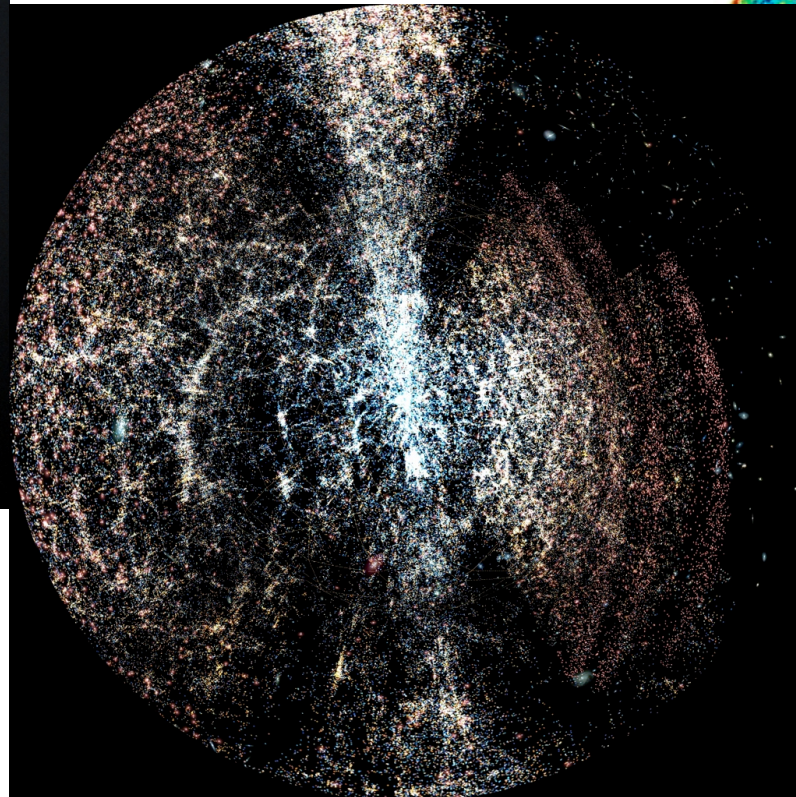
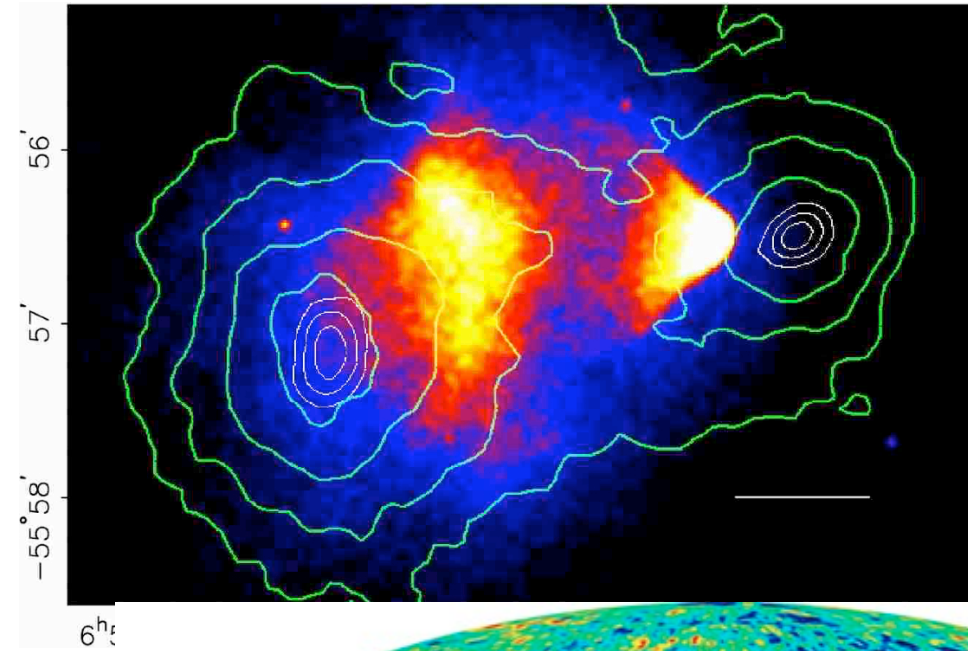


Dark Matter velocity anisotropy - observations and theory

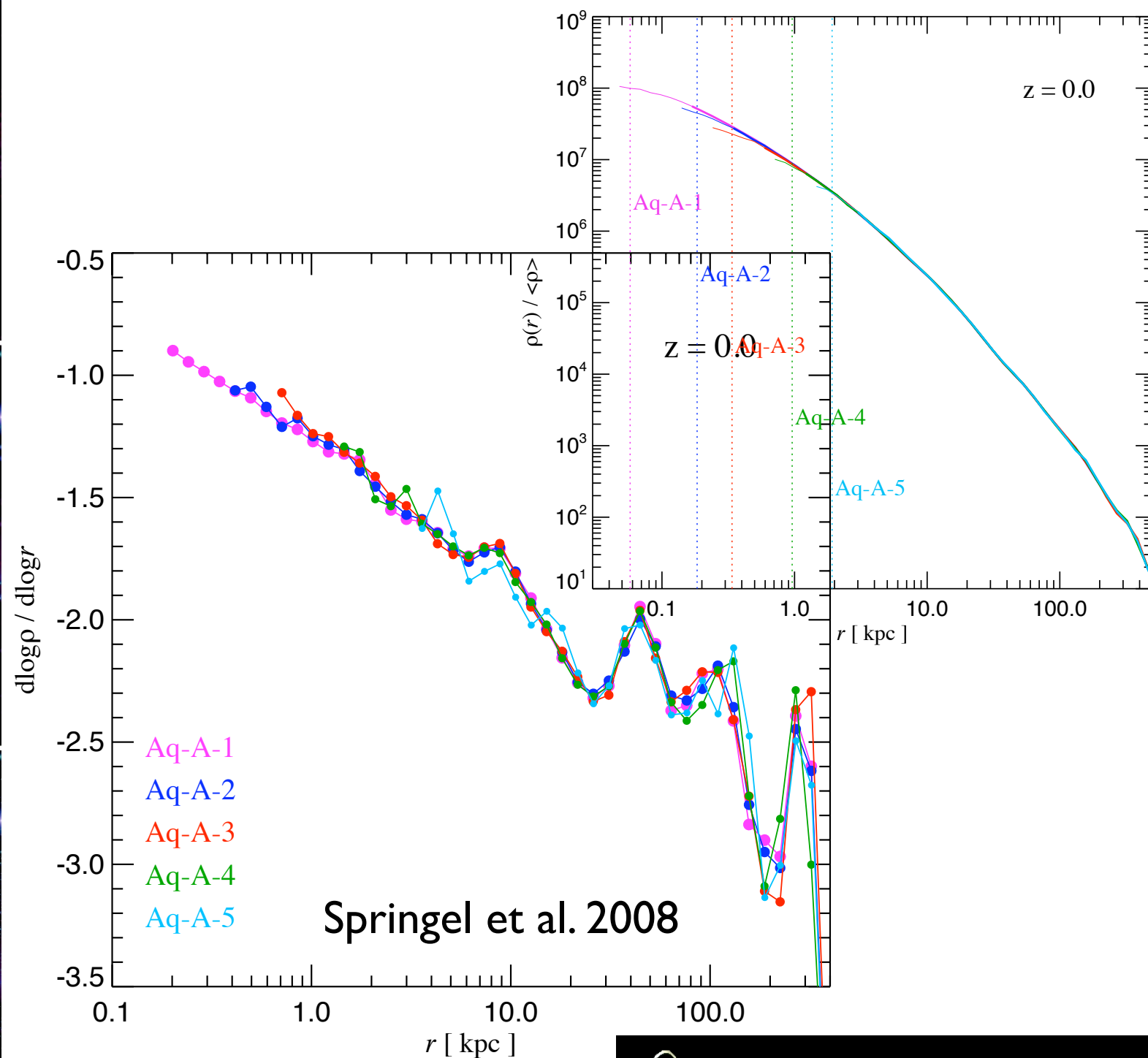
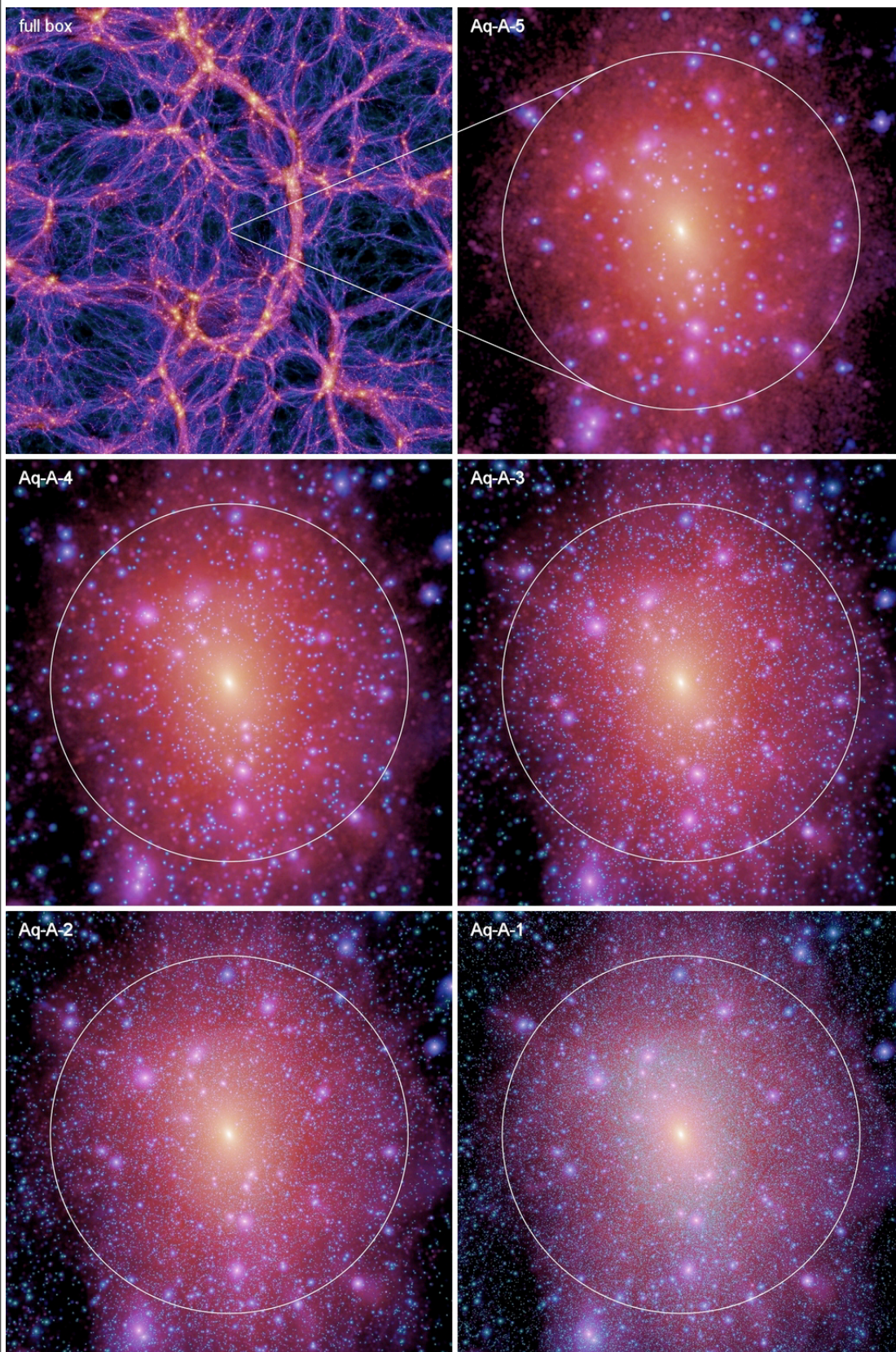


Steen H. Hansen,
Dark Cosmology Centre, NBI
Cargese, Corsica
SW3, April, 2009

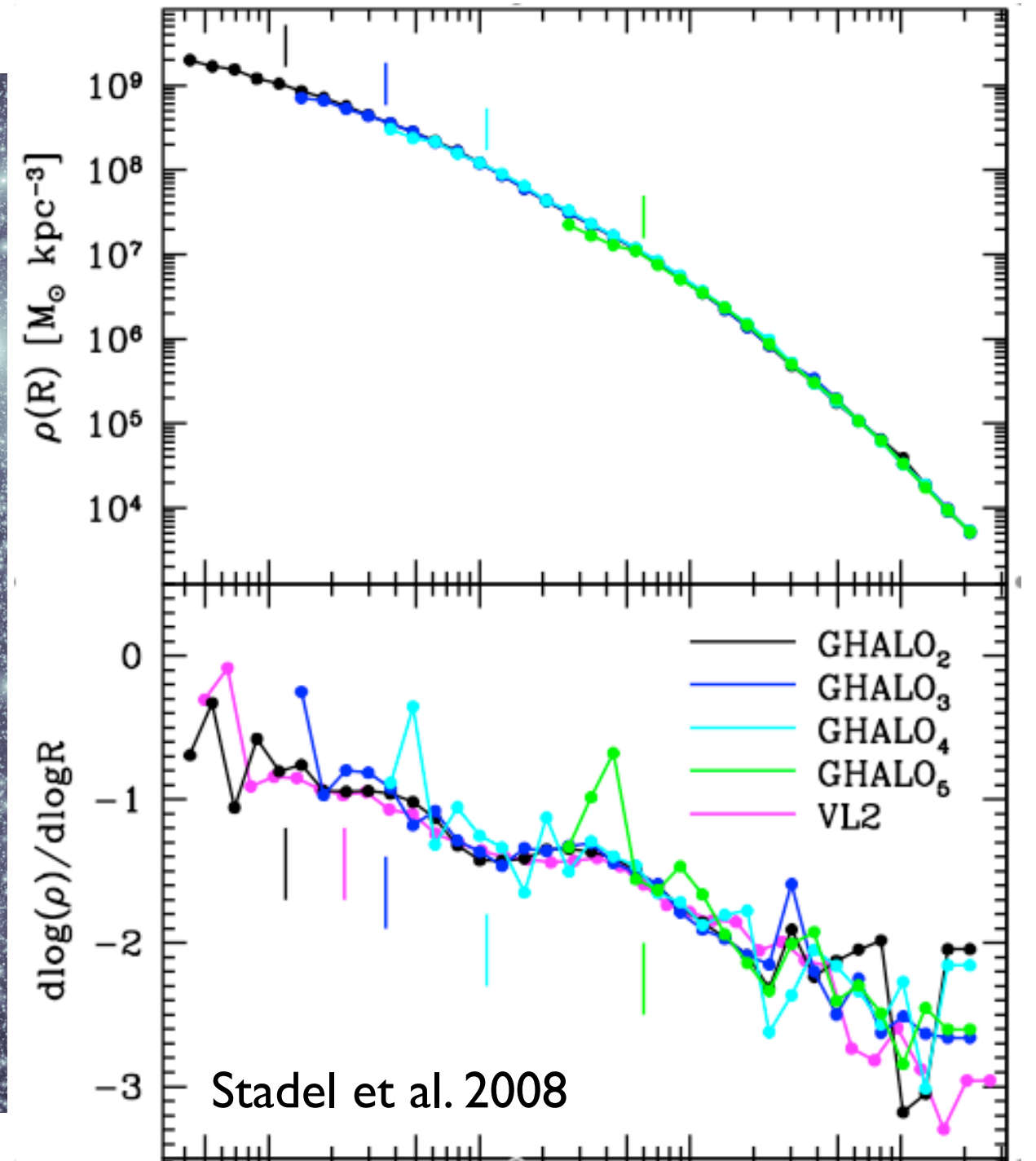
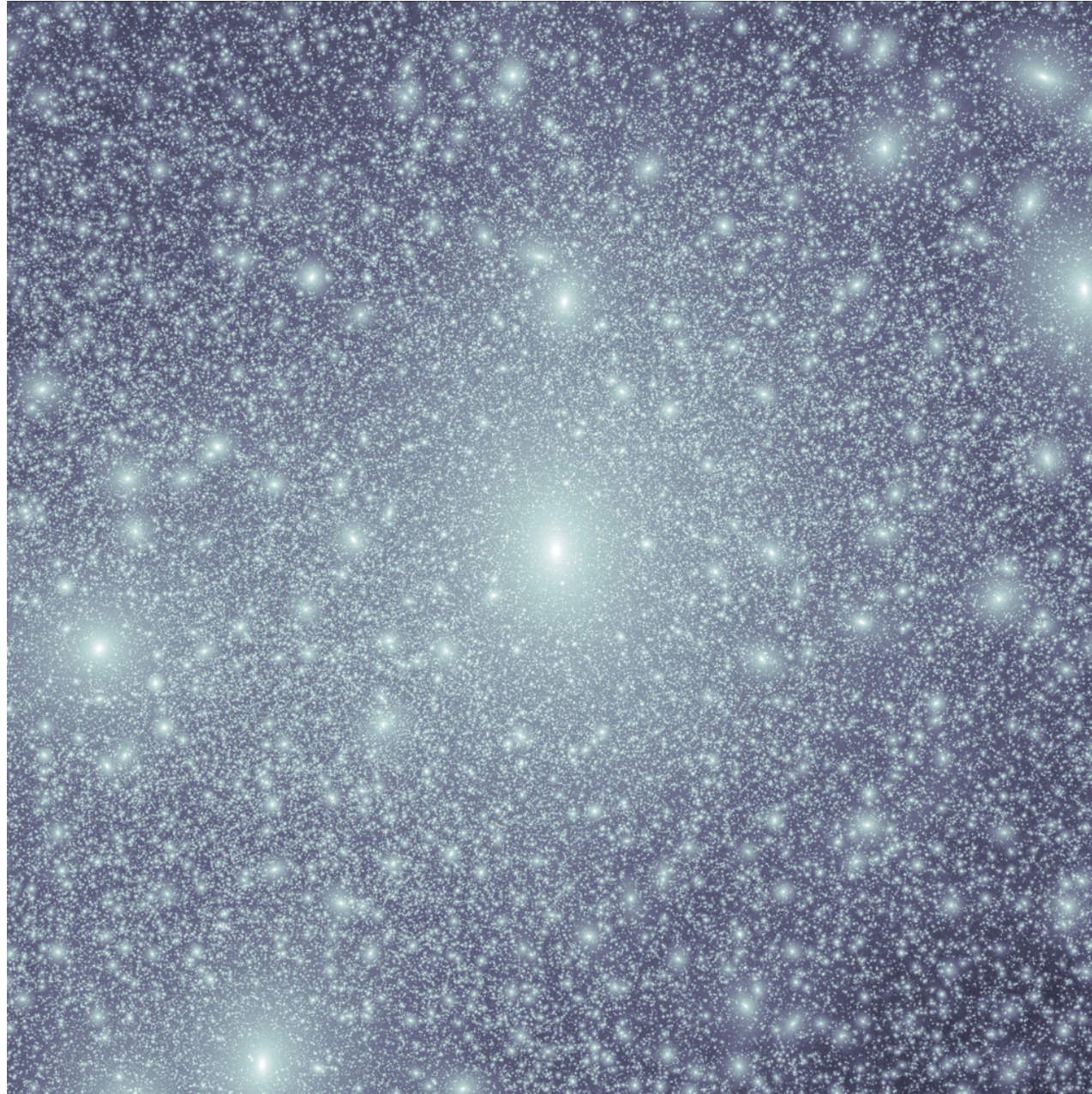
Dark matter observations



Simulated density profiles

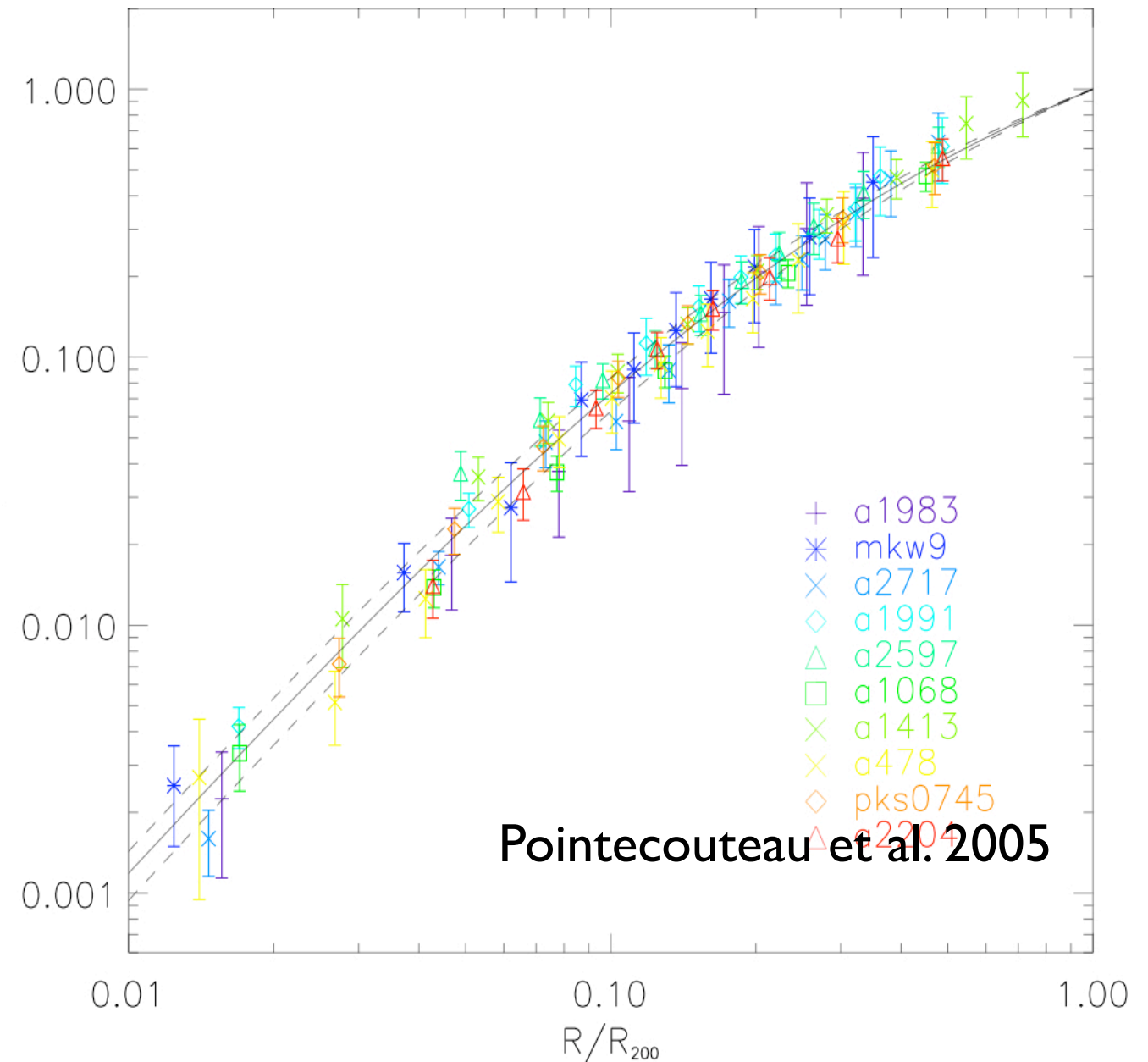
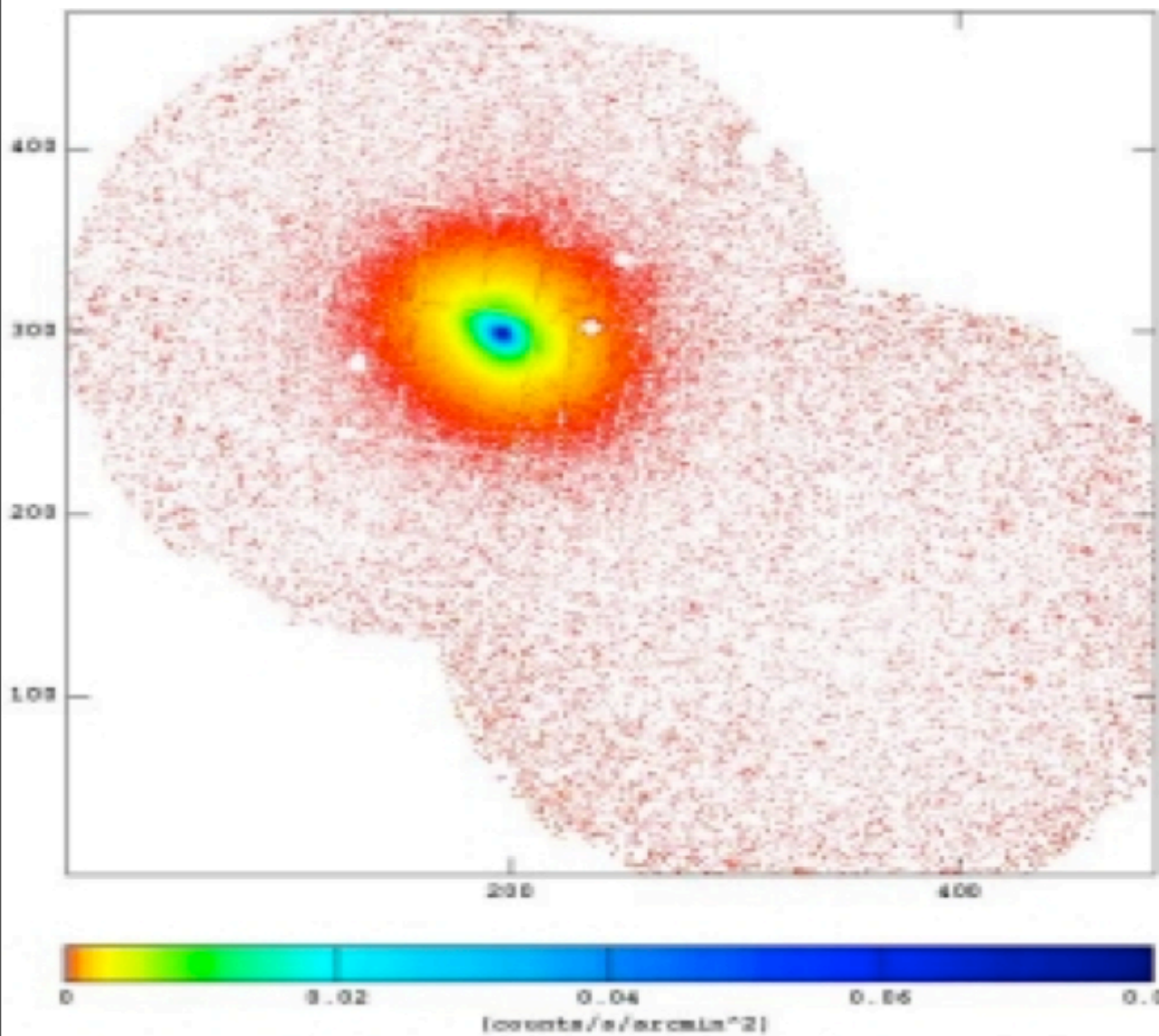


Simulated density profiles



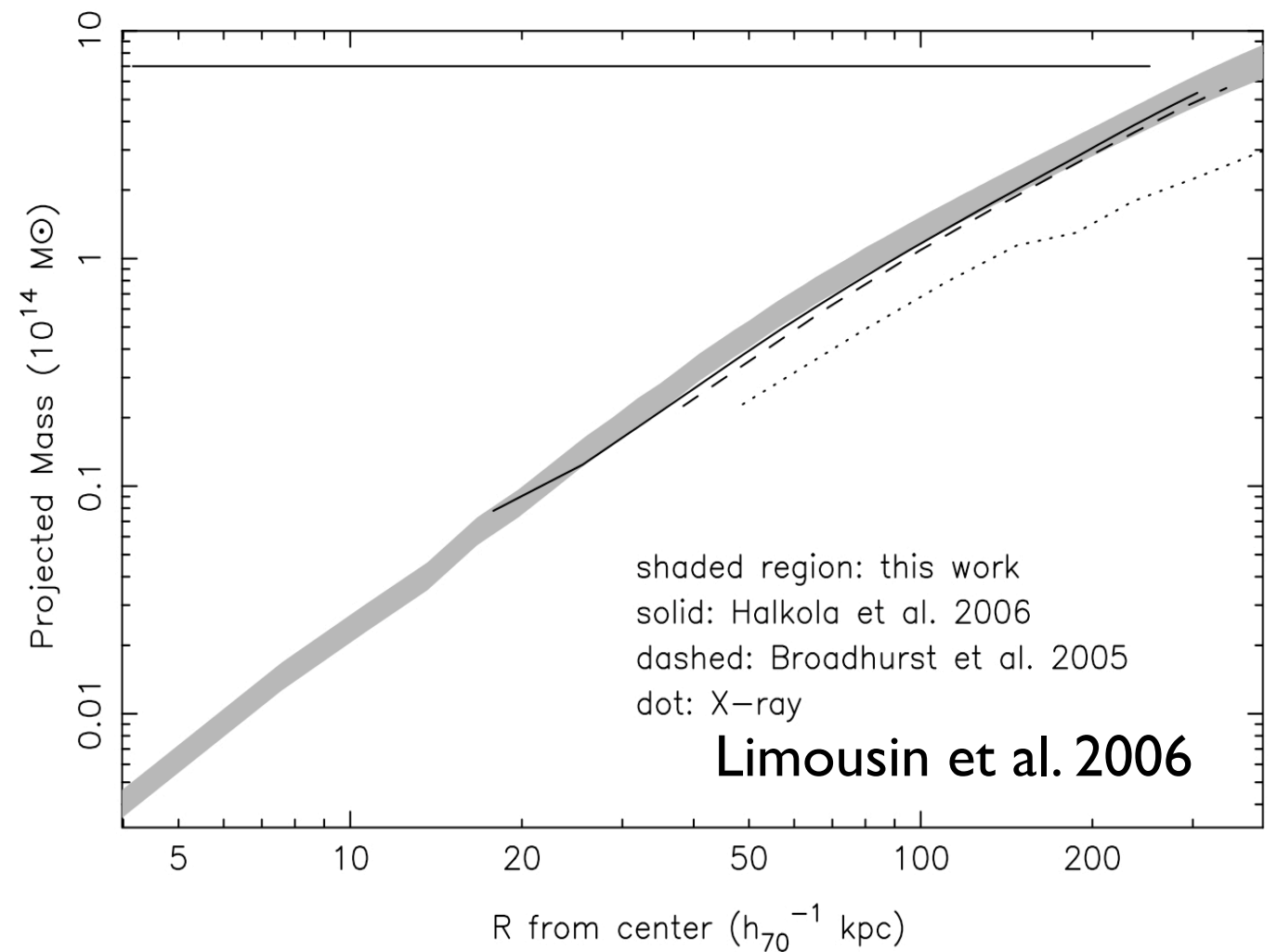
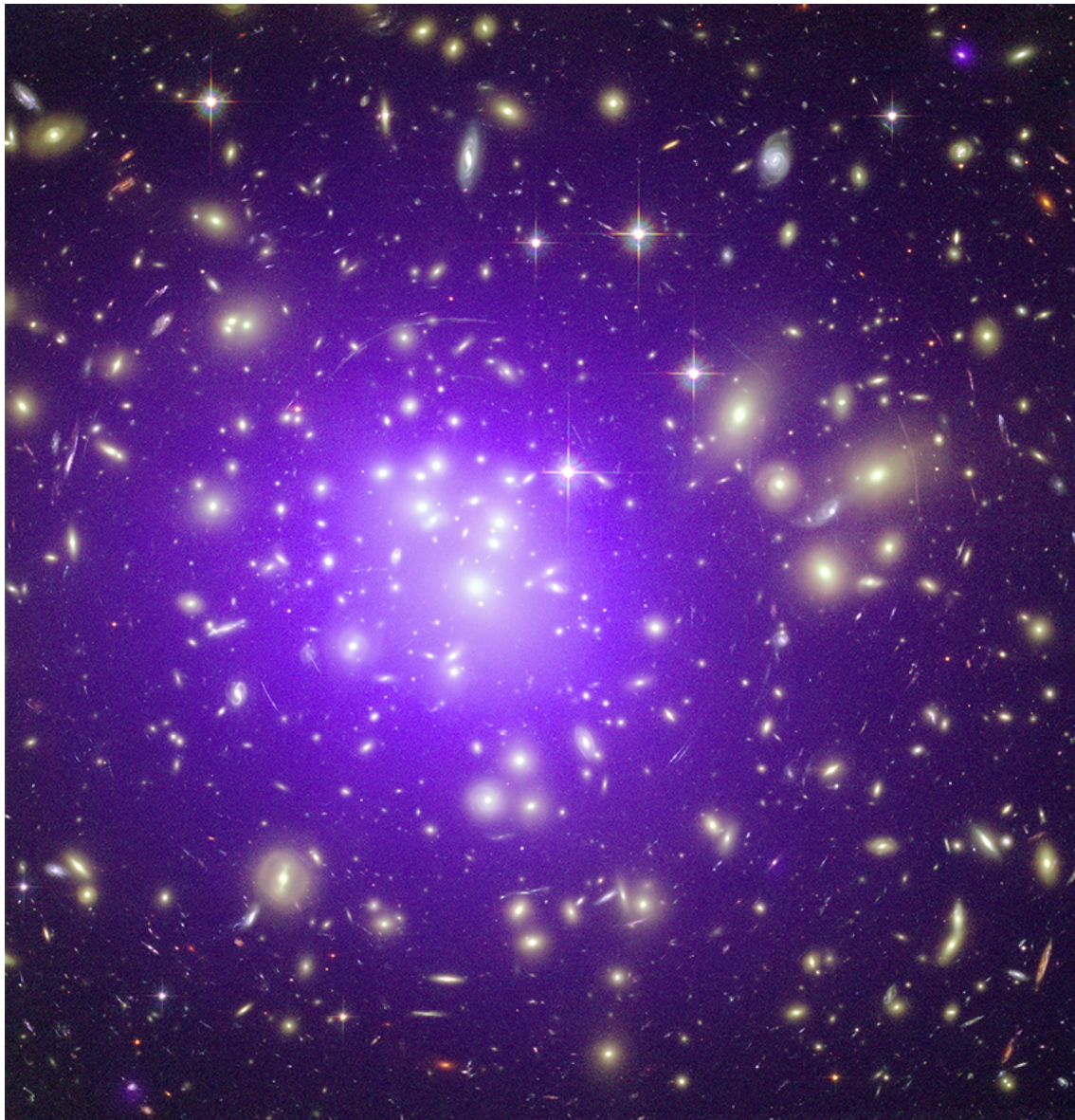
Observed density profile

X-ray observations



Observed density profile

Lensing observations

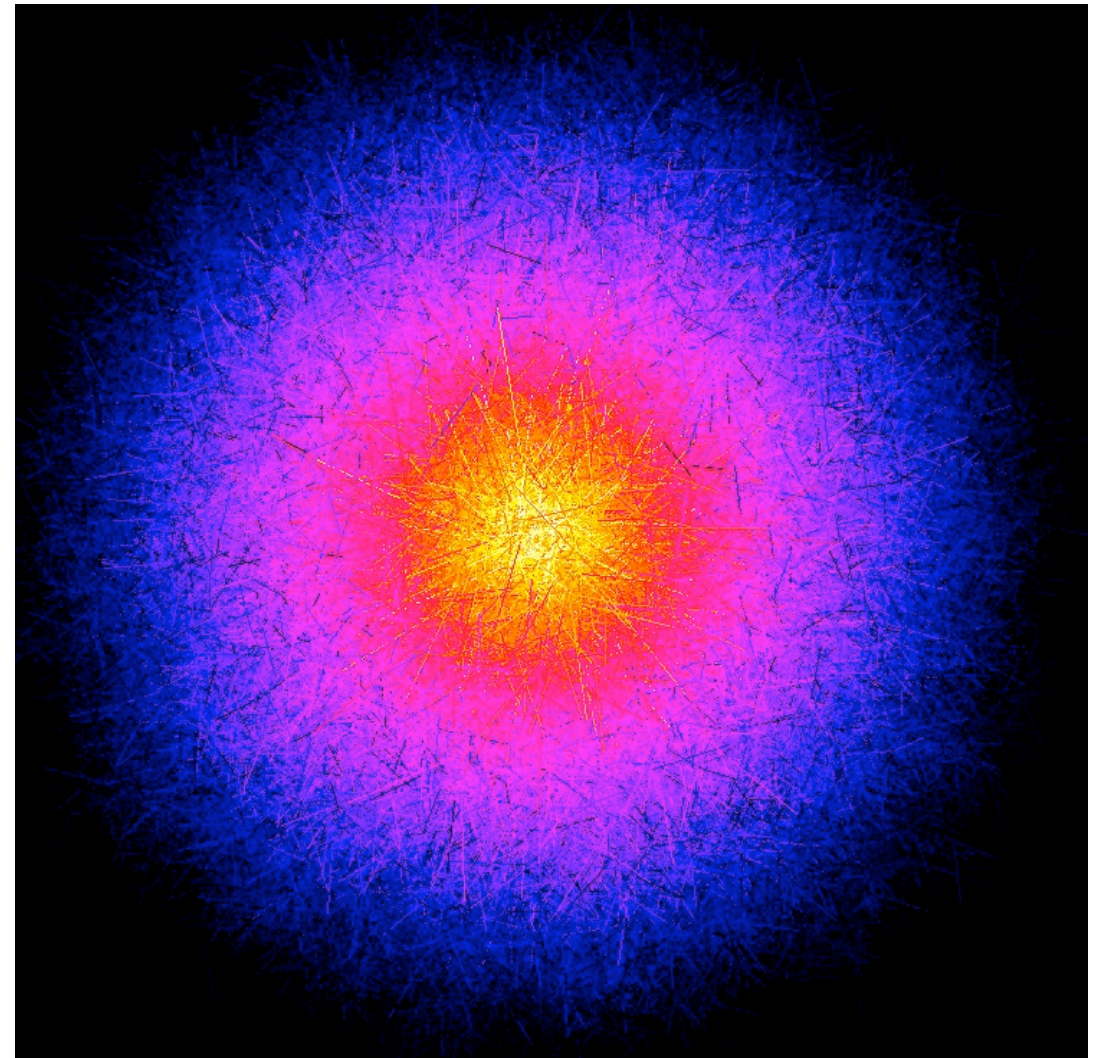


Velocity anisotropy profiles

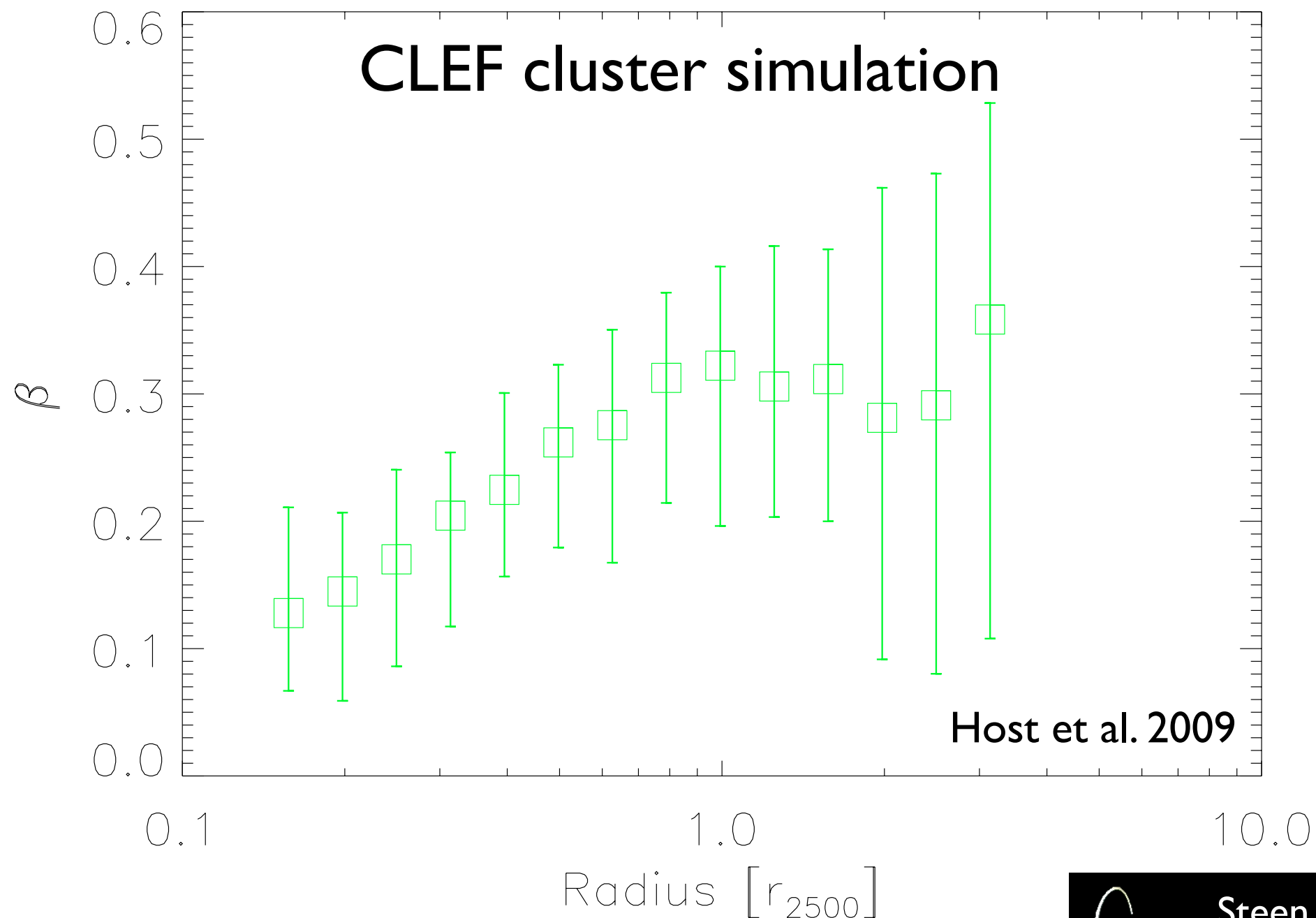
Velocity anisotropy =
different “temperature”
in different directions

$$\beta = 1 - \frac{\sigma_{\text{tan}}^2}{\sigma_{\text{rad}}^2}$$

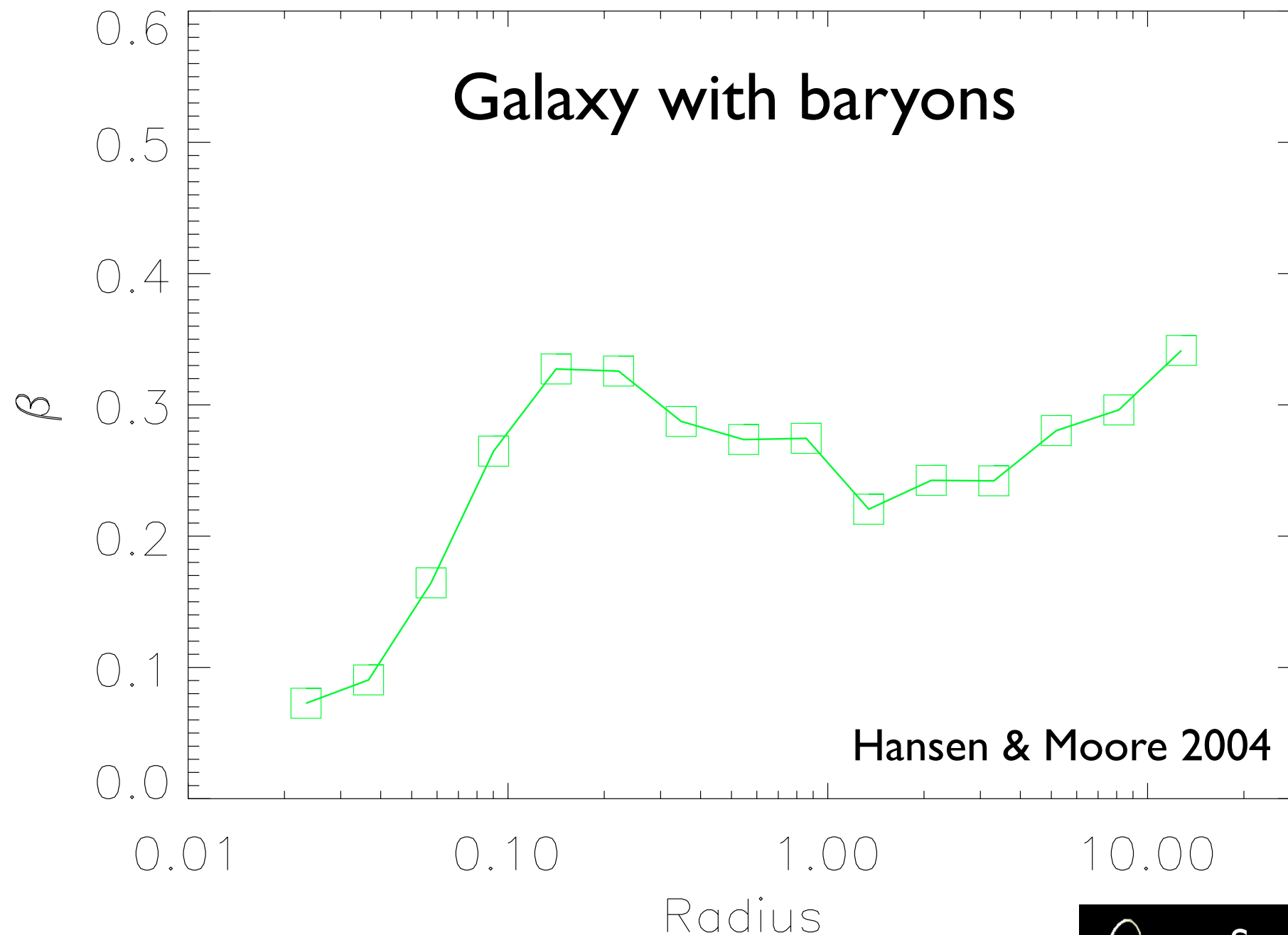
Must be zero for a gas



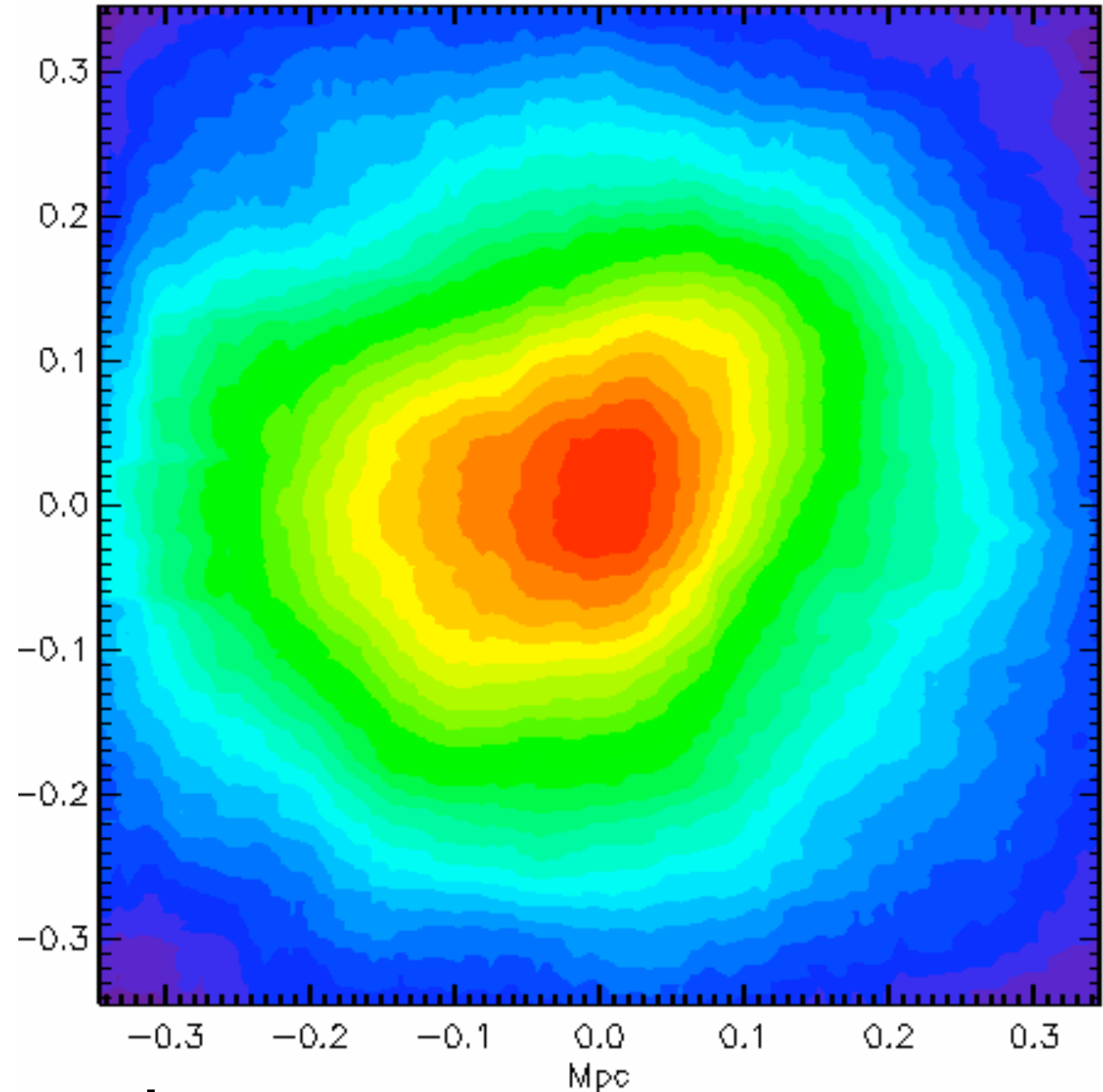
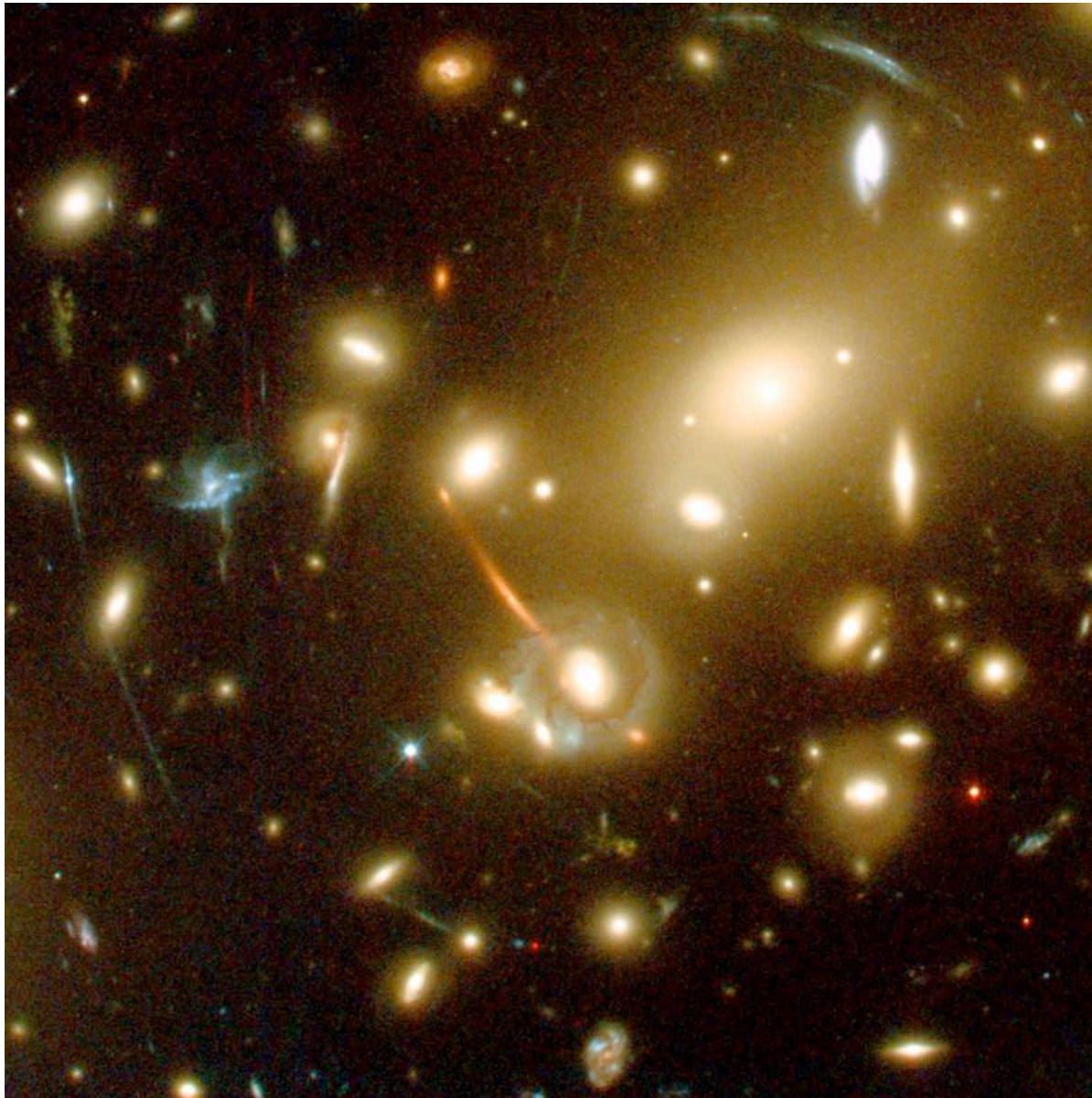
Simulated velocity anisotropy



Simulated velocity anisotropy



Observed velocity anisotropy



Consider an equilibrated galaxy cluster



Steen H. Hansen
Dark Cosmology Centre

Observed velocity anisotropy

Hydrostatic equilibrium (gas)

$$\frac{GM_{\text{tot}}}{r} = -\frac{k_B T}{\mu m_p} \left(\frac{d \ln T}{d \ln r} + \frac{d \ln n_e}{d \ln r} \right)$$

Jeans equation (dark matter)

$$\frac{GM_{\text{tot}}}{r} = -\sigma_r^2 \left(\frac{d \ln \sigma_r^2}{d \ln r} + \frac{d \ln \rho}{d \ln r} + 2\beta \right)$$

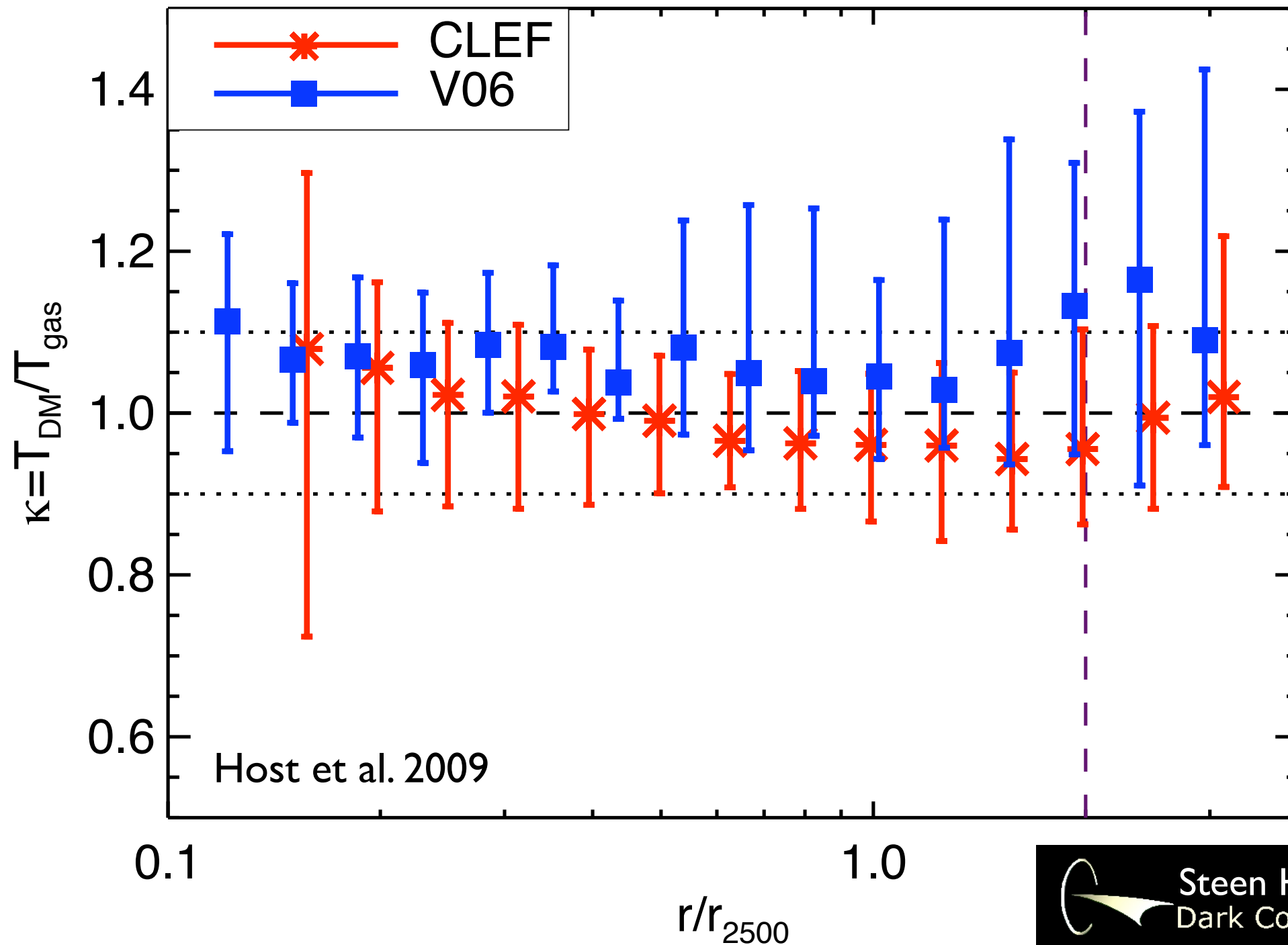
If $\frac{T}{\sigma_{\text{tot}}^2} \approx 1$, then we can solve for β

Hansen & Piffaretti 2007

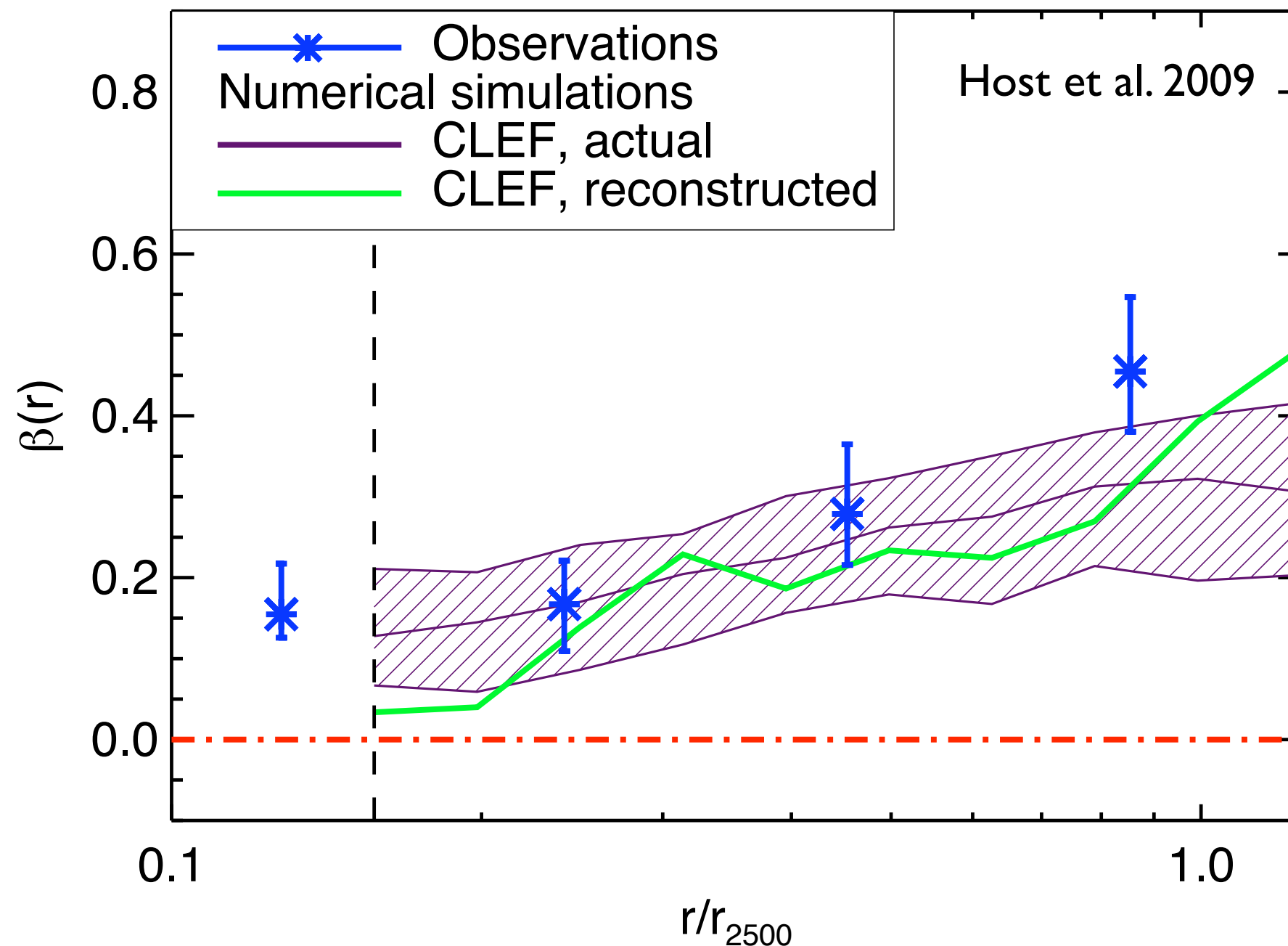


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Observed velocity anisotropy

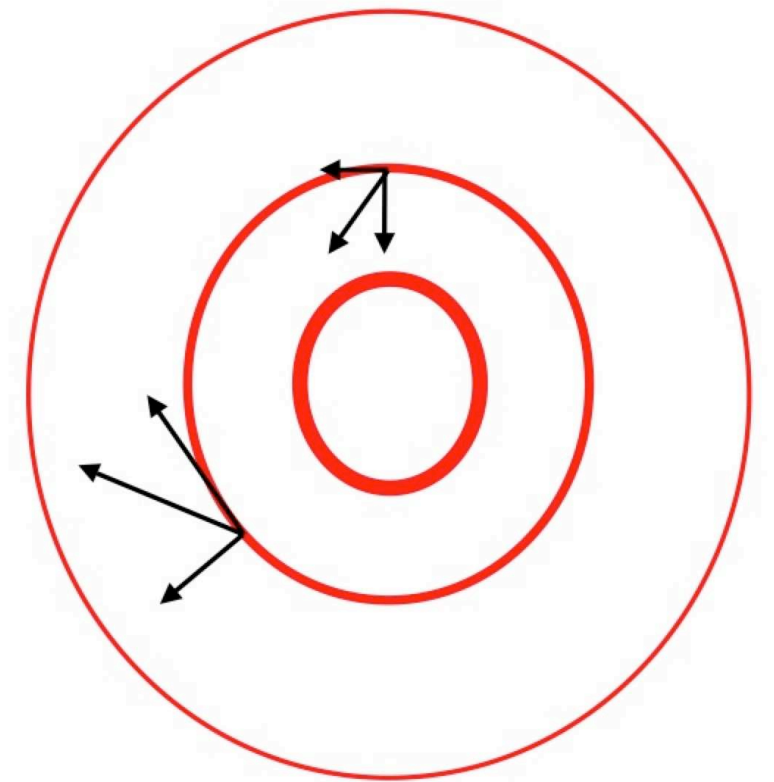
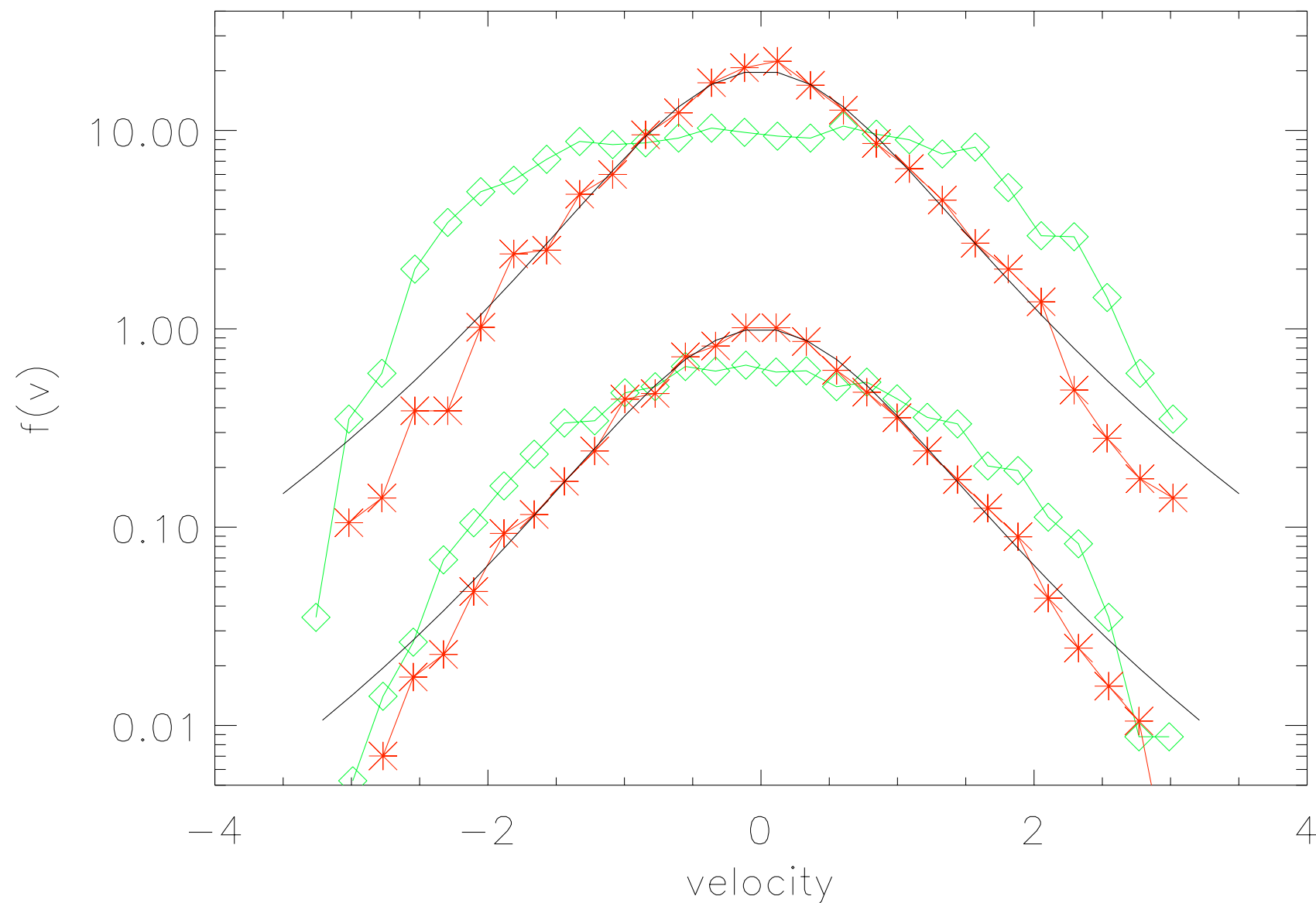


Observed velocity anisotropy

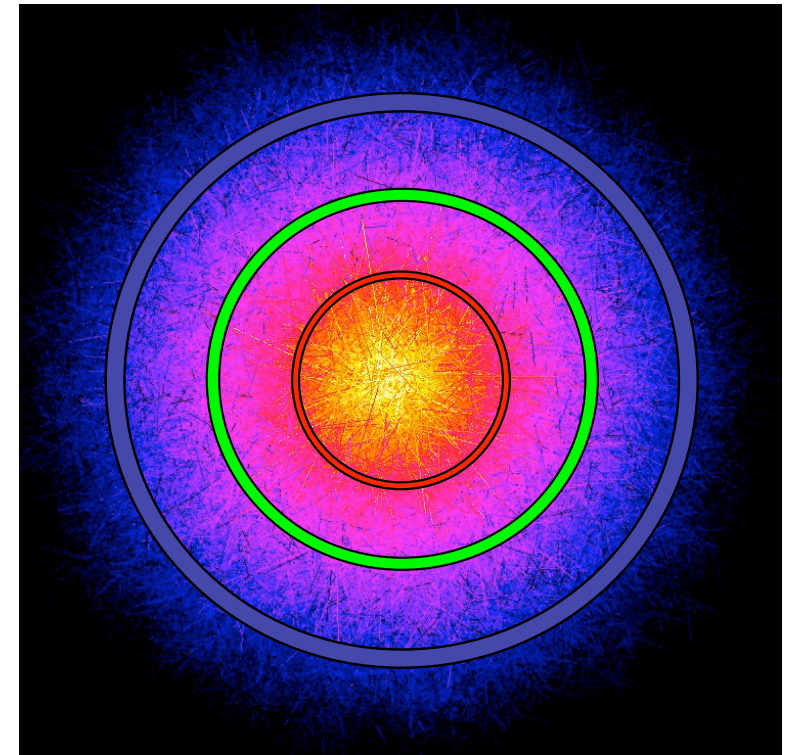
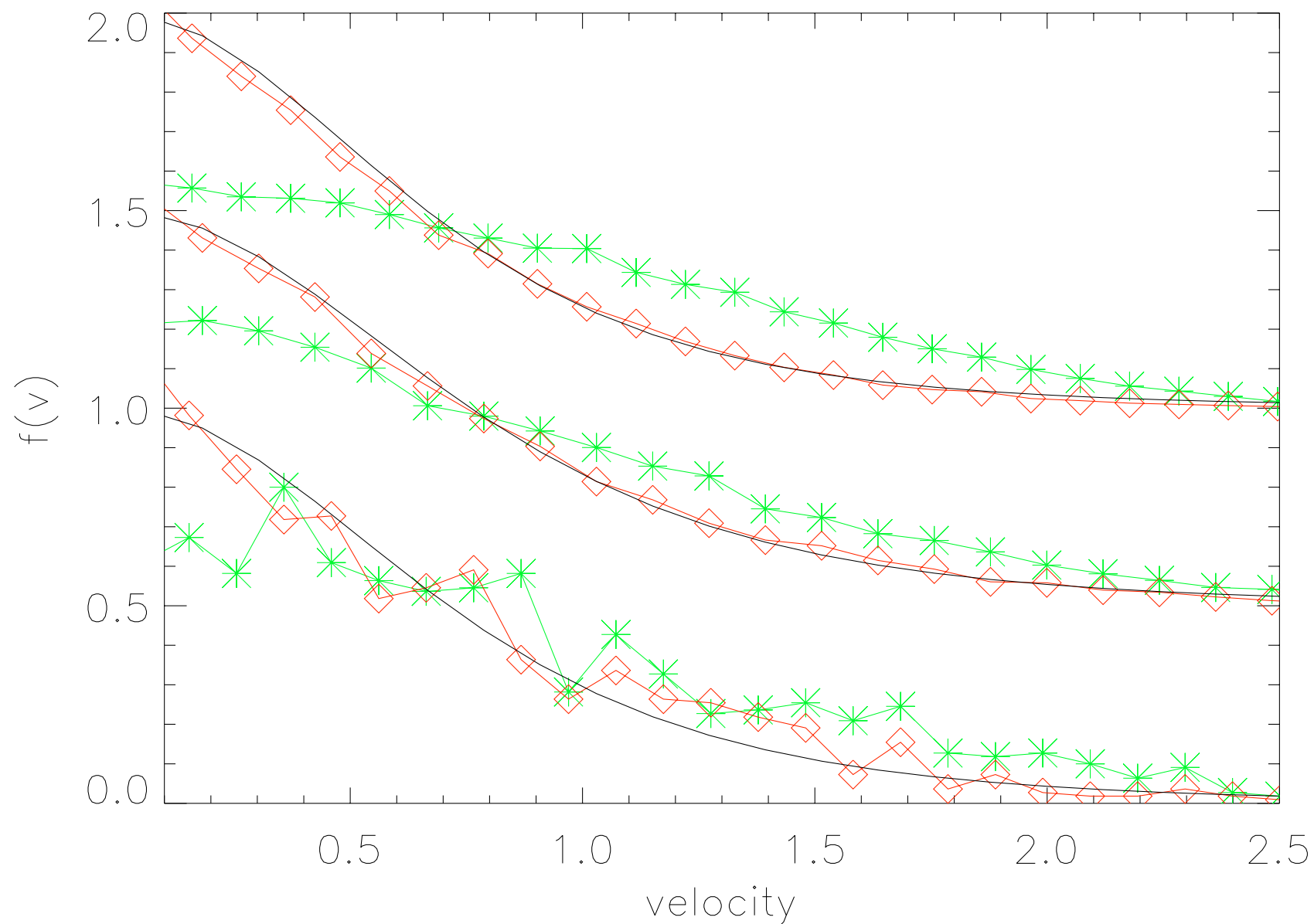


Theoretical velocity anisotropy

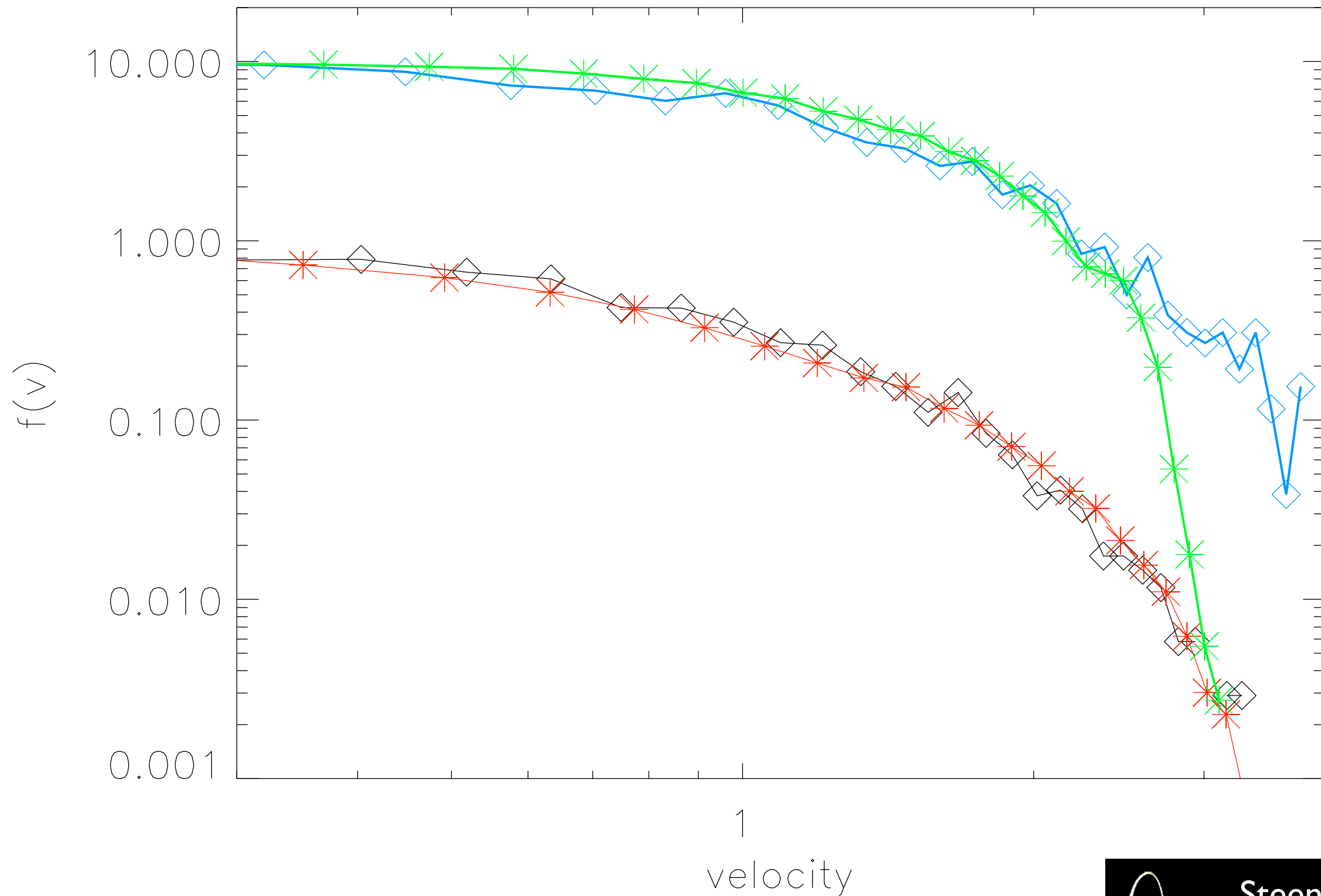
If we understand the velocity distribution function - which is $\exp(-v^2/T)$ for a gas - then we also understand the integrated things like density, velocity dispersions, velocity anisotropy, ...



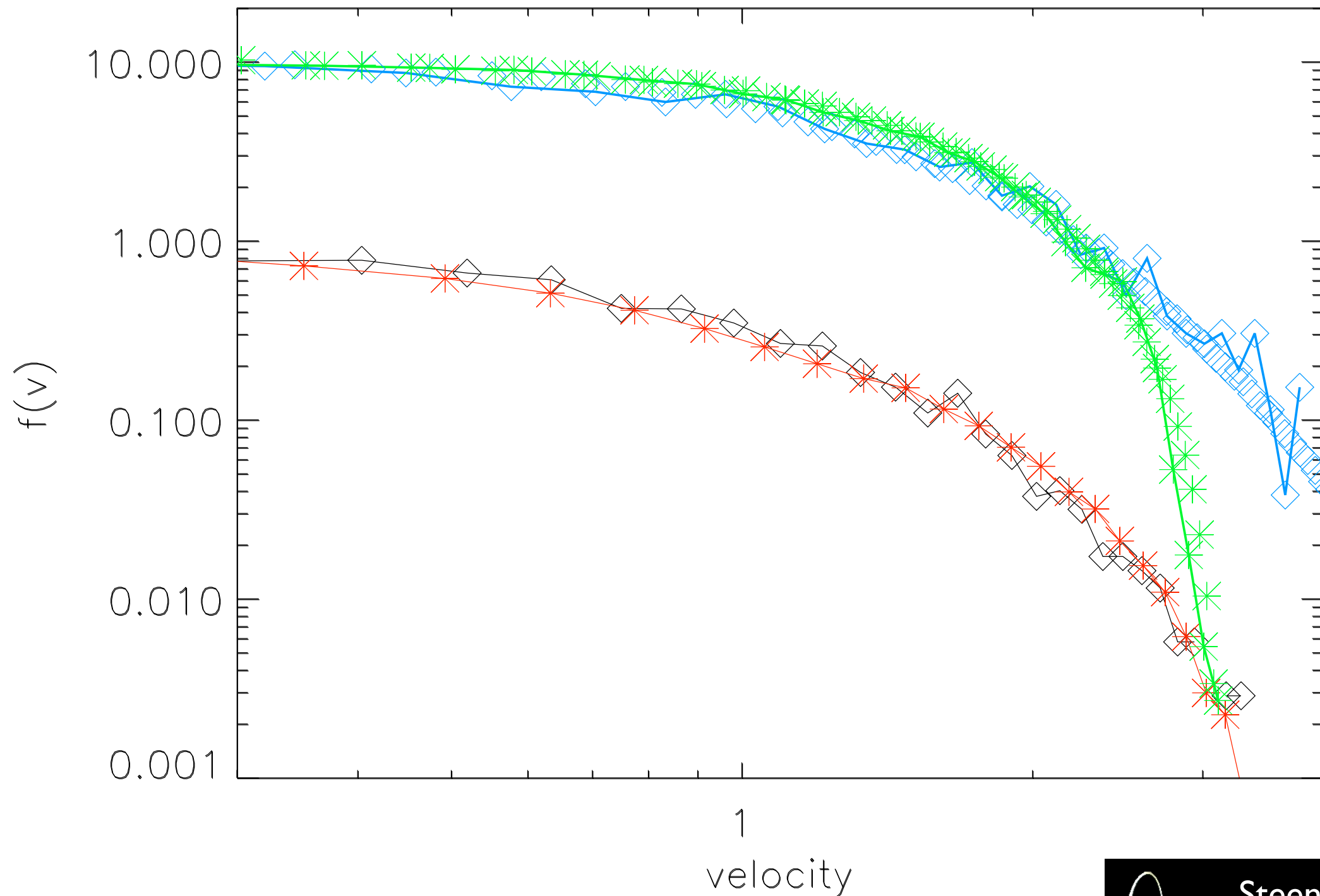
We (almost) know the tangential distribution function



We (almost) know the radial distribution function



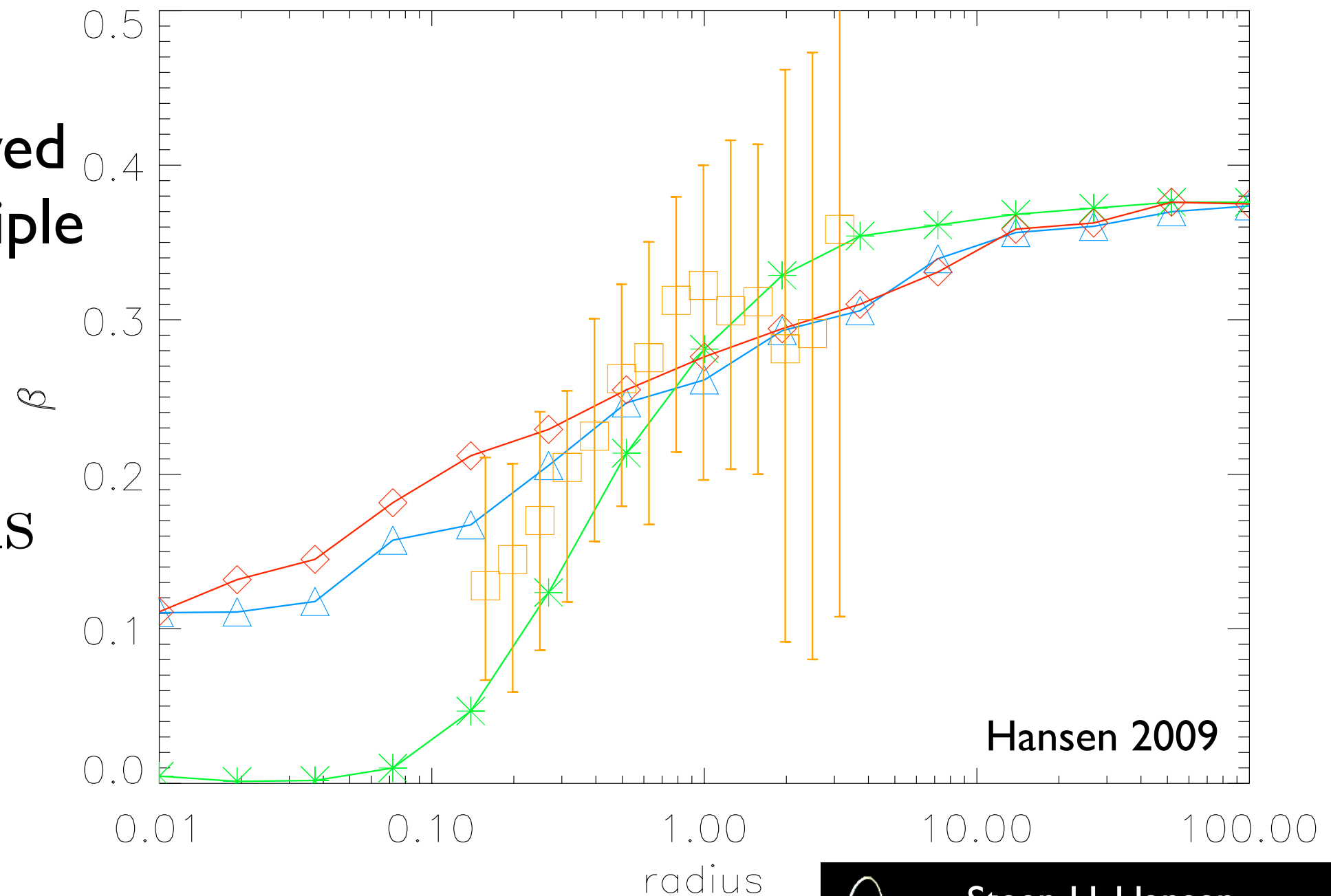
We (almost) know the radial distribution function



Theoretical velocity anisotropy

Analytically derived
from “first” principle

$\beta(r)$ depends
only on $\rho(r)$



Conclusions

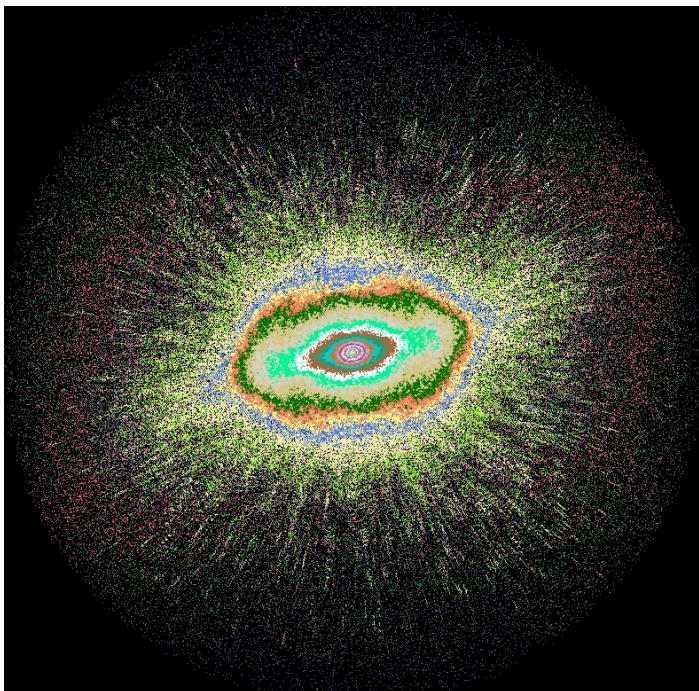
Velocity anisotropy

- 1) Numerical **simulations** show radial variation from about 0 (inner) to about 0.5 (outer)
- 2) First ever **observations** of this dynamical aspect confirm the predicted behavior
- 3) The **analytically** derived velocity anisotropy confirms the magnitude and radial variation
- 4) If this derivation is correct, then the velocity anisotropy is a function only of the density profile. This implies that we can close the Jeans equation



Conclusions - final

We have impressive agreement between numerical simulations, observations and theory concerning the large dark matter structures

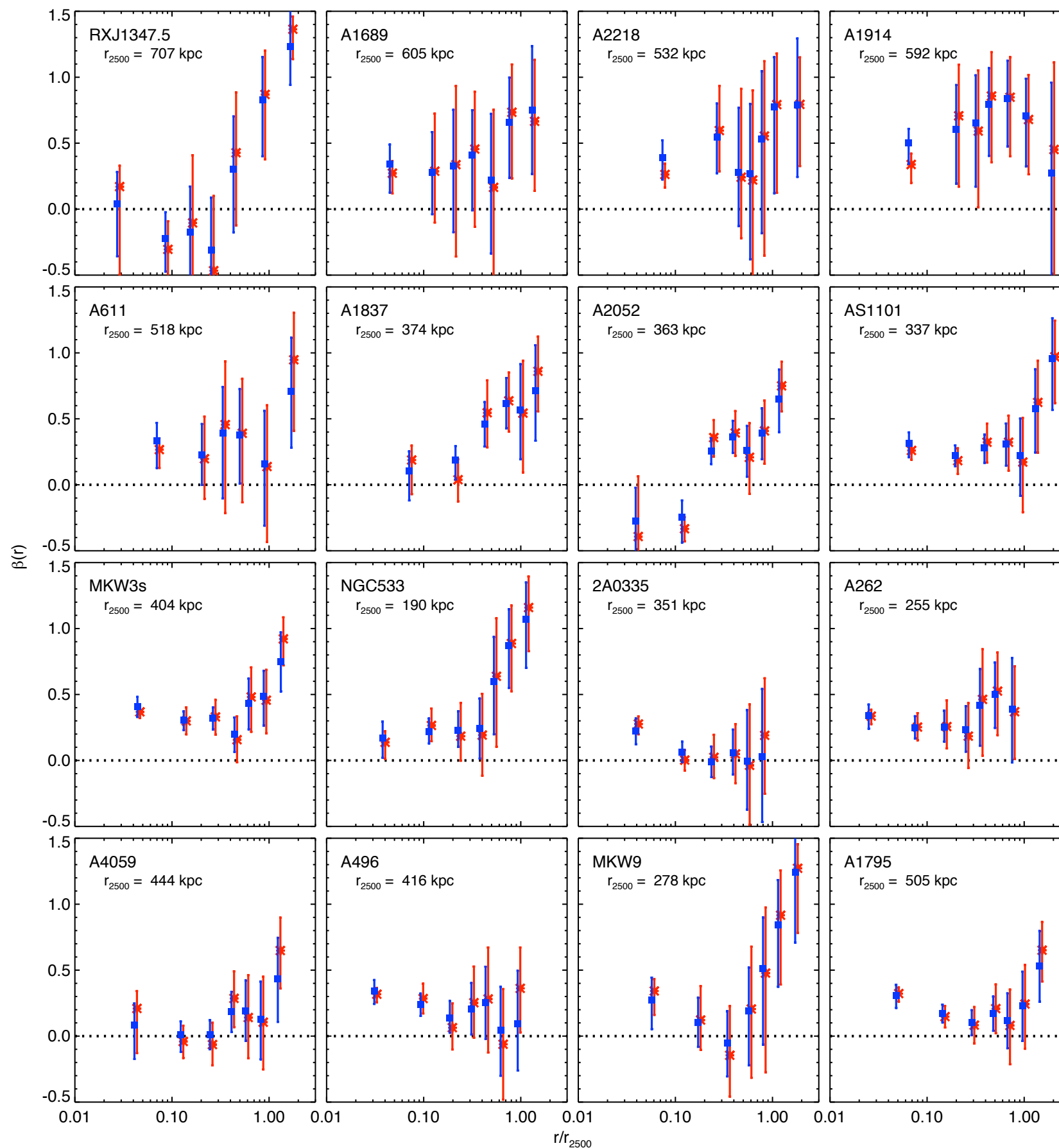


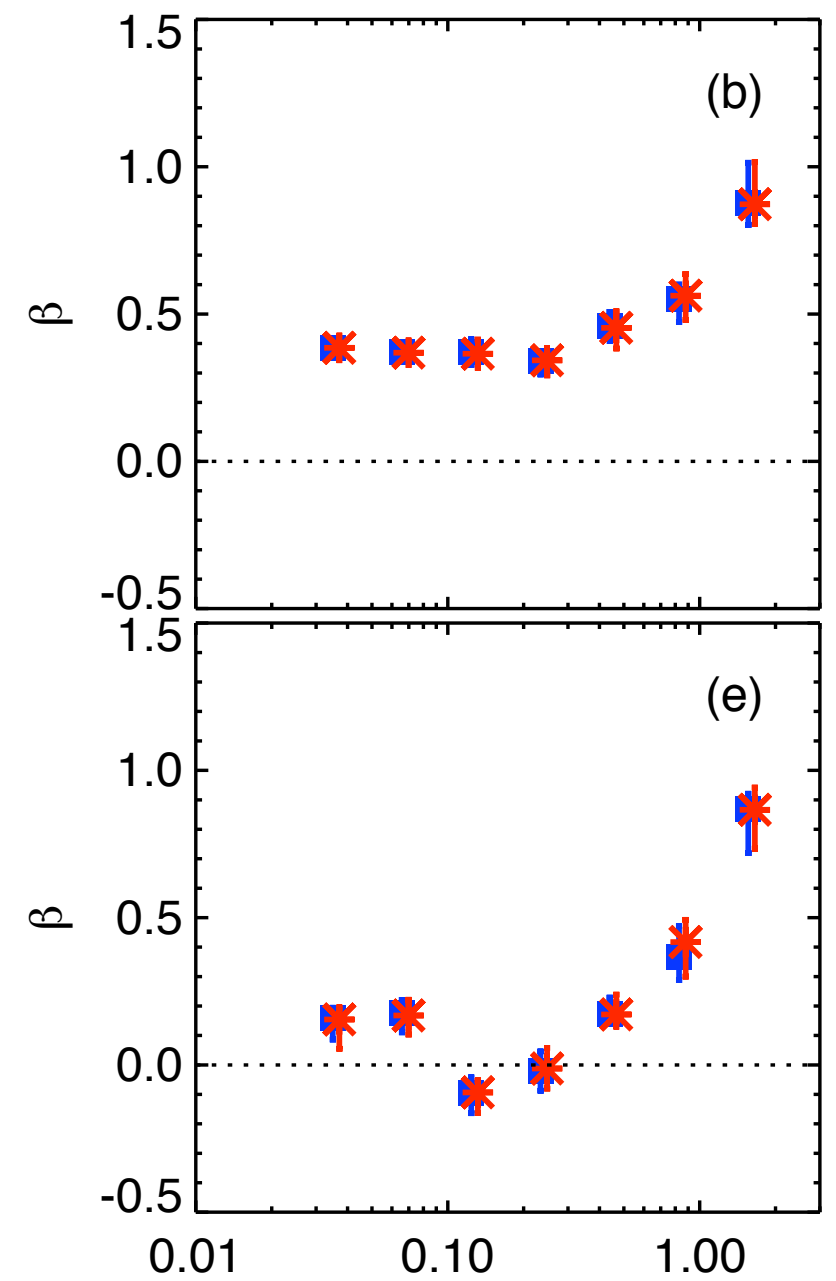
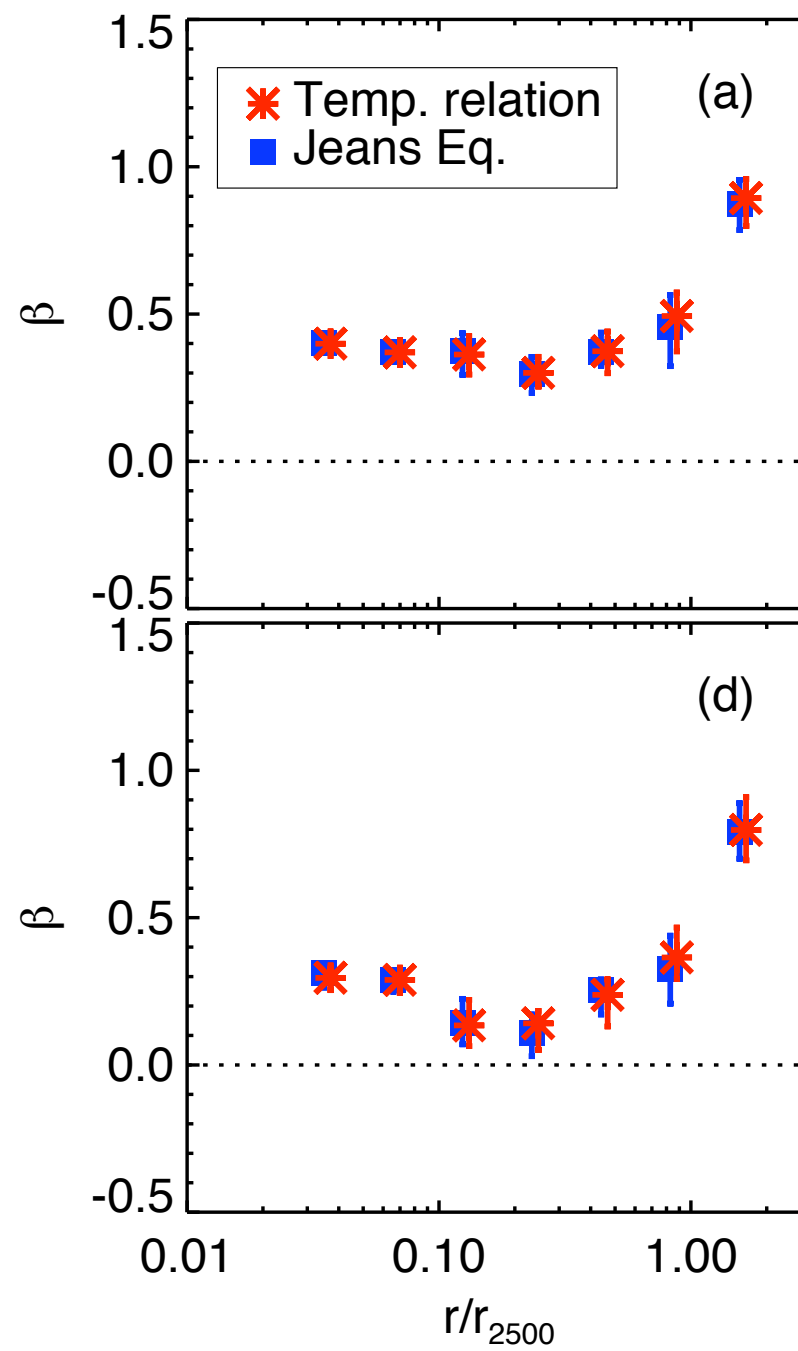
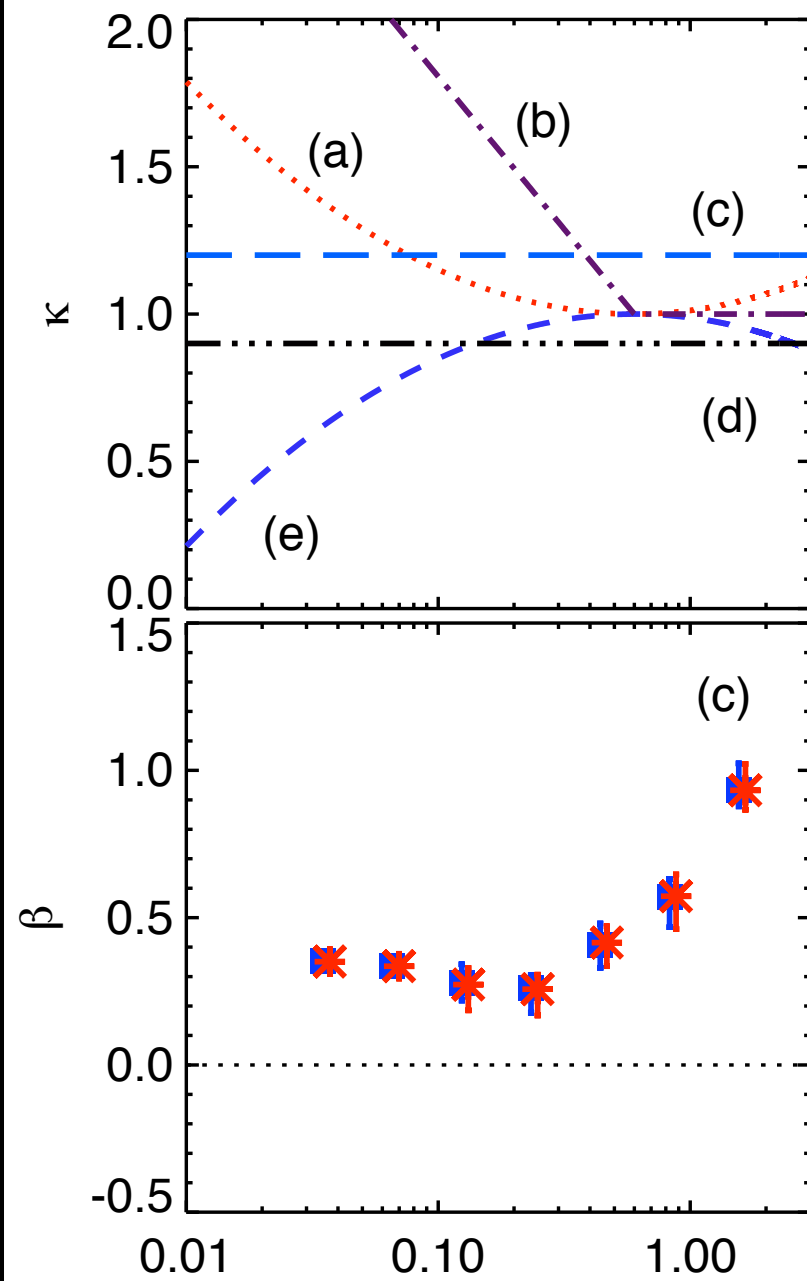
Thank you



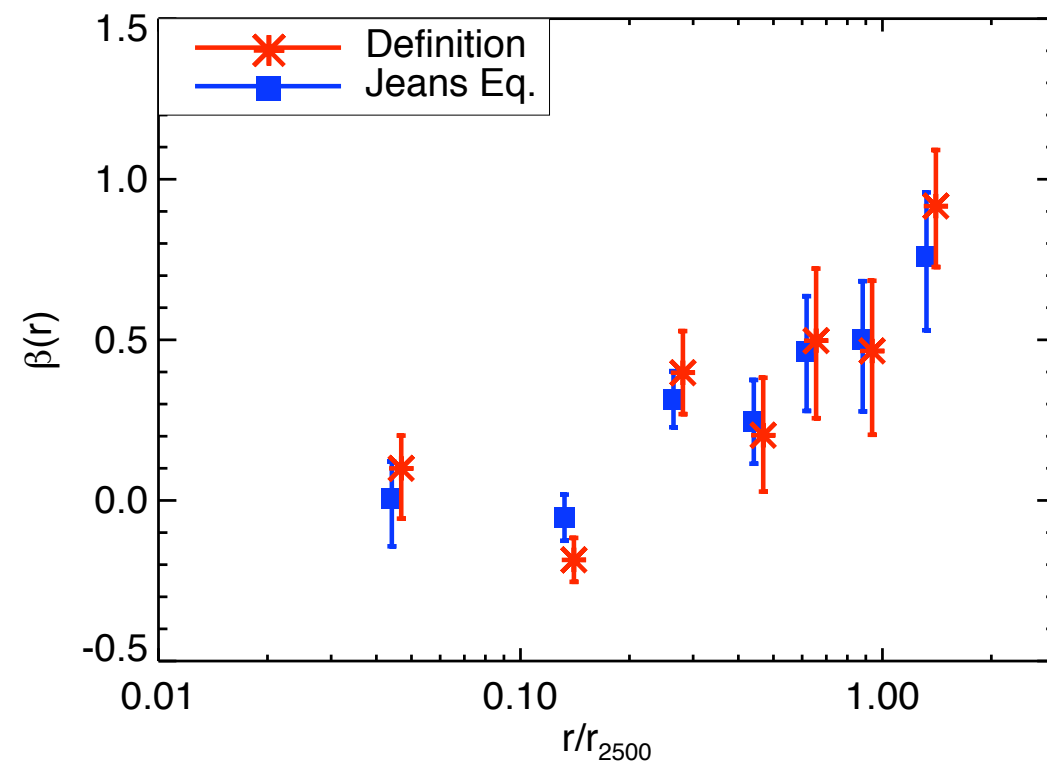
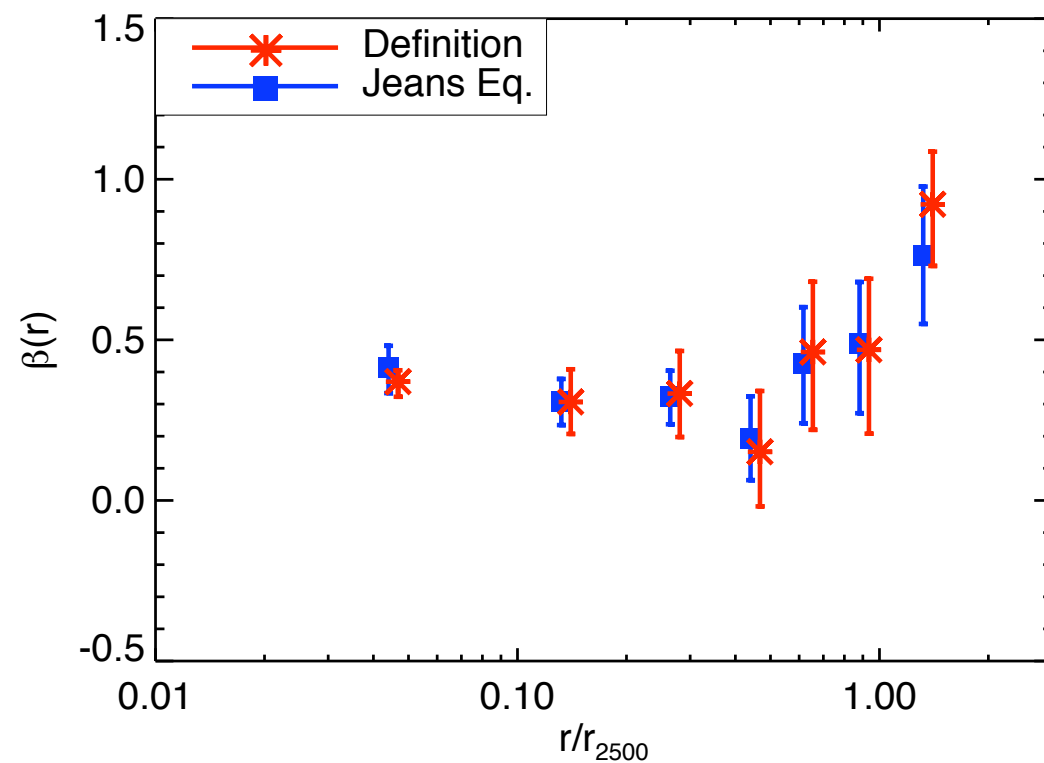
Steen H. Hansen
Dark Cosmology Centre

Extra slides





Stellar density profile?



MKW3s - $r_{2500} = 404$ kpc



Testing in numerical simulations

