

# A Monte Carlo galaxy catalogue generator for CI analysis

Philippe Baratta (CPPM/CPT)

PhD student at Aix-Marseille Université

supervisor:

Julien Bel (CPT)

Anne Ealet (IPNL)

Collaborator:

Stephane Plaszczynski (LAL)



## Outline

- ▶ Motivations
- ▶ Sampling a field with a given p.d.f and power spectrum
- ▶ Generating a galaxy catalogue
- ▶ Analysis on  $\mathcal{C}_\ell$ 's + covariance matrix

## Motivations

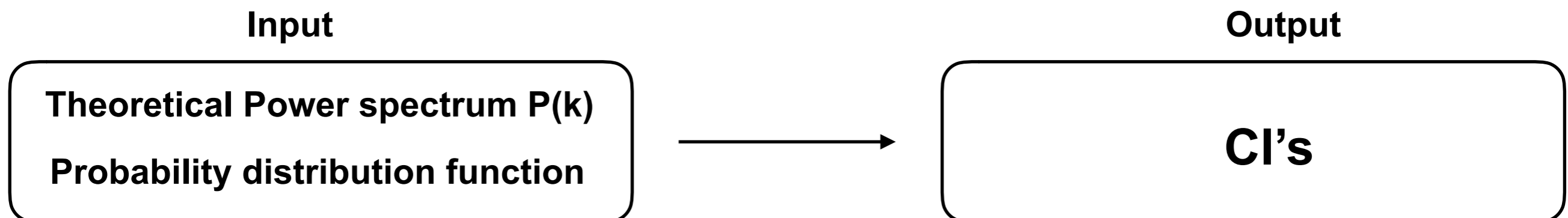
- ▶ Challenging the accuracy of galaxy surveys implies to develop strong statistical methods in LSS data analysis to constrain the large variety of cosmological models. The observational chain must be controlled and unbiased

### Need for reliable covariance matrix for a given observable

- ▶ What kind of observable ? Need for a direct observable that does not suffer from any fiducial bias :

**the angular power spectrum  $C_\ell$**

- ▶ Possibility: galaxy catalogue simulations
  - Fast —> **Monte Carlo** sampling
  - Few characteristics but well controlled



## Sampling a field with a given p.d.f. and power spectrum

► The simplest case of a **gaussian p.d.f.** of a matter field

- In a periodic box of length  $L$  and number of samples per side  $N_s$ , we define

$$\langle \delta_{\vec{k}} \delta_{\vec{k}'} \rangle = \delta^K(\vec{k} + \vec{k}') k_f^{-3} P(\vec{k})$$

$$\delta(\vec{x}) = \Delta\rho(\vec{x})/\rho_0 \quad \text{density contrast field}$$

$$k_f = 2\pi/L \quad \text{the fundamental mode}$$

it can be shown that 
$$\delta_{\mathbf{k}} = \sqrt{-\mathcal{P}(\mathbf{k})/k_f^3 \ln(1 - \epsilon_1)} e^{2\pi\epsilon_2}$$

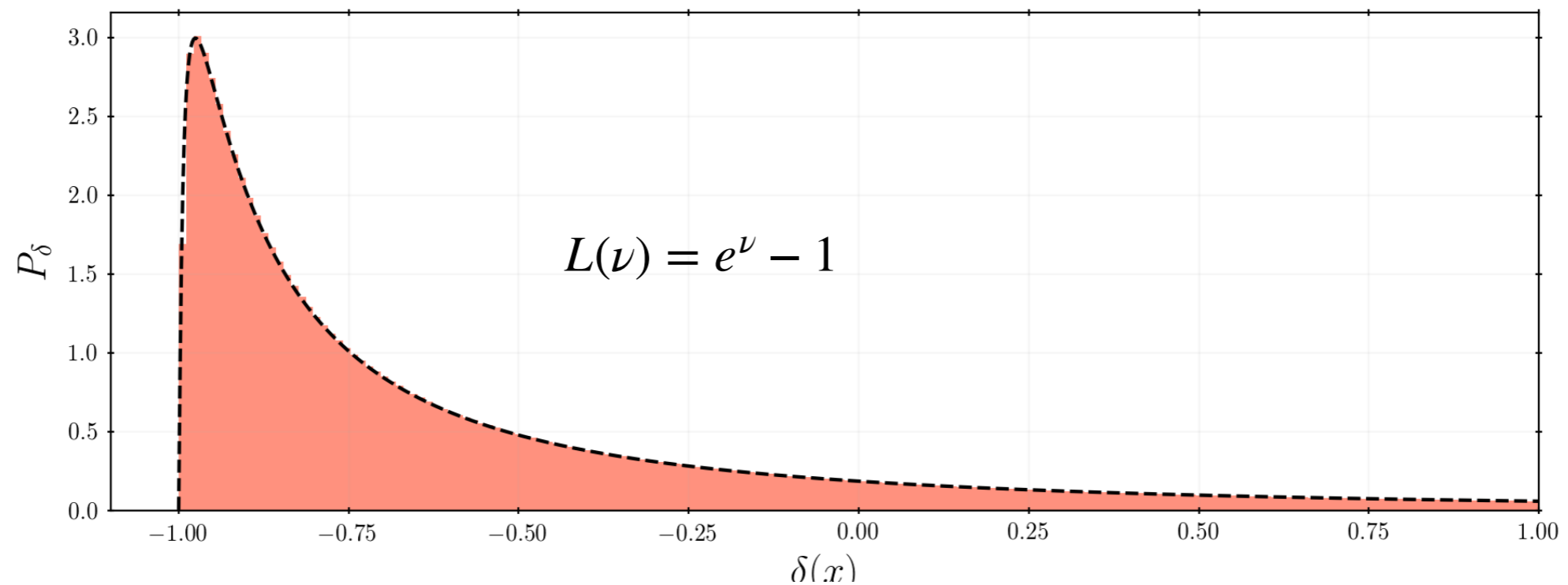
$$\epsilon_1, \epsilon_2 \in [0, 1] \quad \text{from uniform distributions}$$

- p.d.f and spectrum as expected with high level of confidence
- Well suited for CMB but dark matter clustering being non linear  $\rightarrow$  dark matter halo p.d.f non gaussian  $\rightarrow$  galaxy distribution non gaussian as well that introduce correlations between modes appearing in the covariance matrix of spectra

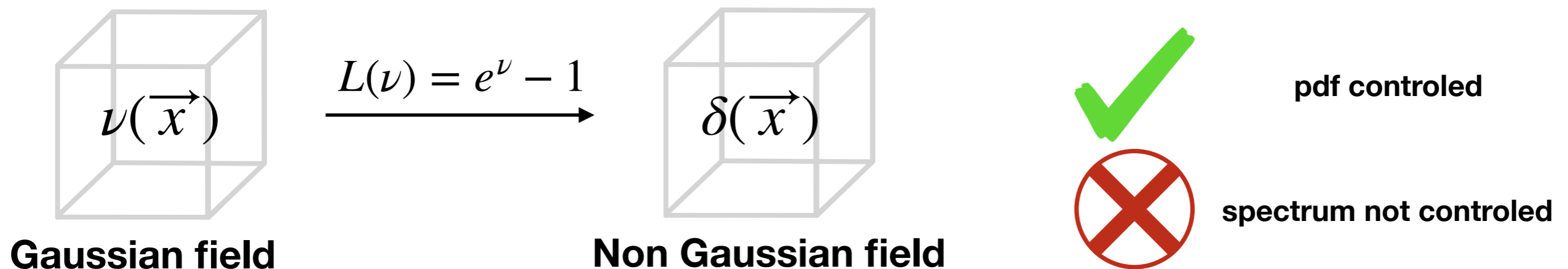
## Sampling a field with a given p.d.f. and power spectrum

► The case of a non gaussian field

**What choice of pdf ?** it can be shown (Coles & Jones (1991), Clerkin et al. (2017)) that the log-normal shape is a good approximation to represent the galaxy field



Does it works?

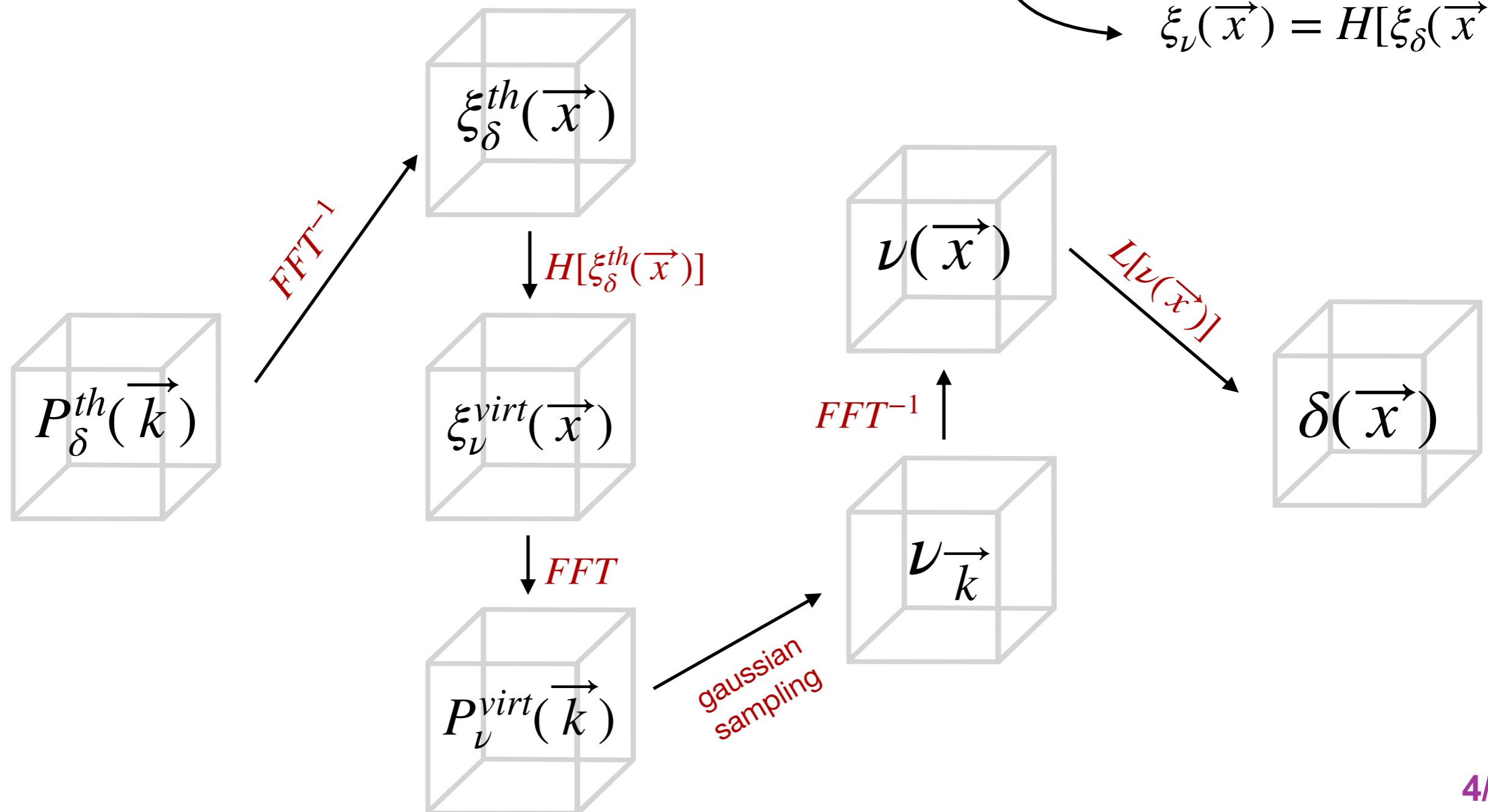


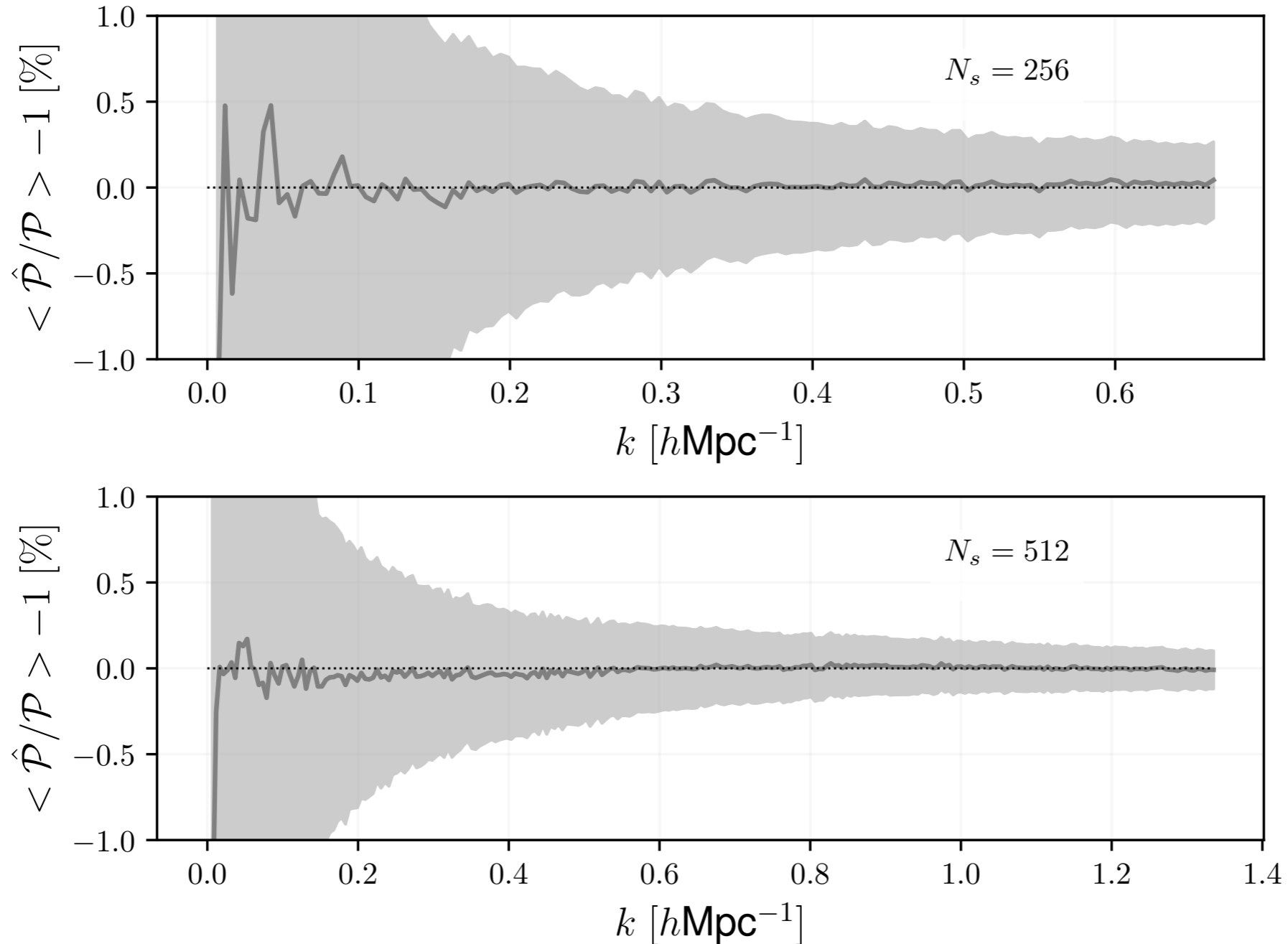
## Sampling a field with a given p.d.f. and power spectrum

► The case of a non gaussian field

- Be  $\nu(\vec{x})$  the initial gaussian field and  $\delta(\vec{x})$  the desired non gaussian field
- $\xi_\nu = FFT^{-1}[P_\nu]$  must be well designed to get a well shaped  $\delta(\vec{x})$
- Must work on  $\xi_\delta \equiv \langle \delta_1 \delta_2 \rangle = \int L(\nu_1)L(\nu_2)\mathcal{B}(\nu_1, \nu_2, \xi_\nu)d\nu_1d\nu_2$

must find out  
 $\xi_\nu(\vec{x}) = H[\xi_\delta(\vec{x})]$





**Fig. 2.** For 1000 realisations of the density field we compute the averaged 3D power spectrum that we compare relatively to the expected 3D power spectrum. We then compute the shell-averaged monopoles of this residuals in shells of width  $|\mathbf{k}| - k_f/2 < |\mathbf{k}| < |\mathbf{k}| + k_f/2$ . The result is presented in percent with error bars. The used setting is a sampling number per side of 256 in the top panel and 512 for the other, all in a box of size  $L = 1200h^{-1}\text{Mpc}$  at redshift  $z = 0$ .

► The power spectrum covariance matrix

- Need to characterise correlations between modes: **the trispectrum**

$$\left\langle \delta_{\vec{k}_1} \delta_{\vec{k}_2} \delta_{\vec{k}_3} \delta_{\vec{k}_4} \right\rangle_c = \delta^D(\vec{k}_1 + \vec{k}_2 + \vec{k}_3 + \vec{k}_4) T(\vec{k}_1, \vec{k}_2, \vec{k}_3)$$

- That have an influence on the **covariance matrix** (Scoccimarro et al. (1999)) :

Definition

$$C(X) = E[(X - E[X])(X - E[X])^T] \quad C_{ij} = \frac{\mathcal{P}(k_i)^2}{M_{k_i}} \delta_{ij}^D + k_F^3 \bar{T}(k_i, k_j)$$

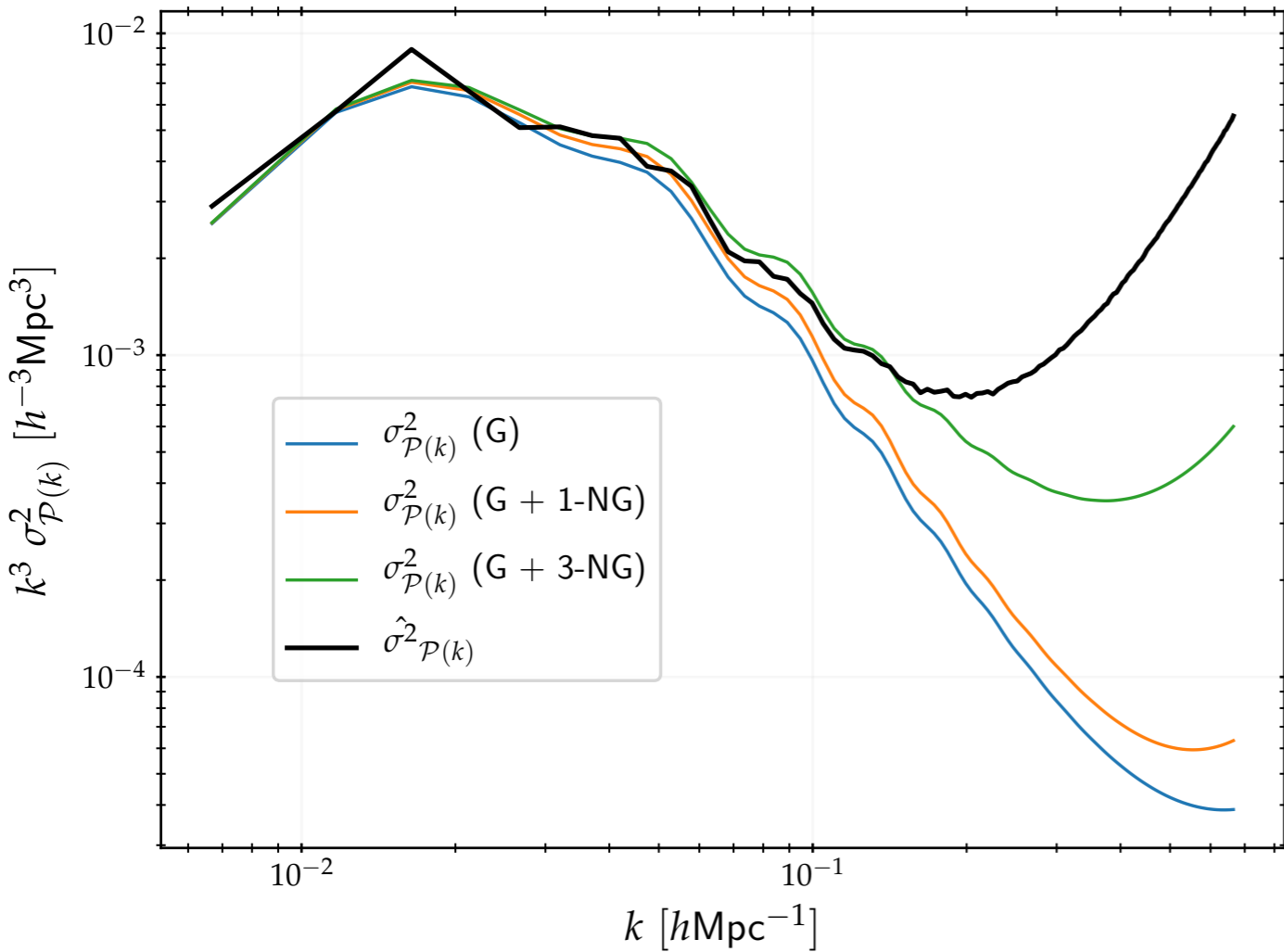
$$\bar{T}(k_i, k_j) = \int_{k_i} \int_{k_j} T(\mathbf{k}_1, -\mathbf{k}_1, \mathbf{k}_2, -\mathbf{k}_2) \frac{d^3 \mathbf{k}_1}{V_{k_i}} \frac{d^3 \mathbf{k}_2}{V_{k_j}}$$

- Developing this relation, we get the approximate expression for the diagonal

$$\begin{aligned} \bar{T}(k_i, k_i) \sim & 8c_1^2 \{4c_2^2 + 3c_3c_1\} \mathcal{P}^3(k_i) + \\ & + 24 \{3c_1^2c_3^2 + 4c_1c_2^2c_3 + 12c_1^2c_2c_4\} \mathcal{P}^2(k_i) \mathcal{P}^{(2)}(k_i) + \\ & + 144c_1^2c_3^2 \mathcal{P}^{(2)}(0) \mathcal{P}^2(k_i) \end{aligned}$$

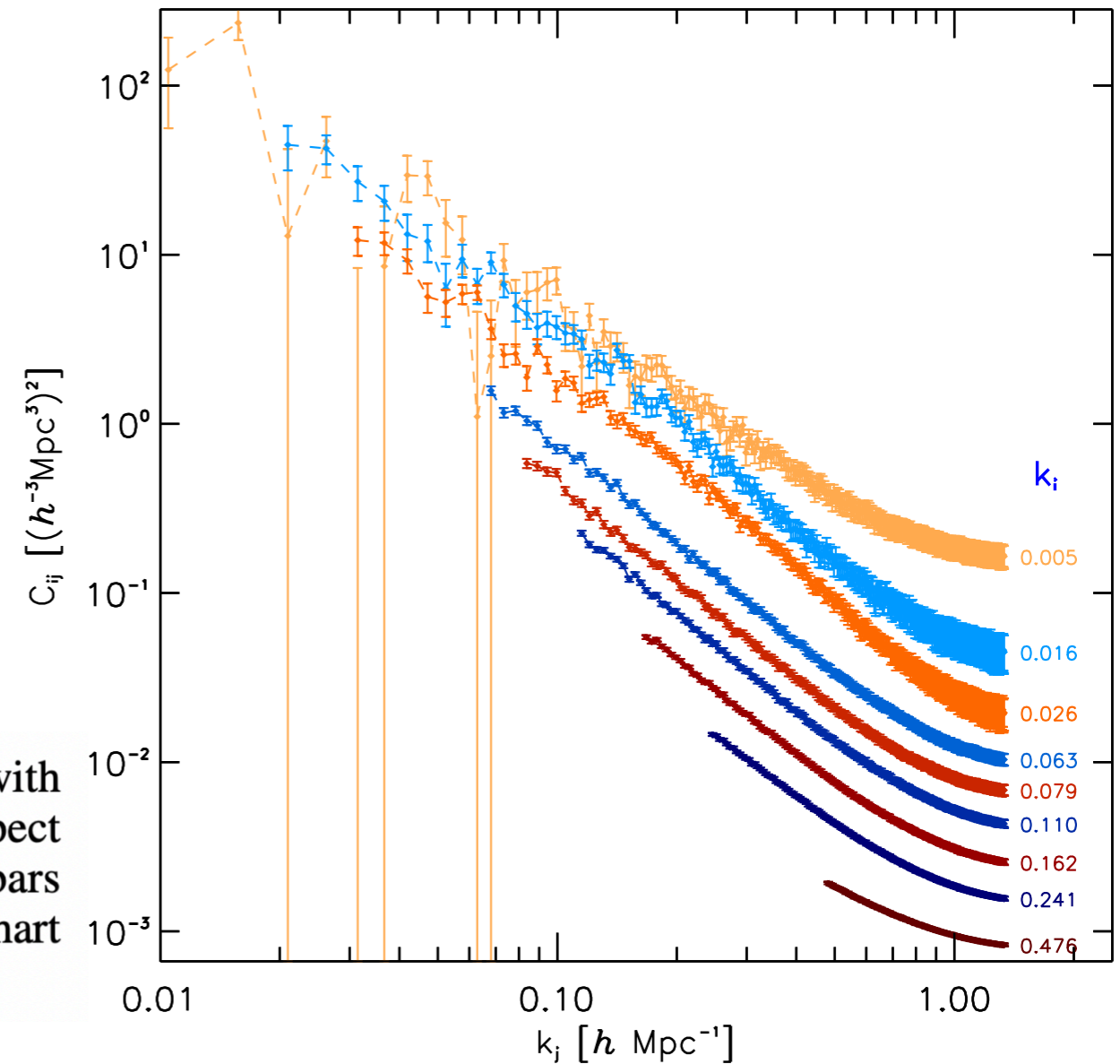
$$c_n = \frac{1}{n!} \int_{-\infty}^{\infty} L(v) H_n(v) P_v(v) dv \quad \text{the coefficients of the Hermite polynomials}$$





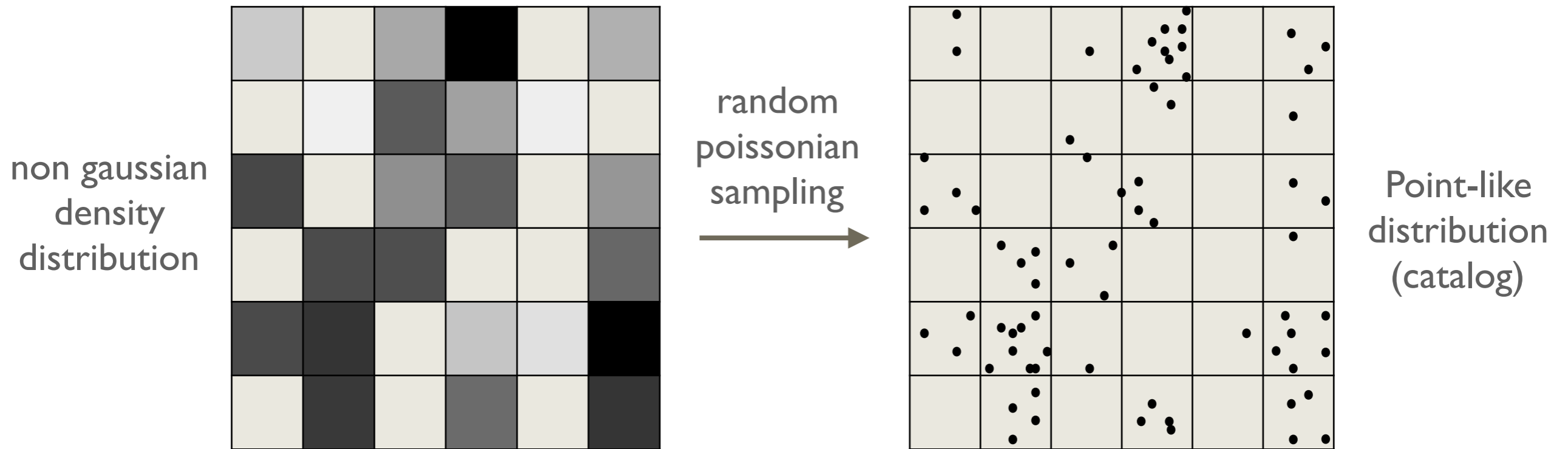
**Fig. 5.** Measured diagonal of the covariance matrix for 7375 power spectra realizations of the density field using the described method (black curve). The other curves represent their predictions taking into account the gaussian part alone (G) or by adding some non gaussian contributions of equation (18). For example in (1-NG) one keeps only the term in  $\mathcal{P}^3(k_i)$  in the trispectrum development presented in equation (20) while in (3-NG) we keep all of them.

**Fig. 6.** Off diagonal elements of the covariance matrix estimated with  $N = 7375$  realisations, showing the dependance of the  $C_{ij}$  with respect to  $k_j$  at various fixed  $k_i$  labeled on the right of the panel. The error bars are obtained assuming that the covariance coefficients follow a Wishart distribution, i.e.  $V[\hat{C}_{ij}] = (C_{ij}^2 + C_{ii}C_{jj})/(N - 1)$ .



## ► Poissonian sampling

- Snapshot : choose an average density and a smoothing scheme

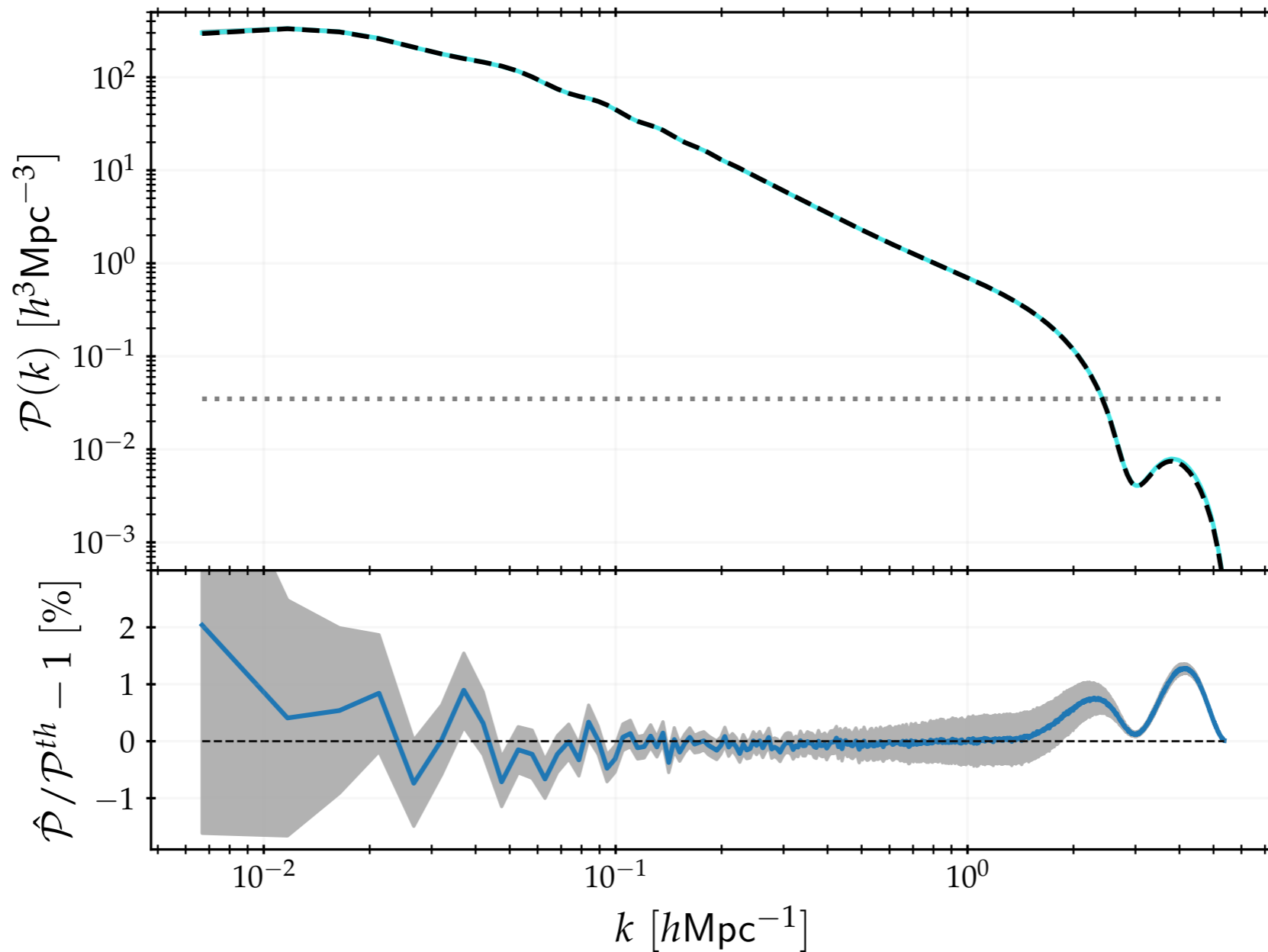


- Predicted spectrum :

$$\hat{P}(\vec{k}) = |W_{TH}(\vec{k})|^2 P^{th}(\vec{k}) + \frac{1}{\rho_0(2\pi)^3}$$

$\uparrow$   
 Convolution function

$\uparrow$   
 Shot noise



**Fig. 7.** Upper panel: Measured power spectrum averaged over 100 realizations of the poissonnian LN field (cyan curve) with associated tiny error bar in grey. Note that the shot noise is subtracted from measures (dotted horizontal line) and is about  $3.49 \times 10^{-2} h^3 \text{Mpc}^3$ . The dashed black line represent the expected power spectrum computed in equation(21). Bottom panel: Relative deviation in percent between the averaged realizations with shot noise contribution and prediction in blue line. Error bars are more relevant here and are filled in grey. The snapshot is computed for a grid of size  $L = 1200h^{-1}\text{Mpc}$  and parameter  $N_s = 256$ . Here comparisons are made well beyond the Nyquist frequency that is close to  $6.7 \times 10^{-1} h\text{Mpc}^{-1}$ .

## ► Generate a galaxy catalogue

- choose  $z_{\min}, z_{\max}$  for your catalogue and generate  $N_{\text{shl}}$  snapshots at intermediate redshifts
- place yourself at the center of each box
- select shells in snapshots that correspond to the comoving volume of the redshift interval of the snapshot
- glue all shells to reconstruct the lightcone

## ► Analysis on $C_\ell$ 's

- In the basis of spherical harmonics

$$Y_\ell^m(\theta, \phi) \equiv \sqrt{\frac{2\ell + 1}{4\pi} \frac{(\ell - m)!}{(\ell + m)!}} P_\ell^m[\cos(\theta)] e^{im\phi}$$

- Expand a scalar field in this basis

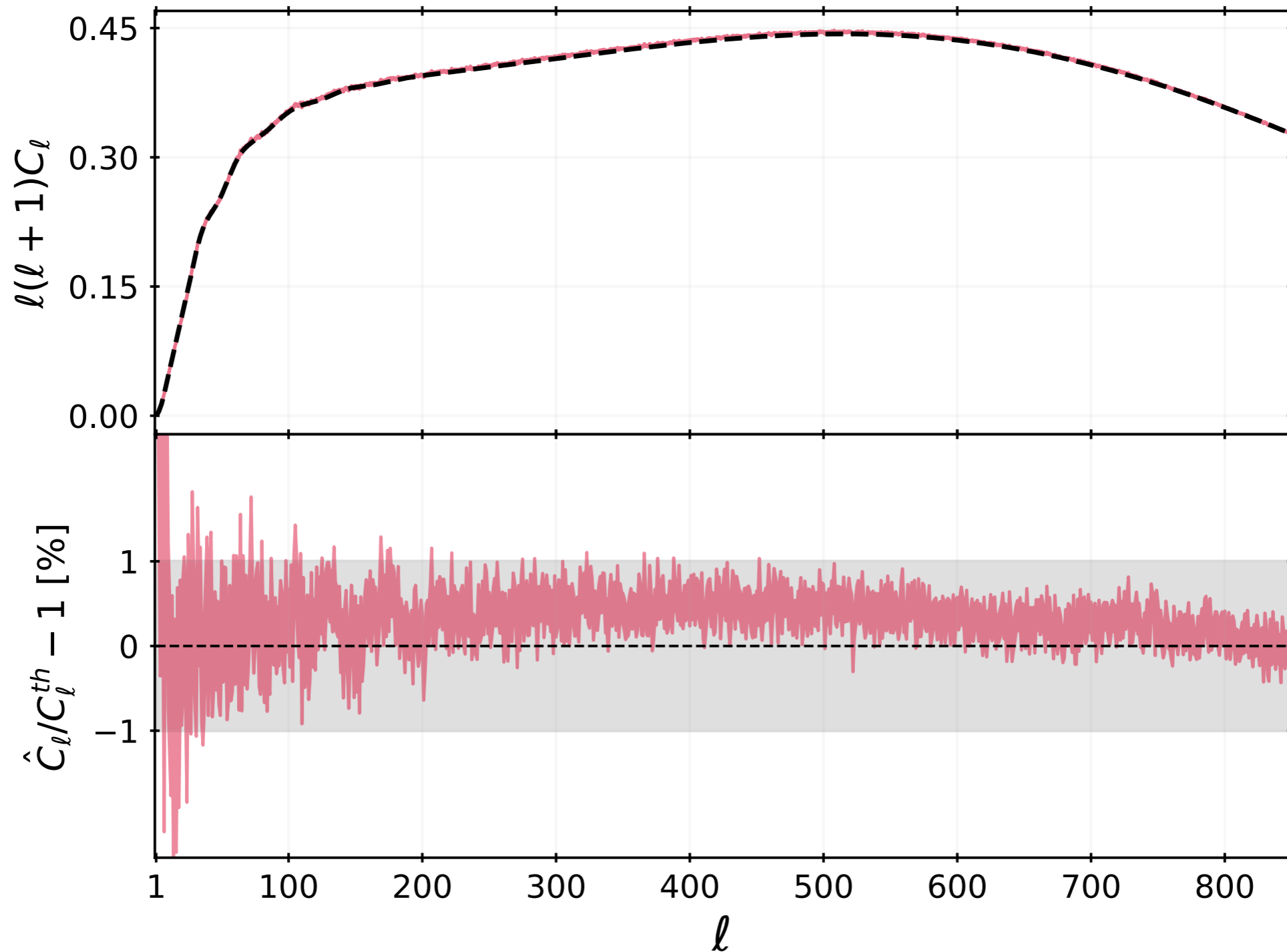
$$\delta(\mathbf{x}) = \sum_{\ell=0}^{\infty} \sum_{m=-\ell}^{\ell} \delta_\ell^m(r) Y_\ell^m(\theta, \phi)$$
$$\delta_\ell^m(r) = \int_S \delta(r, \theta, \phi) Y_\ell^{m*}(\theta, \phi) d^2\Omega.$$

- Angular power spectrum is defined as

$$C_\ell(r, r') \equiv \langle \delta_\ell^m(r) \delta_\ell^{m*}(r') \rangle$$

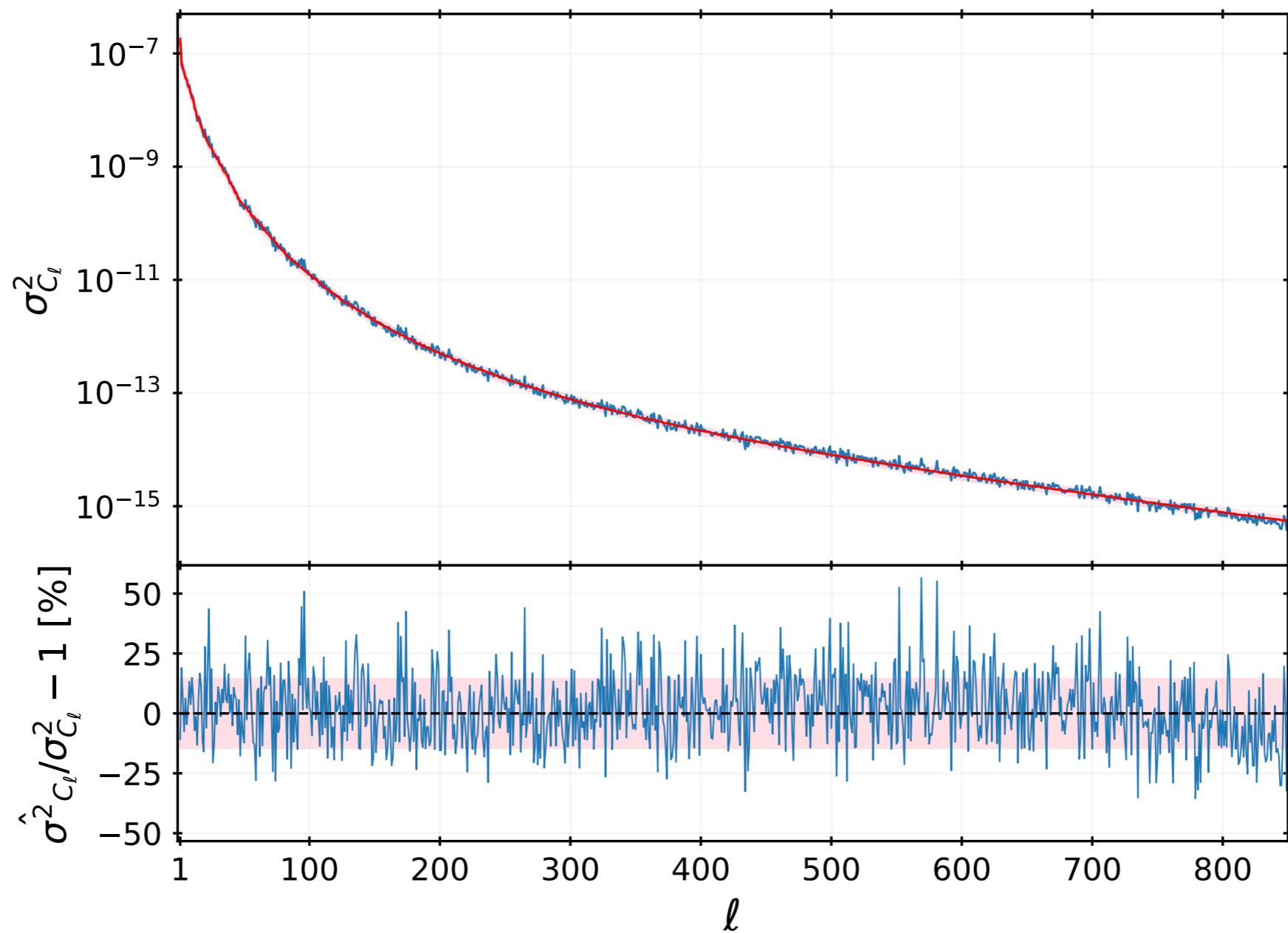
- Related to the power spectrum as

$$C_\ell(r, r') = (4\pi)^2 \int_0^\infty k^2 \mathcal{P}(k) j_\ell(kr) j_\ell(kr') dk$$

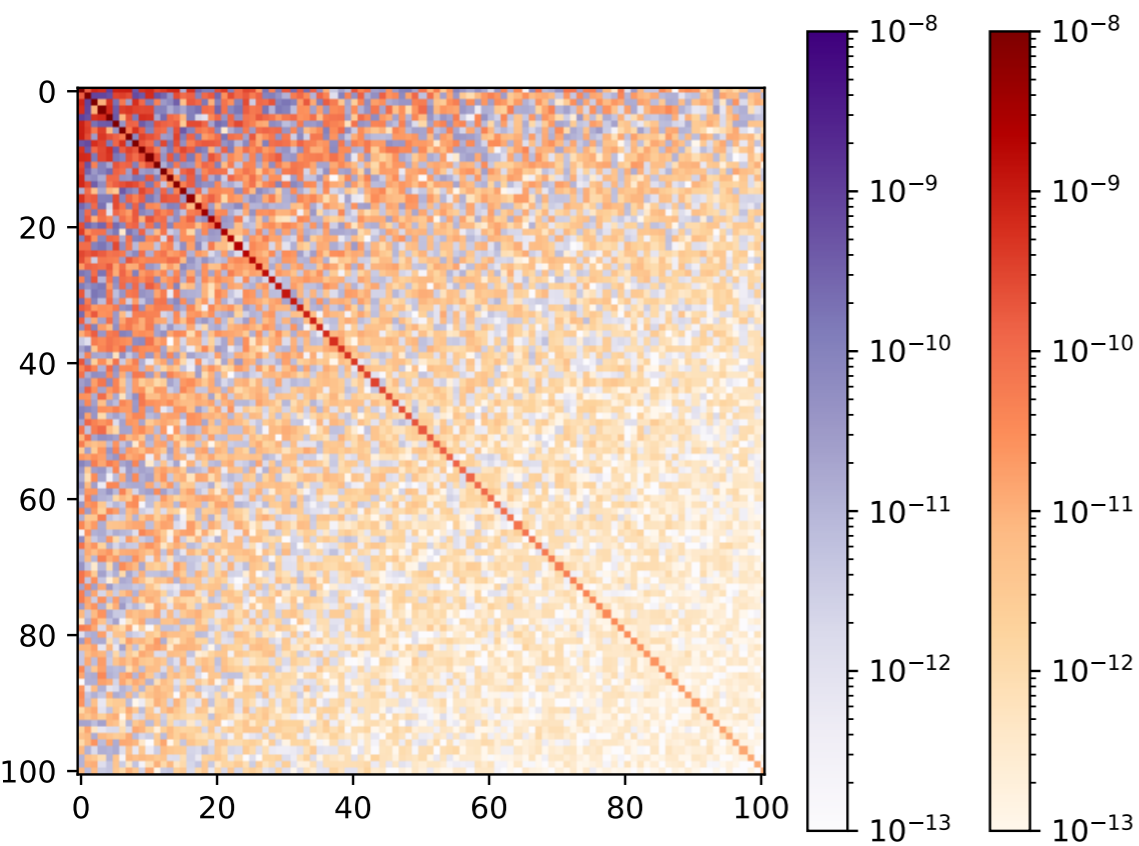


**Fig. 8.** Top panel : Thousand averaged  $C_\ell$ 's for simulated light cones using the shell-method with error bars (red curve) and corresponding prediction (dashed black curve). We simulate here a lightcone between redshifts 0.2 and 0.3 in a sampling  $N_s = 512$  and a number of shells  $N_{shl} = 250$  to ensure a sufficient level of continuity in the density field. Center panel : relative deviation in percent of the averaged  $C_\ell$ 's from prediction with error bars in red.





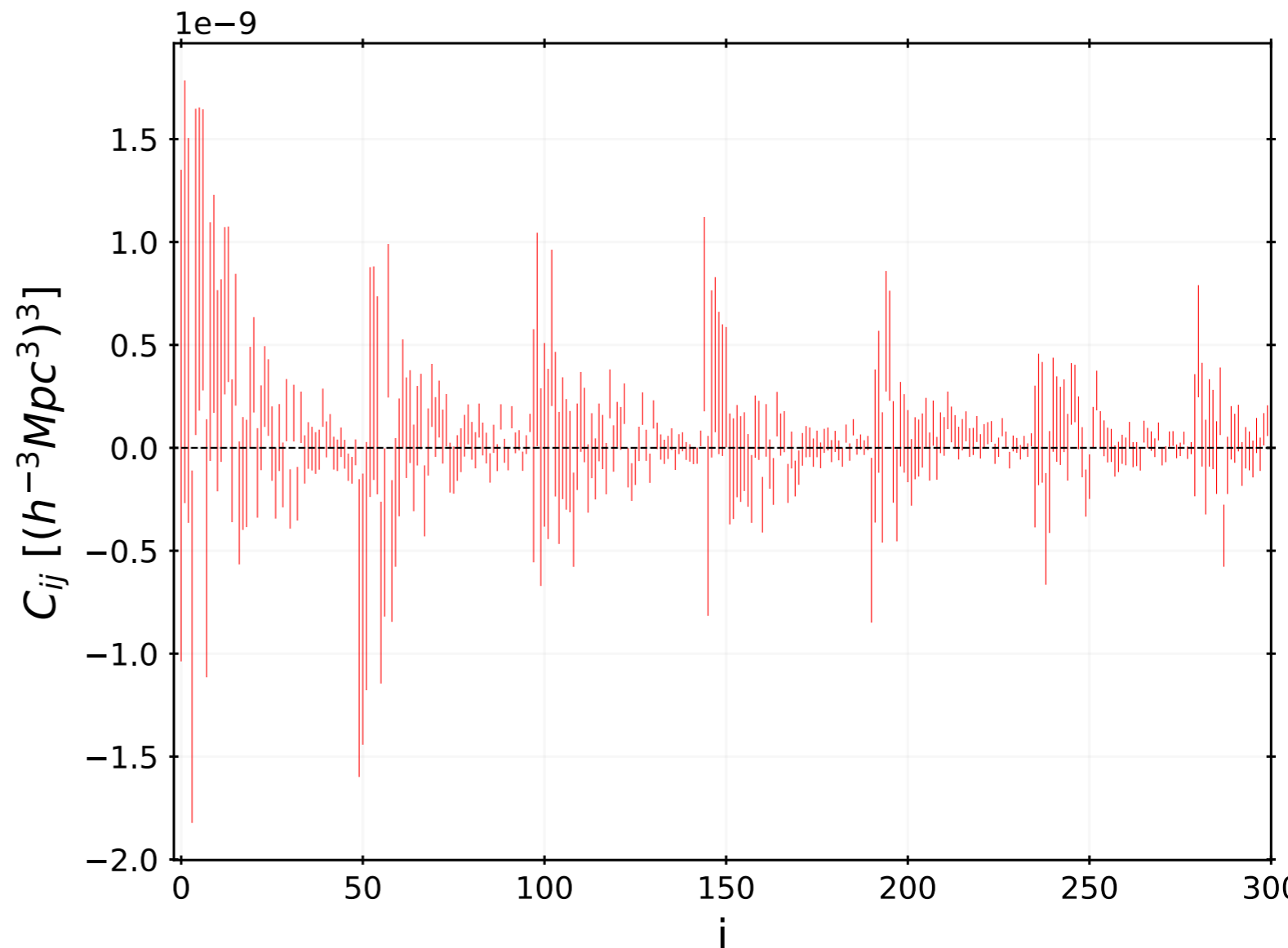
**Fig. 12.** Upper panel : measured diagonal of the covariance matrix (blue curve) over  $n = 100$  realisations of different light cones. The red curve represent the associated prediction if the case of a gaussian field with errors over it (pink area) computed using  $V[C_{ij}^G] = (C_{ii}^{G^2} + C_{ii}^G C_{jj}^G)/(n-1)$ . Here we keep the SN effect in the measures and take into account in the prediction. Bottom panel: relative difference in percent following the same color code.



**Fig. 11.** Covariance matrix for 10000 realizations of  $C_\ell$ 's in a simulated universe between redshifts 0.2 and 0.3 and a sampling  $N_s = 512$ . Only  $(\ell \times \ell) = (100 \times 100)$  first elements of the matrix are represented here. Color maps are here logarithmic scale: the red ones are the positive correlations while the blue ones are anticorrelations.

**Fig. 13.** The 300 first elements measured of the off-diagonal part of the covariance matrix over  $n = 10000$  realisations of light cone (black dots) with gaussian errors (in red) computed using  $V[C_{ij}^G] = (C_{ii}^{G^2} + C_{jj}^{G^2})/(n - 1)$ . The elements are labeled by the index  $i$  and are ordered column by column of the lower half of the matrices without passing by the diagonal.

- Near Gaussian covariance matrix



## ► Conclusion

- General code to simulate any universe in a power spectrum oriented analysis
- Fast method for accurate  $P(k)$  and  $C_{\ell}$ 's
- Covariance matrix prediction

## ► Prospectives

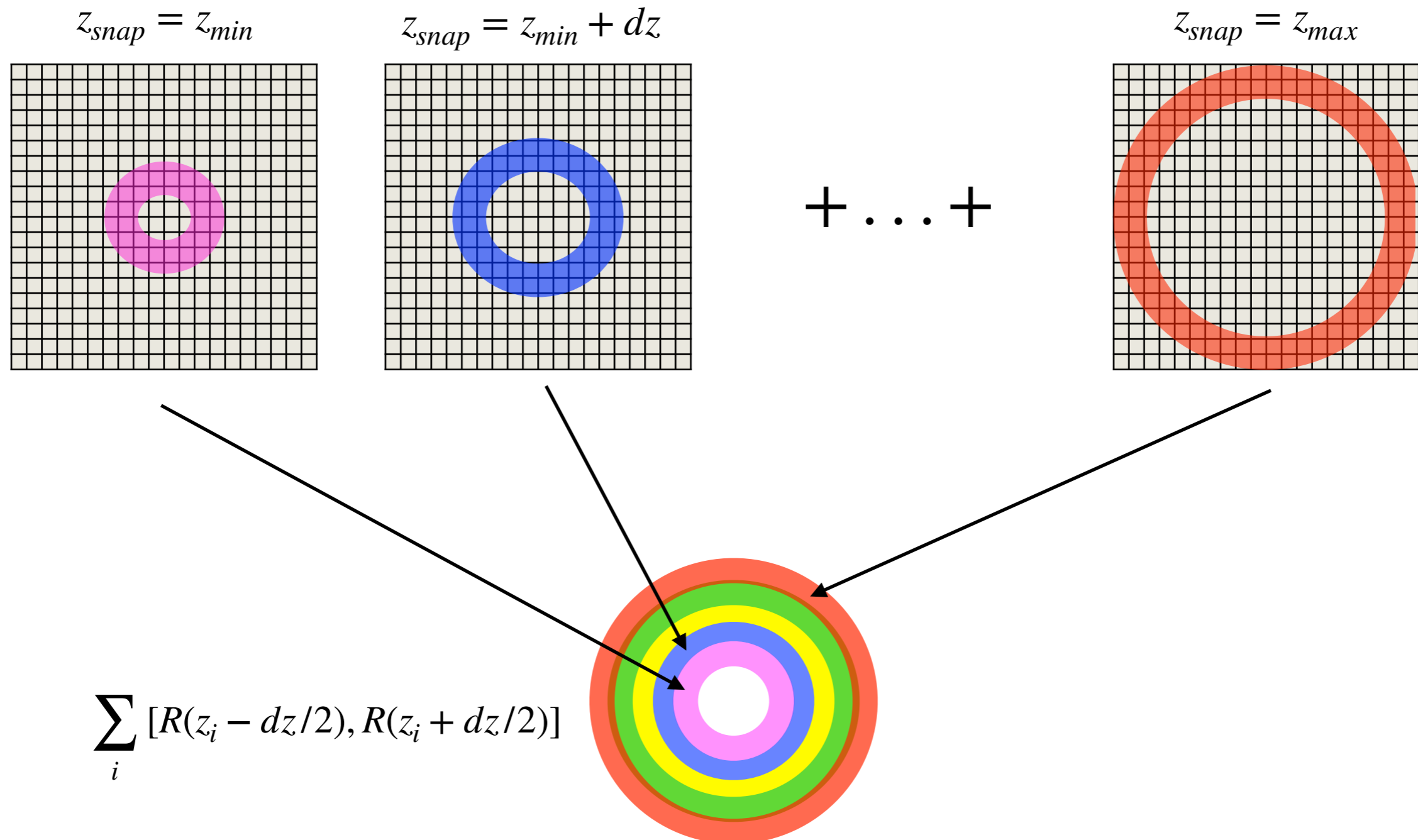
- RSD and bispectrum in next analysis
- Comparison with Nbody codes
- Evolution of covariance matrix with cosmological models



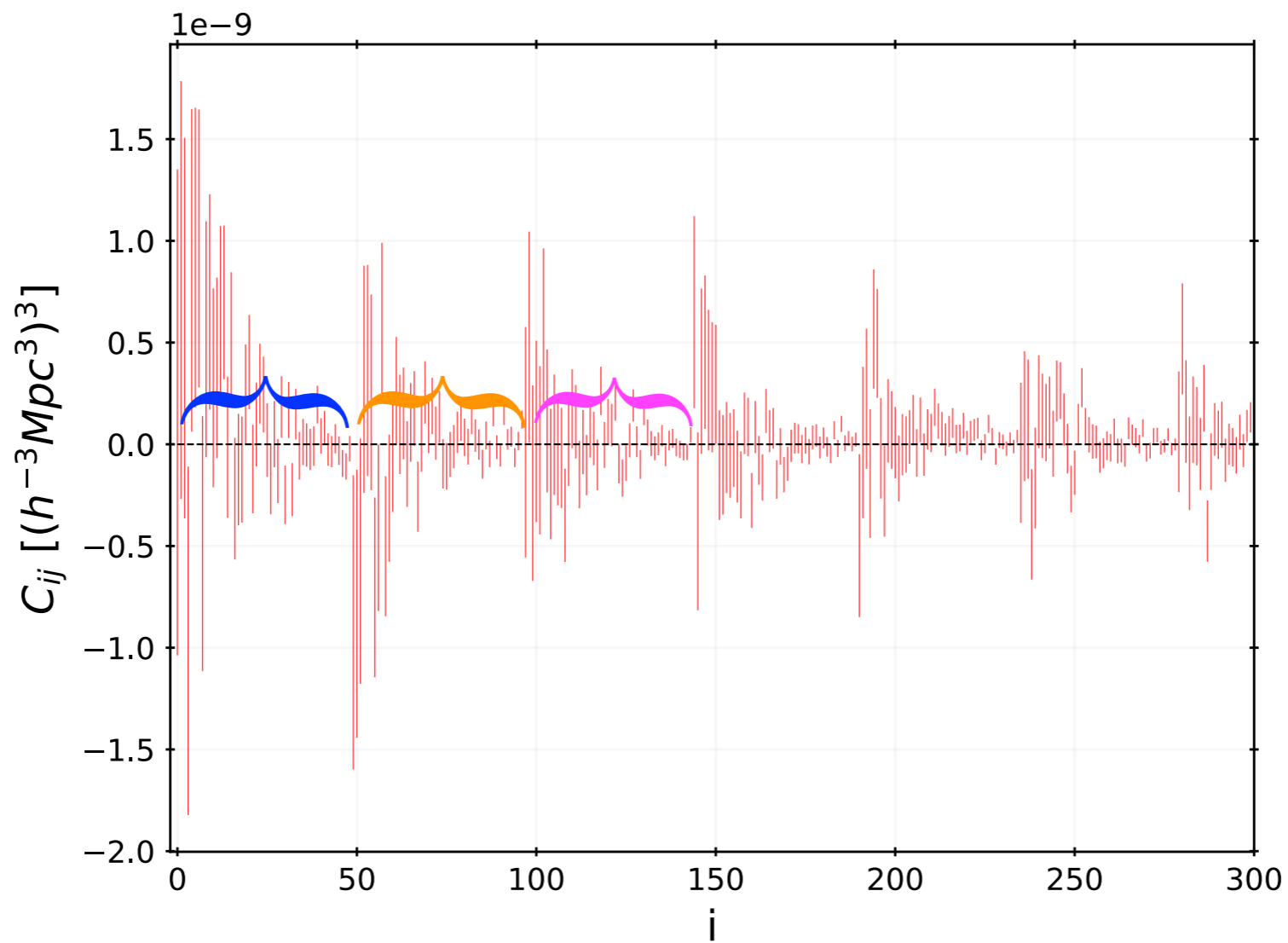
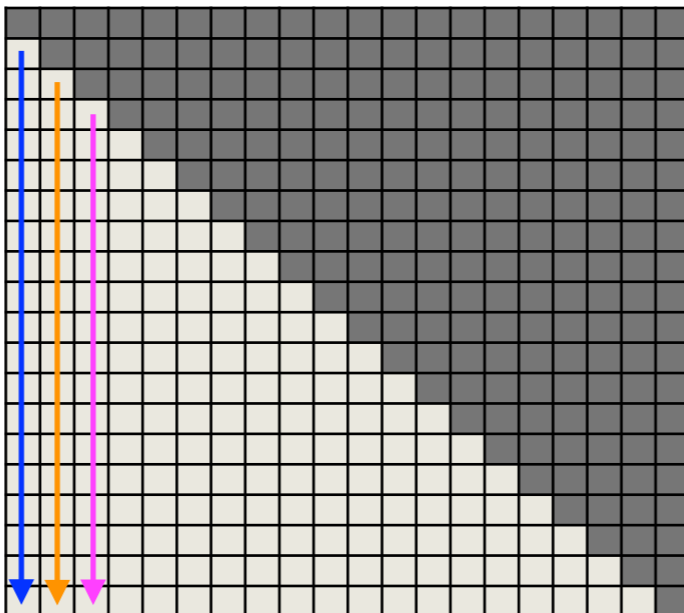
**Extra slides**

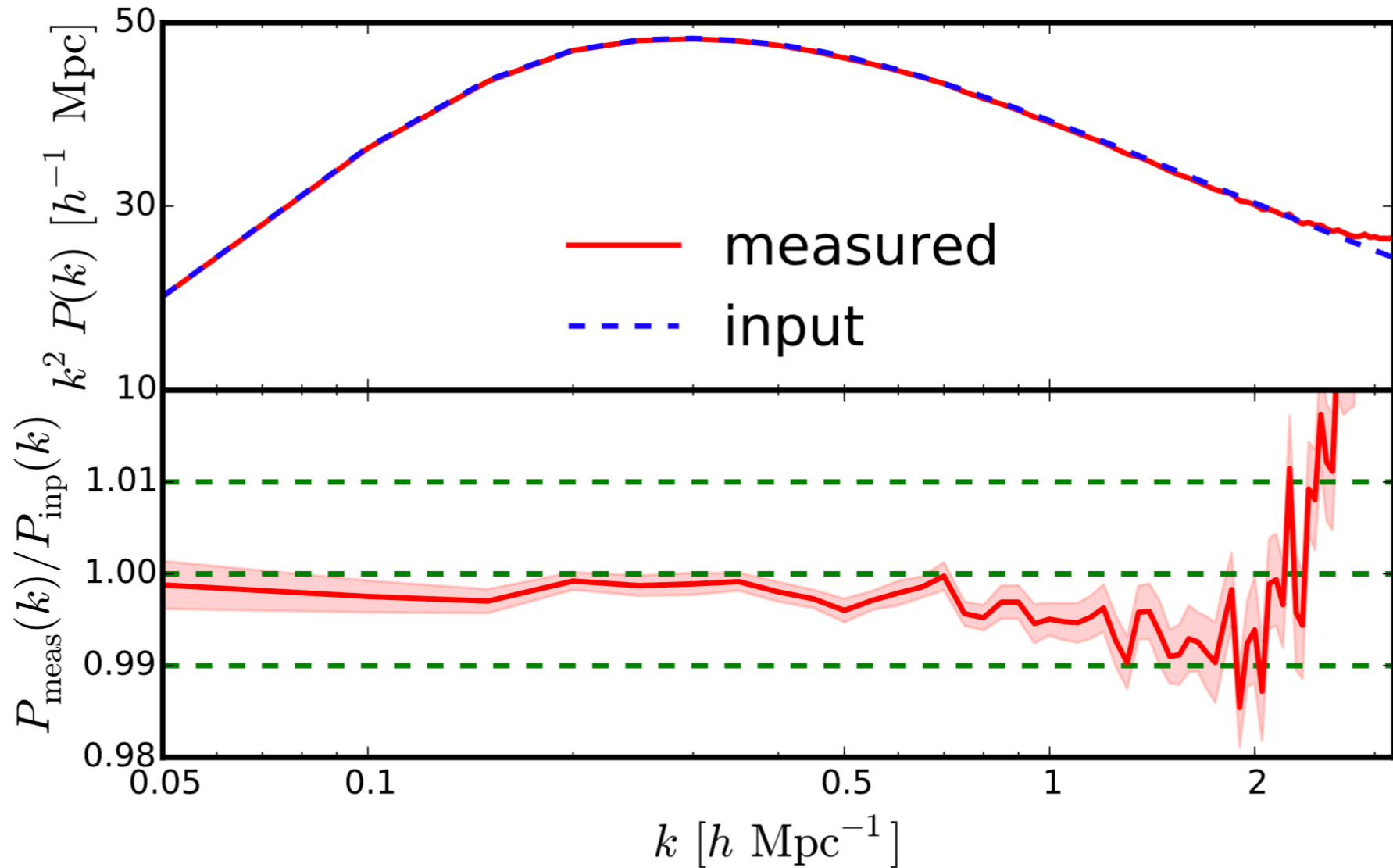
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$C_{ij} =$





**Figure 2:** (*Top*) Mean of the real-space galaxy power spectrum measured from 50 log-normal catalogs (solid) and the input power spectrum (dashed). We show  $k^2 P(k)$ . (*Bottom*) Ratio of the two. The band shows the error on the mean estimated from 50 realisations. The Nyquist frequency for these measurements is  $k_{\text{Ny}} = 3.22 h \text{ Mpc}^{-1}$ .

agrawal et al. (2017)