

# Spontaneous electromagnetic superconductivity **of vacuum** induced by (very) strong magnetic field

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**Based on:**

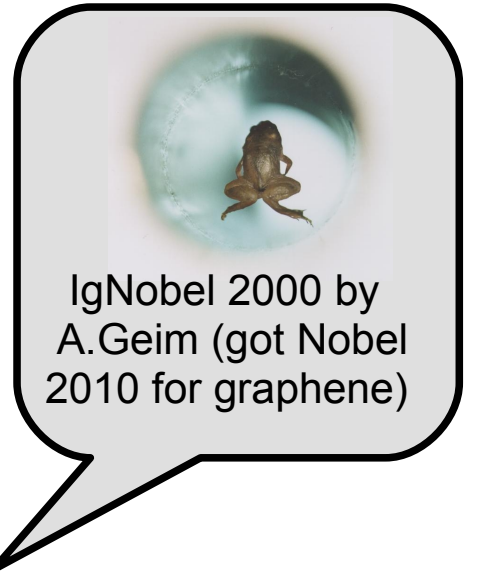
**M.Ch., Phys. Rev. D 82, 085011 (2010) [arXiv:1008.1055]**

**M.Ch., Phys. Rev. Lett. 106, 142003 (2011) [arXiv:1101.0117]**

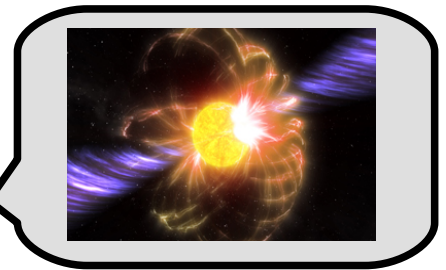
**J. Van Doorselaere, H. Verschelde, M.Ch.,  
Phys. Rev. D 85, 045002 (2012) [arXiv:1111.4401]  
+ arXiv:1104.3767 + arXiv:1104.4404 + ...**

# What is «very strong» field? Typical values:

- Thinking — human brain:  $10^{-12}$  Tesla
- Earth's magnetic field:  $10^{-5}$  Tesla
- Refrigerator magnet:  $10^{-3}$  Tesla
- Loudspeaker magnet: 1 Tesla
- Levitating frogs: 10 Tesla
- Strongest field in Lab:  $10^3$  Tesla
- Typical neutron star:  $10^6$  Tesla
- Magnetar:  $10^{7\cdots 9}$  Tesla
- Heavy-ion collisions:  $10^{15}$  Tesla (and higher)
- Early Universe: even (much) higher

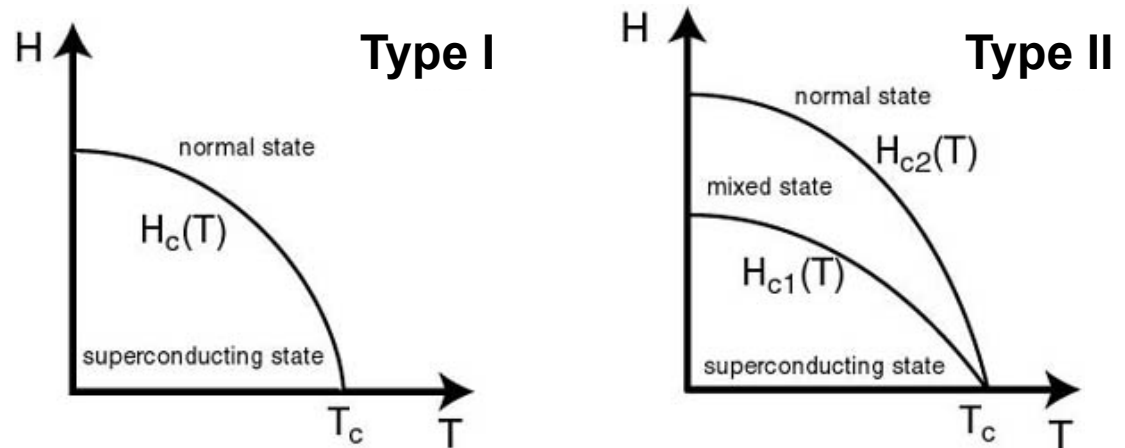
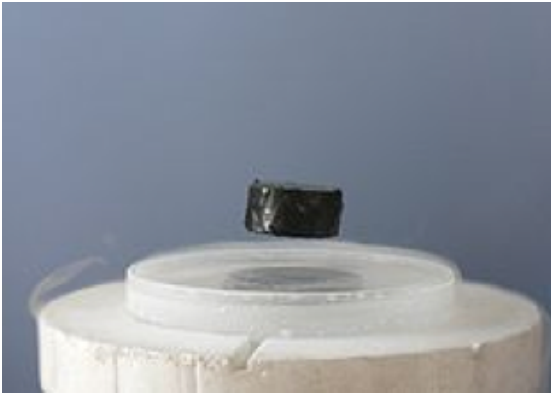


Destructive explosion



# Superconductivity

Discovered by Kamerlingh Onnes at the Leiden University  
100 years ago, at 4:00 p.m. April 8, 1911 (Saturday).



- I. Any superconductor has zero electrical DC resistance
- II. Any superconductor is an enemy of the magnetic field:
  - 1) weak magnetic fields are expelled by all superconductors (the Meissner effect)
  - 2) strong enough magnetic field always kills superconductivity

# Our claim:

**In a background of strong enough magnetic field the vacuum becomes a superconductor.**

**The superconductivity emerges in empty space. Literally, “nothing becomes a superconductor”.**

Some features of the superconducting state of vacuum:

1. spontaneously emerges above the critical magnetic field

$$B_c \approx 10^{16} \text{ Tesla} = 10^{20} \text{ Gauss} \leftarrow \text{can be reached in experiments!}$$

or

$$eB_c \approx m_\rho^2 \approx 31 m_\pi^2 \approx 0.6 \text{ GeV}^2$$

2. conventional Meissner effect does not exist

The claim seemingly contradicts textbooks which state that:

1. Superconductor is a material (= a form of matter, not an empty space)
2. Weak magnetic fields are suppressed by superconductivity
3. Strong magnetic fields destroy superconductivity

# 1+4 approaches to the problem:

0. General arguments; [\(this talk\)](#)
1. Effective bosonic model for electrodynamics of  $\rho$  mesons based on vector meson dominance  
[M.Ch., PRD 2010; arXiv:1008.1055] [\(this talk\)](#)
2. Effective fermionic model (the Nambu-Jona-Lasinio model)  
[M.Ch., PRL 2011; arXiv:1101.0117] ~~[\(this talk\)](#)~~
3. Nonperturbative effective models based on gauge/gravity duality (utilizing AdS/CFT duality)  
[Callebaut, Dudal, Verschelde (Gent U., Belgium), arXiv:1105.2217];  
[Erdmenger, Kerner, Strydom (Munich, Germany), arXiv:1106.4551]  
~~[\(this talk\)](#)~~
5. First-principle numerical simulation of vacuum  
[ITEP Lattice Group, Moscow, Russia, arXiv:1104.3767] [\(this talk\)](#)

# Key players: $\rho$ mesons and vacuum

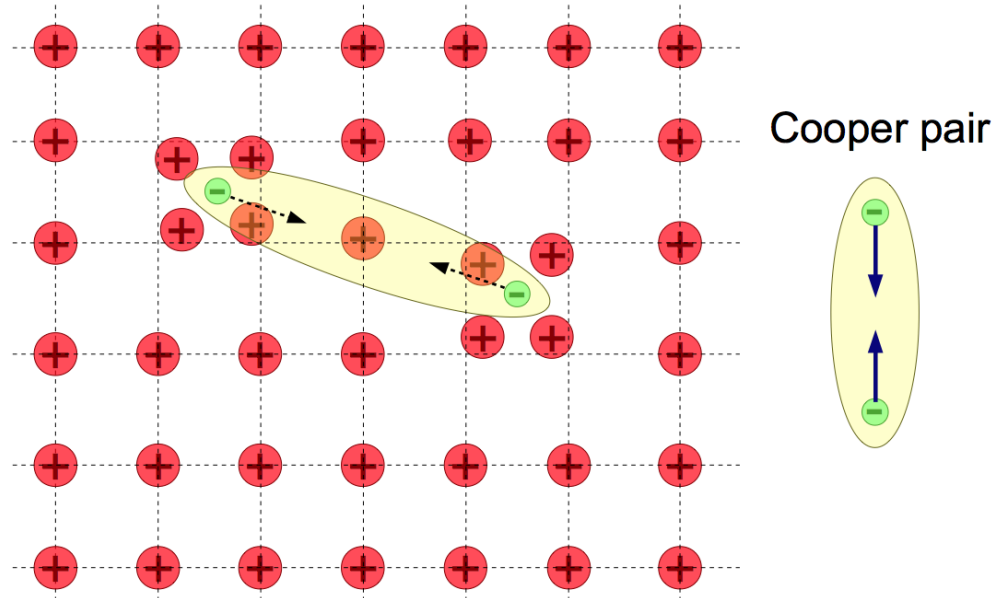
## - $\rho$ mesons:

- electrically charged ( $q = \pm e$ ) and neutral ( $q = 0$ ) particles
- spin:  $s=1$ , vector particles
- quark contents:  $\rho^+ = u\bar{d}$ ,  $\rho^- = d\bar{u}$ ,  $\rho^0 = (u\bar{u} - d\bar{d})/2^{1/2}$
- mass:  $m_\rho = 775.5$  MeV (approximately 1550 electron masses)
- lifetime:  $\tau_\rho = 1.35$  fm/ $c$  (very short: size of the  $\rho$  meson is 0.5 fm)

## - vacuum: QED+QCD, zero temperature and density

# Conventional BCS superconductivity

- 1) The Cooper pair is the relevant degree of freedom!
- 2) The electrons are bounded into the Cooper pairs by the (attractive) phonon exchange.



Three basic ingredients:

- A) the presence of carriers of electric charge (of electric current);
- B) the reduction of physics from (3+1) to (1+1) dimensions;
- C) the attractive interaction between the like-charged particles.

# Real vacuum, no magnetic field

## 1) Boiling soup of everything.

Virtual particles and antiparticles (electrons, positrons, photons, gluons, quarks, antiquarks ...) are created and annihilated every moment.

## 2) Net electric charge is zero.

An insulator, obviously.

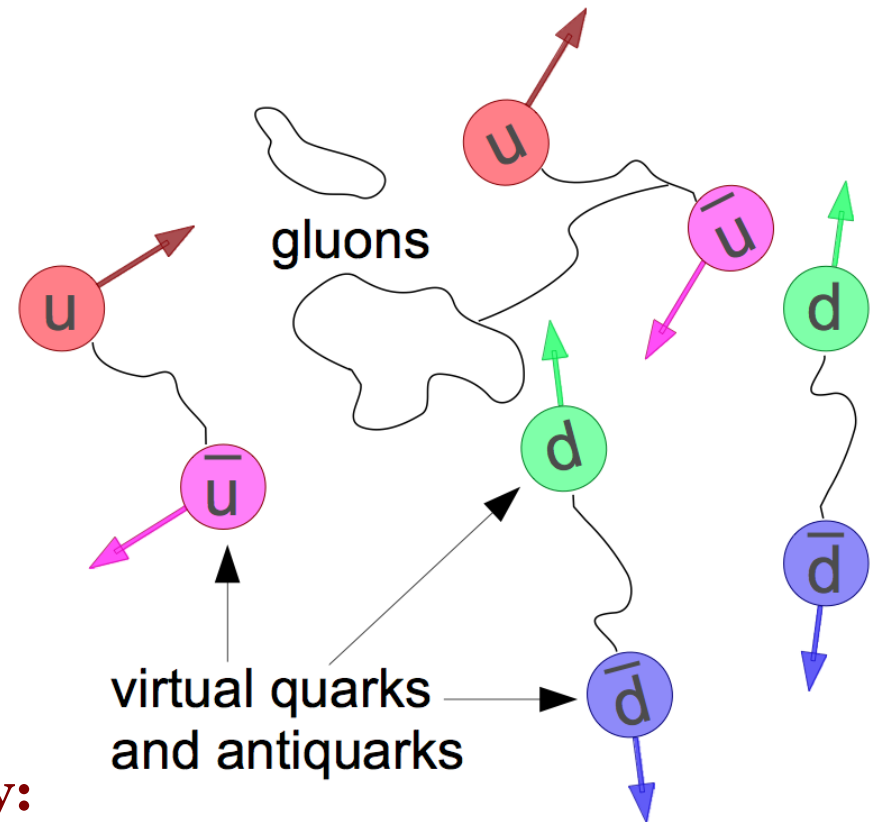
## 3) We are interested in “strongly interacting” sector of the theory:

a) quarks and antiquarks,

i)  $u$  quark has electric charge  $q_u = +2 e/3$

ii)  $d$  quark has electric charge  $q_d = - e/3$

b) gluons (an analogue of photons, no electric charge) “glue” quarks into bound states, “hadrons” (neutrons, protons, etc).





# The vacuum in strong magnetic field

Ingredients needed for possible superconductivity:

A. **Presence of electric charges?**

**Yes**, we have them: there are virtual particles which may potentially become “real” (= pop up from the vacuum) and make the vacuum (super)conducting.

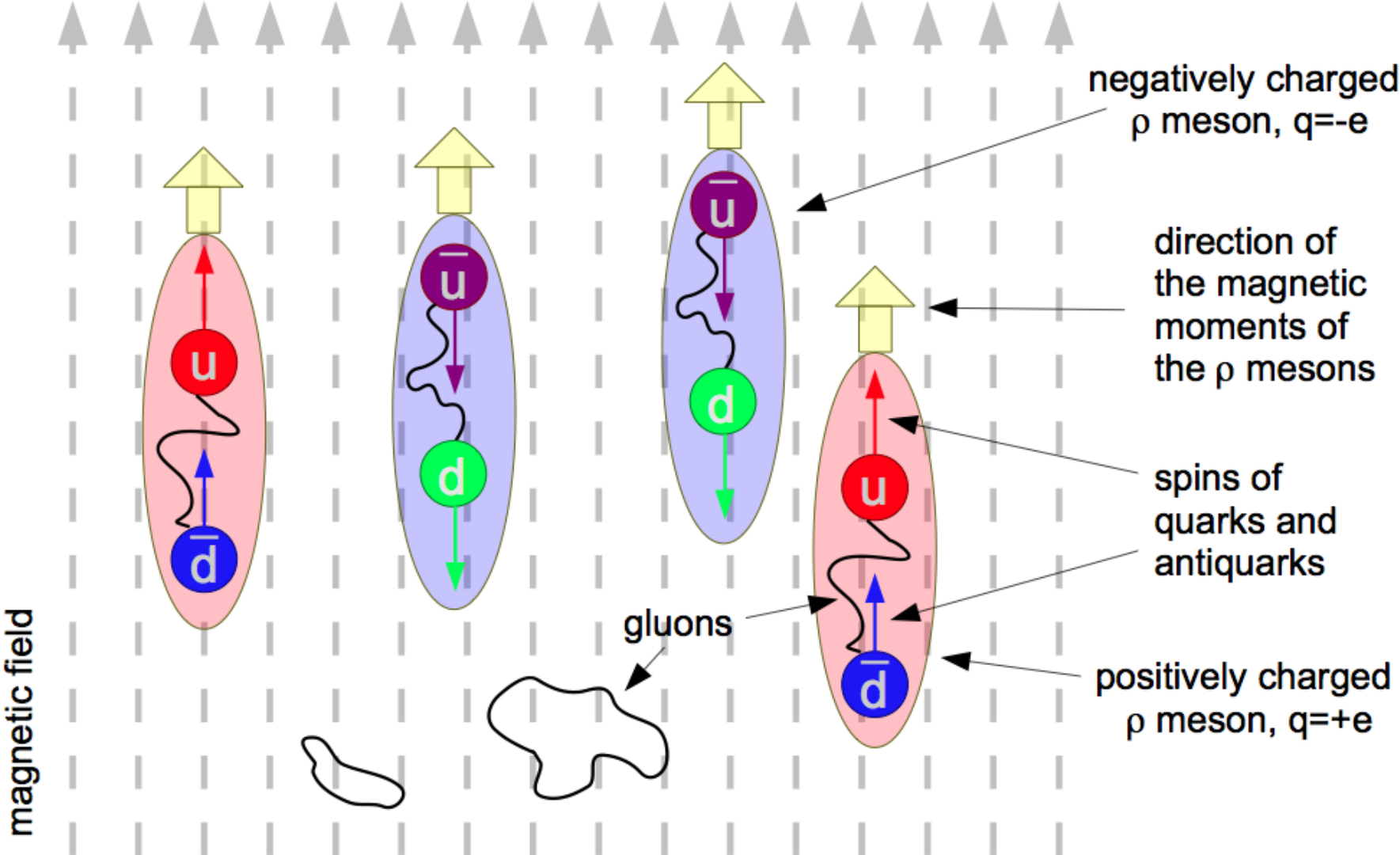
B. **Reduction to 1+1 dimensions?**

**Yes**, we have this phenomenon: in a very strong magnetic field the dynamics of electrically charged particles (quarks, in our case) becomes effectively one-dimensional, because the particles tend to move along the magnetic field only.

C. **Attractive interaction between the like-charged particles?**

**Yes**, we have it: the gluons provide attractive interaction between the quarks and antiquarks ( $q_u = +2 e/3$  and  $q_{\bar{d}} = +e/3$ )

# Strong magnetic field, picture



# Charged relativistic particles in magnetic field

- Energy of a relativistic particle in the external magnetic field  $B_{\text{ext}}$ :

$$\varepsilon_{n,s_z}^2(p_z) = p_z^2 + (2n - 2s_z + 1)eB_{\text{ext}} + m^2$$

momentum along  
the magnetic field axis
nonnegative integer number
projection of spin on  
the magnetic field axis

(the external magnetic field is directed along the z-axis)

- Masses of  $\rho$  mesons and pions in the external magnetic field

$$m_{\pi^\pm}^2(B_{\text{ext}}) = m_{\pi^\pm}^2 + eB_{\text{ext}} \quad \text{becomes heavier}$$

$$m_{\rho^\pm}^2(B_{\text{ext}}) = m_{\rho^\pm}^2 - eB_{\text{ext}} \quad \text{becomes lighter}$$

$$\rho^\pm \rightarrow \pi^\pm \pi^0$$

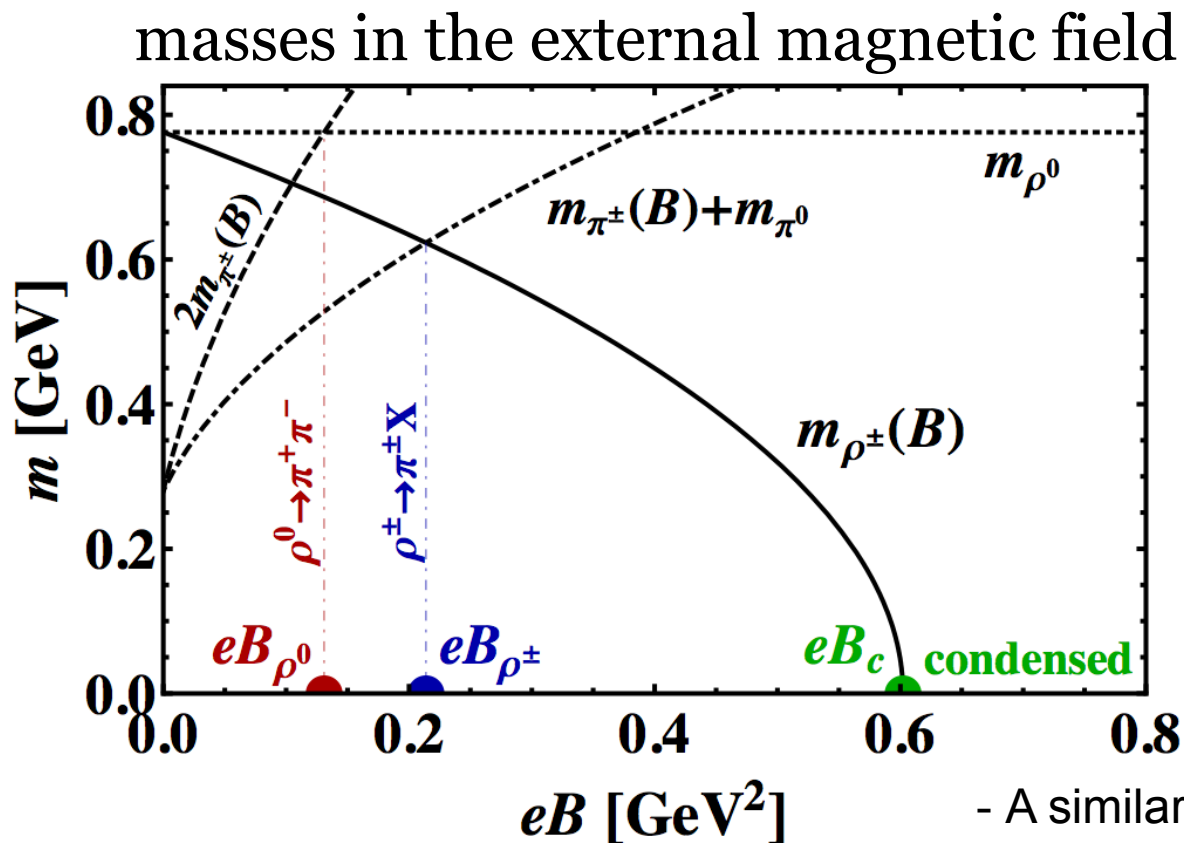
- Masses of  $\rho$  mesons and pions:

$$m_\pi = 139.6 \text{ MeV}, \quad m_\rho = 775.5 \text{ MeV}$$

# Condensation of $\rho$ mesons

The  $\rho^\pm$  mesons become massless and condense at the critical value of the external magnetic field

$$B_c = \frac{m_\rho^2}{e} \approx 10^{16} \text{ Tesla}$$



**Kinematical impossibility of dominant decay modes**

The pion becomes heavier while the rho meson becomes lighter

- The decay  $\rho^\pm \rightarrow \pi^\pm \pi^0$  stops at certain value of the magnetic field

$$m_{\rho^\pm}(B_{\rho^\pm}) = m_{\pi^\pm}(B_{\rho^\pm}) + m_{\pi^0}$$

- A similar statement is true for  $\rho^0 \rightarrow \pi^+ \pi^-$

# Electrodynamics of $\rho$ mesons

- Lagrangian (based on vector dominance models):

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{1}{2} \rho_{\mu\nu}^\dagger \rho^{\mu\nu} + m_\rho^2 \rho_\mu^\dagger \rho^\mu - \frac{1}{4} \rho_{\mu\nu}^{(0)} \rho^{(0)\mu\nu} + \frac{m_\rho^2}{2} \rho_\mu^{(0)} \rho^{(0)\mu} + \frac{e}{2g_s} F^{\mu\nu} \rho_{\mu\nu}^{(0)}$$

**Nonminimal coupling leads to  $g=2$**

- Tensor quantities

$$\begin{aligned} F_{\mu\nu} &= \partial_\mu A_\nu - \partial_\nu A_\mu, \\ f_{\mu\nu}^{(0)} &= \partial_\mu \rho_\nu^{(0)} - \partial_\nu \rho_\mu^{(0)}, \\ \rho_{\mu\nu}^{(0)} &= f_{\mu\nu}^{(0)} - ig_s (\rho_\mu^\dagger \rho_\nu - \rho_\mu \rho_\nu^\dagger) \\ \rho_{\mu\nu} &= D_\mu \rho_\nu - D_\nu \rho_\mu, \end{aligned}$$

- Gauge invariance

$$U(1) : \begin{cases} \rho_\mu^{(0)}(x) \rightarrow \rho_\mu^{(0)}(x), \\ \rho_\mu(x) \rightarrow e^{i\omega(x)} \rho_\mu(x), \\ A_\mu(x) \rightarrow A_\mu(x) + \partial_\mu \omega(x) \end{cases}$$

- Covariant derivative

$$D_\mu = \partial_\mu + ig_s \rho_\mu^{(0)} - ie A_\mu$$

- Kawarabayashi-Suzuki-Riadzuddin-Fayyazuddin relation

$$g_s \equiv g_{\rho\pi\pi} = \frac{m_\rho}{\sqrt{2}f_\pi} = 5.88$$

$$g_s \gg e \equiv \sqrt{4\pi\alpha_{\text{e.m.}}} \approx 0.303$$

# Homogeneous approximation

- Energy density:  $\epsilon \equiv T_{00} = \frac{1}{2}F_{0i}^2 + \frac{1}{4}F_{ij}^2 + \frac{1}{2}(\rho_{0i}^{(0)})^2 + \frac{1}{4}(\rho_{ij}^{(0)})^2$   
 $+ \frac{m_\rho^2}{2} [(\rho_0^{(0)})^2 + (\rho_i^{(0)})^2] + \rho_{0i}^\dagger \rho_{0i} + \frac{1}{2}\rho_{ij}^\dagger \rho_{ij}$   
 $+ m_\rho^2(\rho_0^\dagger \rho_0 + \rho_i^\dagger \rho_i) - \frac{e}{g_s} F_{0i} \rho_{0i}^{(0)} - \frac{e}{2g_s} F_{ij} \rho_{ij}^{(0)}$

- Disregard kinetic terms (for a moment) and apply  $B_{\text{ext}}$ :

$$\begin{aligned} \epsilon_0^{(2)}(\rho_\mu) &= ieB_{\text{ext}}(\rho_1^\dagger \rho_2 - \rho_2^\dagger \rho_1) + m_\rho^2 \rho_\mu^\dagger \rho_\mu \\ &= \sum_{a,b=1}^2 \rho_a^\dagger \mathcal{M}_{ab} \rho_b + m_\rho^2(\rho_0^\dagger \rho_0 + \rho_3^\dagger \rho_3) \end{aligned}$$

mass matrix  $\nearrow$

$$\mathcal{M} = \begin{pmatrix} m_\rho^2 & ieB_{\text{ext}} \\ -ieB_{\text{ext}} & m_\rho^2 \end{pmatrix}$$

$$\vec{B} = (0, 0, B)$$

- Eigenvalues and eigenvectors of the mass matrix:

$$\mu_\pm^2 = m_\rho^2 \pm eB_{\text{ext}}, \quad \rho_\pm = \frac{1}{\sqrt{2}}(\rho_1 \pm i\rho_2)$$

At the critical value of the magnetic field: imaginary mass (=condensation)!

# Homogeneous approximation (II)

- The condensate of the rho mesons:  $\rho_1 = -i\rho_2 = \rho$
- The energy of the condensed state:

$$\epsilon_0(\rho) = \frac{1}{2}B_{\text{ext}}^2 + 2(m_\rho^2 - eB_{\text{ext}}) |\rho|^2 + 2g_s^2 |\rho|^4$$

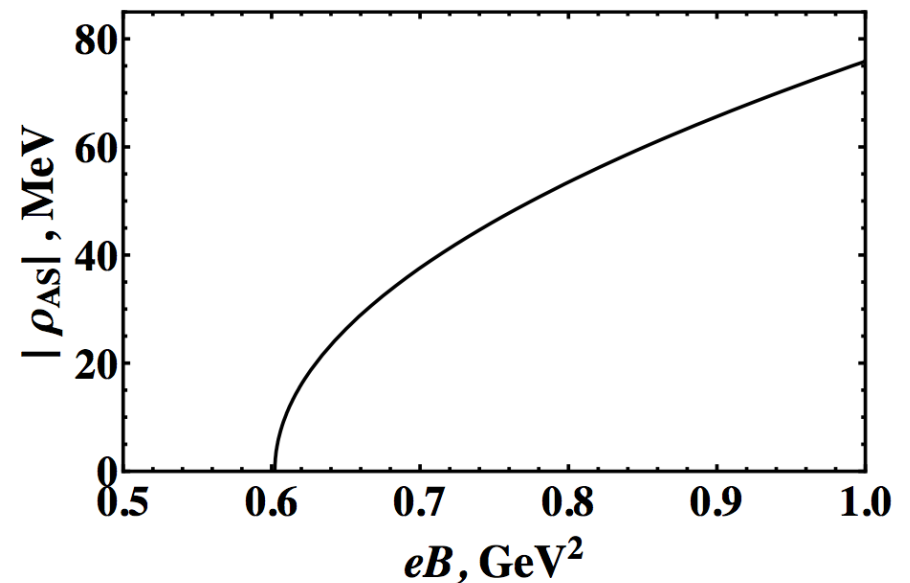
(basically, a Ginzburg-Landau potential for an s-wave superconductivity!)

- The amplitude of the condensate:

$$|\rho|_0 = \begin{cases} \sqrt{\frac{e(B_{\text{ext}} - B_c)}{2g_s^2}}, & B_{\text{ext}} \geq B_c \\ 0, & B_{\text{ext}} < B_c \end{cases}$$

Second order (quantum) phase transition, critical exponent = 1/2

(qualitatively the same picture in NJL)



# Structure of the condensates

In terms of quarks, the state  $\rho_1 = -i\rho_2 = \rho$  implies

$$\langle \bar{u}\gamma_1 d \rangle = \rho(x_\perp), \quad \langle \bar{u}\gamma_2 d \rangle = i\rho(x_\perp)$$

Depend on transverse coordinates only

(the same results in different models,  
for example, in Nambu-Jona-Lasinio)

$$\vec{B} = (0, 0, B)$$

$$U(1)_{\text{e.m.}} : \quad \rho(x) \rightarrow e^{i\omega(x)} \rho(x) \quad \text{Abelian gauge symmetry}$$

$$O(2)_{\text{rot}} : \quad \rho(x) \rightarrow e^{i\varphi} \rho(x) \quad \text{Rotations around B-axis}$$

- The condensate “locks” rotations around field axis and gauge transformations:

$$U(1)_{\text{e.m.}} \times O(2)_{\text{rot}} \rightarrow U(1)_{\text{locked}}$$



# Basic features of $\rho$ meson condensation

- The condensate of the  $\rho$  mesons appears in a form of an inhomogeneous state, analogous to the Abrikosov lattice in the mixed state of type-II superconductors.

A similar state, the vortex state of W bosons, may appear in Electroweak model in the strong external magnetic field [Ambjorn, Olesen (1989)]

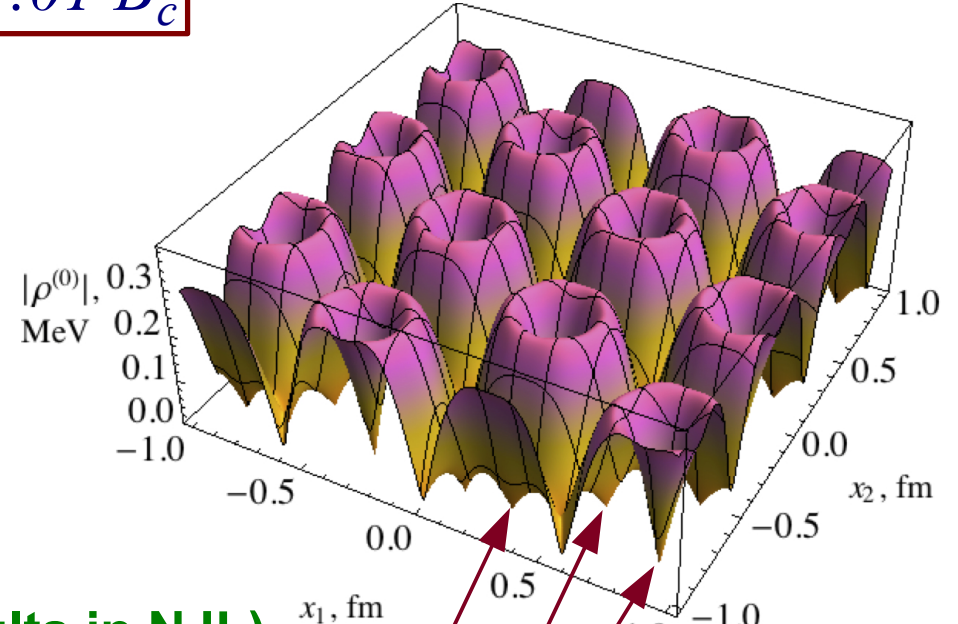
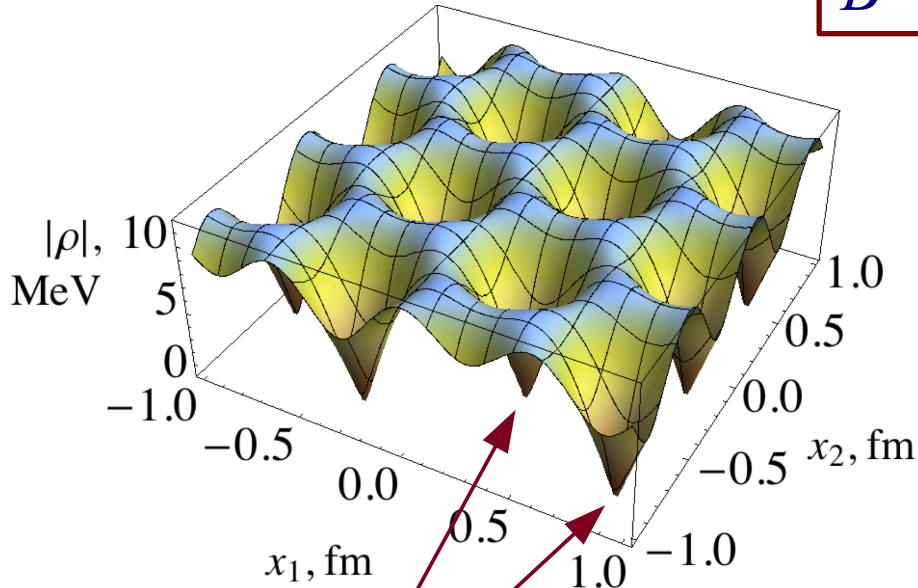
- The condensate forms a lattice, which is made of the new type of topological defects, the  $\rho$  vortices.
- The emergence of the condensate of the charged  $\rho$  mesons induces spontaneous condensation of the neutral  $\rho$  mesons.
- The condensate of charged  $\rho$  mesons implies superconductivity.
- The condensate of neutral  $\rho$  mesons implies superfluidity.
- Unusual optical properties of the superconducting state:  
It is a metamaterial (“perfect lens” optical phenomenon) with negative electrical permittivity ( $\epsilon$ ), negative magnetic permeability ( $\mu$ ), negative index of refraction ( $n$ ) [Smolyaninov, PRL 107, 253903 (2011)].

# Solution for condensates of $\rho$ mesons

Superconducting condensate  
(charged rho mesons)

Superfluid condensate  
(neutral rho mesons)

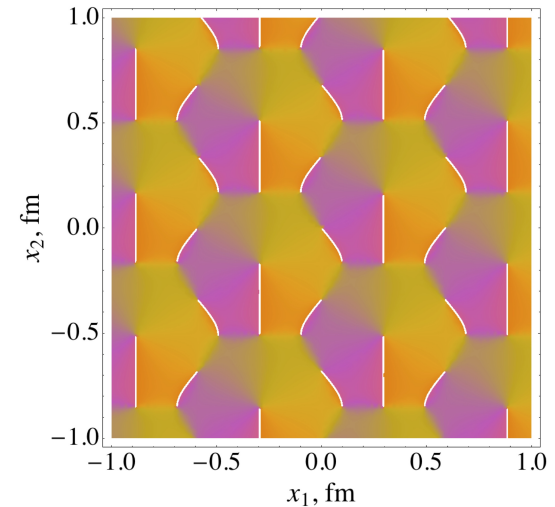
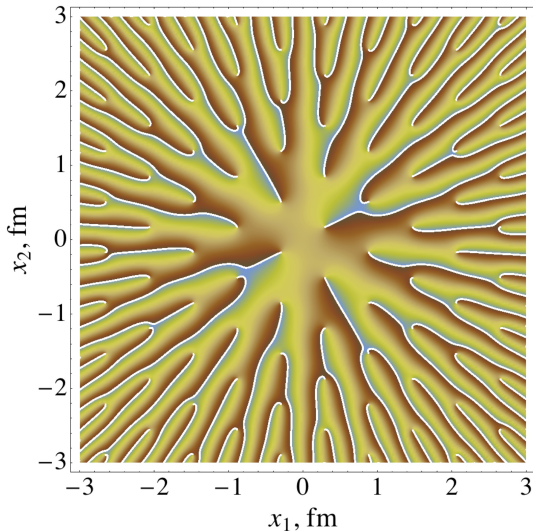
$$B = 1.01 B_c$$



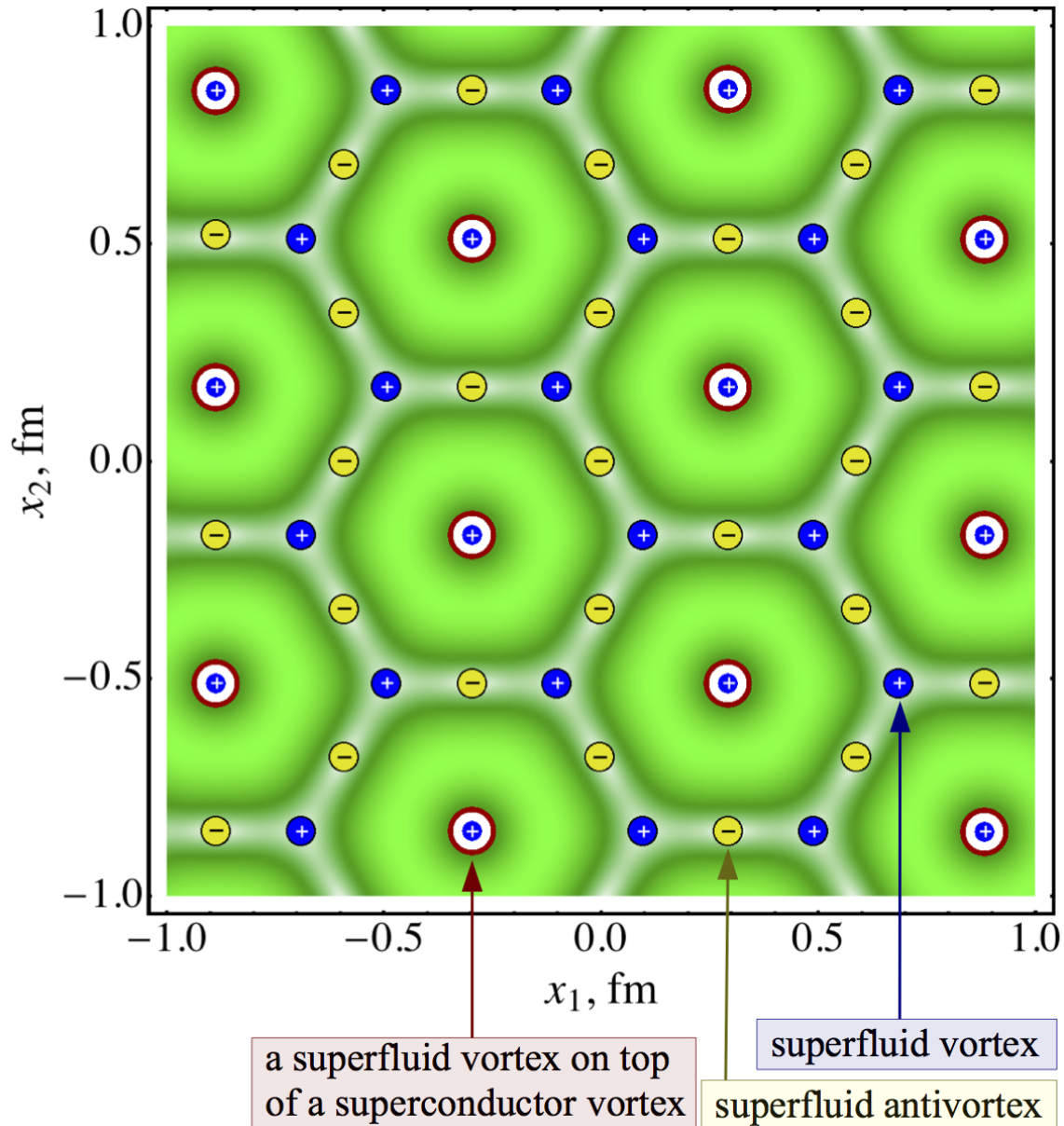
(similar results in NJL)

New objects, topological vortices, made of the rho-condensates

The phases of the rho-meson fields wind around vortex centers, at which the condensates vanish.



# Topological structure of the $\rho$ mesons condensates



# Anisotropic superconductivity

(via an analogue of the London equations)

- Apply a weak electric field  $E$  to an ordinary superconductor
- Then one gets accelerating electric current along the electric field:

$$\frac{\partial \vec{J}_{\text{GL}}}{\partial t} = m_A^2 \vec{E} \quad \text{[London equation]}$$

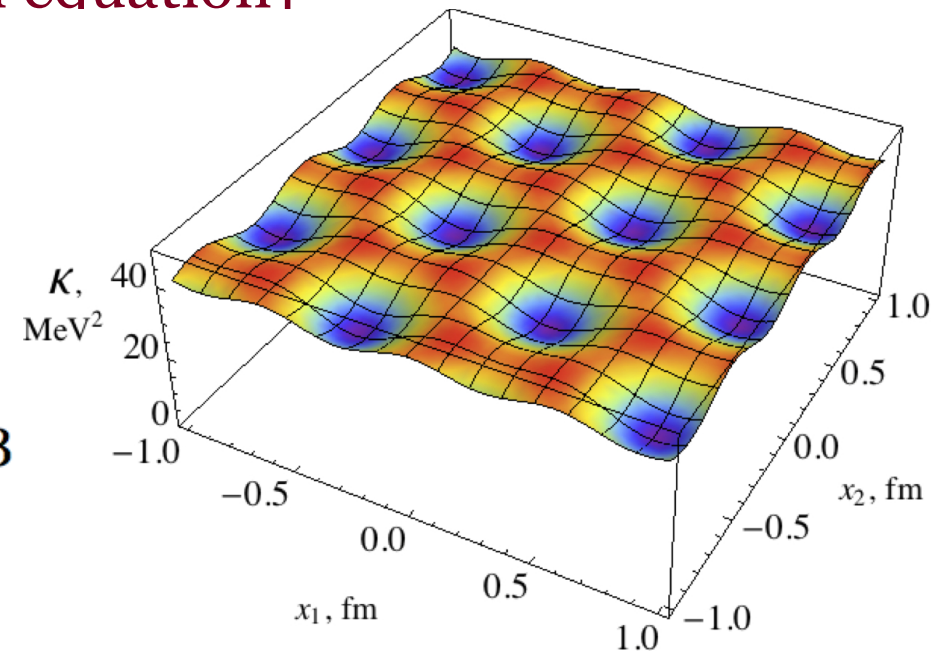
- In the QCDxQED vacuum, we get an accelerating electric current along the magnetic field  $\mathbf{B}$ :

$$\frac{\partial}{\partial t} \langle J_3 \rangle = -\frac{2e^3}{g_s^2} (B_{\text{ext}} - B_c) E_3$$

$$\frac{\partial}{\partial t} \langle J_1 \rangle = \frac{\partial}{\partial t} \langle J_2 \rangle = 0$$

(for  $B \geq B_c$ )

Written for an electric current averaged over one elementary (unit) rho-vortex cell



(similar results in NJL)

# Basic features of $\rho$ meson condensation, results

(now we are solving the full set of equations of motion)

- The condensate of the  $\rho$  mesons appears in a form of an inhomogeneous state, analogous to the Abrikosov lattice in the mixed state of type-II superconductors.

A similar state, the vortex state of W bosons, may appear in Electroweak model in the strong external magnetic field [Ambjorn, Olesen (1989)]

- The condensate forms a lattice, which is made of the new type of topological defects, the  $\rho$  vortices.
- The emergence of the condensate of the charged  $\rho$  mesons induces spontaneous condensation of the neutral  $\rho$  mesons.
- The condensate of charged  $\rho$  mesons implies superconductivity.
- The condensate of neutral  $\rho$  mesons implies superfluidity.

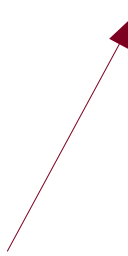

# Anisotropic superconductivity

(Lorentz-covariant form of the London equations)

We are working in the vacuum, thus the transport equations may be rewritten in a Lorentz-covariant form:

Electric current  
averaged over  
one elementary  
rho-vortex cell



$$\partial_{[\mu, j_{\nu]} = \kappa \frac{(F \cdot \tilde{F})}{(F \cdot F)} \tilde{F}_{\mu\nu}$$



A scalar function of Lorentz invariants.  
In this particular model:

$$\kappa = (e^3 / g_s^2) (\sqrt{(F \cdot F) / 2} - B_c)$$

(slightly different form of  $\kappa$  function in NJL)

Lorentz invariants:

$$(F \cdot \tilde{F}) = F^{\mu\nu} \tilde{F}_{\mu\nu} \equiv 4(\vec{B} \cdot \vec{E})$$

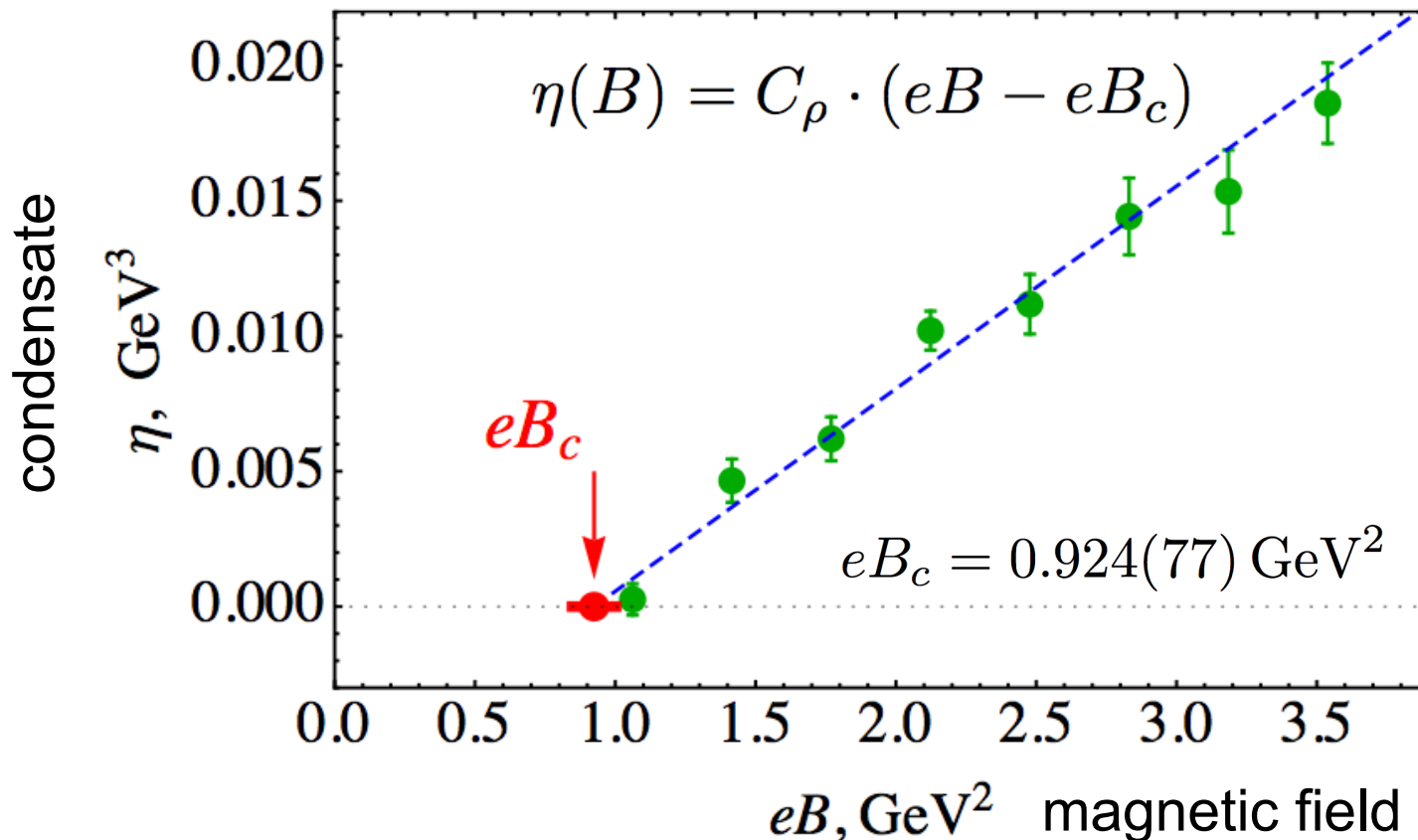
$$(F \cdot F) = F^{\mu\nu} F_{\mu\nu} \equiv 2(\vec{B}^2 - \vec{E}^2)$$

$$\tilde{F}_{\mu\nu} = \frac{1}{2} \epsilon_{\mu\nu\alpha\beta} F^{\alpha\beta}$$

# Numerical simulations of vacuum in the magnetic field background

V.Braguta, P. Buividovich, M. Polikarpov, M.Ch., arXiv:1104.3767

Numerical simulation:  $B_c = (1.56 \pm 0.13) \cdot 10^{16}$  Tesla



Theory:

$$B_c = \frac{m_\rho^2}{e} \approx 10^{16} \text{ Tesla}$$
$$\eta \sim \sqrt{B - B_c}$$

for  $B \geq B_c$

[qualitatively realistic vacuum, quantitative results may receive corrections (20%-50% typically)]

# Too strong magnetic field?

$$B_c = \frac{m_\rho^2}{e} \approx 10^{16} \text{ Tesla}$$

Over-critical magnetic fields (of the strength  $B \sim 2 B_c$ ) may be generated in ultraperipheral heavy-ion collisions (duration is short, however – clarifications are needed)

W. T. Deng and X. G. Huang,

Phys.Rev. C85 (2012) 044907 [arXiv:1201.5108]

**A bit of dreams (in deep verification stage):**

**Signatures of the superconducting state of the vacuum could possibly be found in ultra-peripheral heavy-ion collisions at LHC.**

***[ultra-peripheral: cold vacuum is exposed to strong magnetic field]***

**Early Universe?**



# Conclusions

- In a sufficiently strong magnetic field condensates with  $\rho^\pm$  meson quantum numbers are formed spontaneously via a second order phase transition with the critical exponent  $1/2$ .
- The vacuum (= no matter present, = empty space, = nothing) becomes electromagnetically superconducting.
- The superfluidity of the neutral  $\rho^0$  mesons emerges as well.
- The superconductivity is anisotropic: the vacuum behaves as a superconductor only along the axis of the magnetic field.
- New type of topological defects, " $\rho$  vortices", emerge.
- The  $\rho$  vortices form Abrikosov-type lattice in transverse directions.
- The Meissner effect is absent.