Acceleration Mechanisms Part II



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- Nonlinear theory of DSA, field amplification, relativistic shocks and reconnection.
 - Luke Drury





Reminder and summary

- etc...
- less shocks.

Shocks are self-forming I-D dynamical structures which convert mechanical flow energy into random particle motion.

• Ubiquitous in SNRs, stellar wind bubbles, accretion flows

• Scale of shock determined by the physics of the dissipation molecular mean free path for gas-dynamic shocks, thermal ion gyroradius or other relevant plasma scale for collision-

- to near isotropy, but not to thermal equilibrium.

 Astrophysical plasmas are very low density and collisionless - they behave as fluids only because of the long-range collective coupling through the electromagnetic field.

Magnetic fields can easily drive plasma velocity distribution

Non-thermal distributions can survive for very long times.

- that operates at collisionless shocks

Diffusive Shock Acceleration is a variant of Fermi acceleration

 Produces non-thermal power-law tails extending to high energy on the downstream particle momentum distribution function.

• Shock is simple jump discontinuity

 $U(x) = \begin{cases} U_1, & x < 0, \\ U_2, & x > 0 \end{cases}$

• Particles have power-law spectrum in momentum



Acceleration time-so



Summary of test-particle (linear) theory

$$s = \frac{3U_1}{U_1 - U_2}$$

cale is
$$\left(\frac{\kappa_1}{U_1} + \frac{\kappa_2}{U_2}\right)$$

But easy to show that accelerated particle pressure can be significant, so must worry about reaction effects. Also, if process is to work with high efficiency, as appears to be required, eg, to explain the Galactic cosmic ray origin, we need a nonlinear theory.

In principle easy - we just have to solve the diffusive transport equation and the usual hydrodynamic equations with an additional cosmic ray pressure in the momentum equation!

In practice very hard!

 $P_C(x) = \int \frac{4\pi p^3 v}{3} f(p, x) dp$

- Throw it at the computer
- Monte-Carlo approach
- Two-fluid approximation
- Semi-analytic theories

Possible approaches

Good general agreement now between all approaches!

Very wide scale separation - numerical nightmare, but useful for analytic approaches. Can distinguish two extreme scales..

energies

Aim of analytic theory should be to bridge the gap between these two regimes (mesoscopic theory), but not to try to be a complete theory. Analogy to inertial range theories of turbulence.

Outer scale of macroscopic system and maximum

Inner scale of injection processes and kinetic effects



Outer scale Astrophysics

Precursor

Intermediate scales Shock acceleration theory

Subshock

Inner scale Plasma physics Injection!

Shock modification

- Extended upstream precursor + subshock structure
- Increased total compression due to
 - softer equation of state
 - additional energy flux to high energy particles (escape, geometrical dilution, diffusion)

 $\rho_1 U_1 = \rho_2 U_2 = A$ $AU_1 = AU_2 + P_2$ $\frac{1}{2}AU_1^2 = \frac{1}{2}AU_2^2 + U_2(\mathcal{E}_2 + P_2) + \Phi$ $\implies \frac{U_1}{U_2} = 1 + \frac{2\mathcal{E}_2}{P_2} + \frac{2\Phi}{U_2P_2}$

Aside on compression in a strong shock....

Typically see compression rations of 10 and more in simulations

- Spectrum at low energies given by testsofter.
- increased compression of total shock structure, thus harder
- law.

particle theory applied to the sub-shock, thus

• Spectrum at high energies should reflect much

Concave spectrum - no longer perfect power-

Semi-analytic approach to steady mesoscopic structure

Can (hopefully) assume steady planar structure with fixed mass and momentum fluxes.

 $AU + P_G + P_C = B$

and we still have the steady balance between acceleration and loss downstream...

 $\frac{-}{\partial p} = -4\pi p^2 f_0(p) U_2$

- $\rho U = A$

.. but the problem is that the acceleration flux now distribution.

However, if one makes an Ansatz $f_0(p) \rightarrow f(x,p)$

the particle conservation equation and the momentum balance equations, become two coupled equations (in general integrodifferential) for the two unknown functions.

 $U(x), f_0(p)$

depends on the upstream velocity profile and the particle

An obvious Ansatz would be to assume a distribution similar to that familiar from the test-particle theory,

 $f(x,p) = f_0(p) \epsilon$

 $f(x,p) = f_0(p) \exp \left(\right)$

$$\exp\int \frac{U(x)\,dx}{\kappa(x,p)}$$

This is actually close to Malkov's Ansatz who, however, uses

$$\left(\frac{1}{3}\frac{\partial \ln f_0}{\partial \ln p}\right)\frac{U(x)dx}{\kappa(x,p)}$$

which is better for strongly modified shocks.

 $f = p^{-7/2} \, \text{ex}$

Motivation comes from exact solution for uniformly distributed compression, ie linear velocity field. Easy to check that

$$\exp\left(\frac{-\alpha x^2}{2\kappa}\right)$$

identically satisfies

 $\frac{\partial f}{\partial t} + U \frac{\partial f}{\partial x} - \frac{1}{3} \frac{\partial U}{\partial x} p \frac{\partial f}{\partial p} = \frac{\partial}{\partial x} \left(\kappa \frac{\partial f}{\partial x} \right)$ for U(x) = -x, $\kappa \propto p$, $\alpha = \frac{1}{6}$

 $f(x,p) = p^{-7/2} \exp\left(\frac{-\alpha x^2}{2\kappa}\right)$ $= f_0(p) \int \left(-\frac{1}{3} \frac{\partial \ln f_o}{\partial \ln p} \right) \frac{U(x) dx}{\kappa}$

So the additional factor introduced by Malkov in the exponential can be thought of as compensating for the fact that the acceleration is distributed over the whole precursor and is not just concentrated at one point.

Blasi introduces a further factor to interpolate between these and recommends the following modified version of Malkov's Ansatz

 $f(x,p) = f_0(p) \exp \int \left(-\frac{1}{3}\right)$

Note that all of these are approximations and not exact solutions despite the impressions sometimes given. The good news is that they all give very similar answers....

$$\frac{1}{3} \frac{\partial \ln f_0}{\partial \ln p} \left(1 - \frac{1}{r_{\text{tot}}} \right) \frac{U(x) \, dx}{\kappa(x, p)}$$

Remarkably, the crudest *Ansatz*, which simply assumes the accelerated particles penetrate a fixed distance upstream and then abruptly stop, appears to work quite well and gives results very similar to the more complicated ones. This approximation, originally due to Eichler, is

 $f(x,p) = \begin{cases} f_0(x) \\ 0 \\ 0 \end{cases}$

It leads to equations which can be heuristically derived in a nonlinear box model and which have been used by a number of authors, most recently P. Blasi and co-workers (their method A).

$$(p), \quad x > -L(p)$$

$$D, \quad x < -L(p)$$



and particle number conservation reads..





 $\Phi(p) = \int \frac{4\pi p^3}{3} f(x,p) \frac{du}{dx} dx$ $= \frac{4\pi p^3}{3} f_0(U_p - U_2)$

 $3U_2$ Φ $U_p - U_2 p$



Ignoring for the moment the gas pressure momentum balance gives

$$= \frac{4\pi}{3}p^{3}vf_{0}(p)dp$$
$$= \frac{\Phi}{U_{p}-U_{2}}vdp$$

- So in this simple case get a non-linear box model described by two coupled ODEs.
- In general coupled integro-differential equations.

written

Thus if losses can be neglected and the acceleration flux is a constant

 $U_2 \approx 0, \quad U_p \approx \sqrt{}$

which is just Malkov's "universal" spectrum

Remarkably, if we ignore gas pressure and switch to particle kinetic energy, rather than momentum, as independent variable, the last equation can be

 $\frac{\partial}{\partial T} \left(U_p - U_2 \right)^2 = \frac{2\Phi}{A}$

$$\frac{\sqrt{2\Phi T}}{A}, \quad f_0 \propto p^{-3}T^{-1/2}$$

Can be thought of as the asymptotic attractor for all nonlinearly modified solutions at high energies.

Power-law spectrum hardens to 3.5

No particle escape!

Precursor velocity profile is linear.

Corresponds to accelerator going flat-out, all energy goes into flux of particles upwards in energy space...

Reality lies in between. If the shock modifies itself to the point that the injection of ions is reduced to the level required, then the subshock has to be weakened, but still exist. Because the pressure per logarithmic momentum interval is



in the asymptotic limit of a very low injection energy, the subshock has to have a compression ratio of at least 2.5, corresponding to a local spectral index of 5,

- $\frac{3 \times 2.5}{=5}$
- 2.5 1

If the pressure is not to fall away too rapidly.



From P. Blasi, 2002

Has important consequences for the post-shock gas temperature. If indeed the shock is self-regulated by the need to reduce the sub-shock compression to a value of order 2.5, then the post-shock gas temperature is fixed not so much by the shock speed as by the upstream temperature.

compression in the precursor followed by shock is, say, 10 with 4 in the precursor and 2.5 in the of $4^{\gamma-1}$ in the precursor and a further factor of 12/5 in the subshock - in total a modest factor 6.

The postshock temperature is a result of adiabatic heating in the subshock, and if the total compression subshock, then the gas temperature rises by a factor

Consensus view...

- before cutting off.
- extreme
- ratio of about 2.5.

• Spectra are generically curved, softer at low energies, hardening in the relativistic region

• Hardening at high energies at most changes spectral index from 4 to 3.5, so not too

 Subshock is reduced to point where injection matches capacity of shock to accelerate; suggests minimum subshock compression

- All approaches assume steady structure on the mesoscopic scale.
- In fact exist many possible instabilities.
- However can hope that theory still applies in mean sense - basic physics is very robust.
- Also not all bad news offers exciting prospect of amplified B fields and thereby reaching higher energies.

But...

The Instability Zoo

- Streaming excitation of Alfven waves (eg Wentzel, 1974; Skilling 1975)
- Acoustic instability (Drury and Falle, 1986)
- Parker instability (1966, 1967)
- McKenzie and Voelk, 1981 wave heating or "plastic deformation of field".
- Bell and Lucek, 2000, 2001; Bell 2004, 2005
- Generic Weibel-type instabilities
- Jokipii downstream vorticity

- Streaming excitation of Alfven waves
 - Originally proposed to give enhanced scattering at the shock (Bell 1978)
 - resonant v non-resonant terms (Achterberg, 1983; Bell, 2004; Reville 2006)
 - physical ordering of terms inappropriate for shock precursor case as noted by Bell.

Acoustic instability

- Exists in purely I-D models (and thus important for numerical codes).

• Depends on collective nature of scattering



- For small scale perturbations in I-D
 - $\kappa \nabla P_C \approx const$
- (drive constant flux through structures)
- Associated acceleration fluctuations are
 - $\frac{d^2x}{dt^2} \propto \frac{\nabla P_C}{\rho} \propto \frac{1}{\kappa\rho}$
- Unless the diffusion is exactly inversely proportional to the density (two body scattering case!) density fluctuations induce velocity fluctuation which rapidly amplify the initial perturbation. Mathematically appears as a mechanism driving sound waves unstable.



But in some sense not very physical as clearly relies strongly on the I-D nature of the initial perturbation. Consider more realistic 2-D and 3-D fluctuations in a shock precursor.

Effective gravitational field

Parker Instability!

- Original Parker instability
 - cosmic ray sources in disc
 - gravitational field of Galaxy
 - buoyant flux tubes inflate with cosmic rays and rise up

- Exactly the same pl shock precursor
- deceleration provides an effective gravitational field towards the shock
- strong cosmic ray gradient away from shock
- magnetic field loops linked to the shock should inflate and "rise up".

• Exactly the same physics should occur in a

Only way to avoid this effect would be to completely decouple diffusion from the density (and magnetic field!) distribution.

 $\frac{\partial \kappa}{\partial \rho} = 0$

Thus it is impossible for the cosmic-ray pressure gradient to uniformly decelerate density fluctuations in the inflowing plasma and at the same time avoid inducing transverse velocity perturbations.

Bell's non-resonant instability

- Energetic cosmic rays penetrate upstream ignoring small-scale field structure unmagnetised on these scales.
- Return current of low-energy particles is forced through magnetised plasma
- Field lines coil up and attraction of parallel currents amplifies disturbance.

- MHD is theory of strongly magnetised plasmas.
- Usually rewrite Lorentz force on plasma to eliminate currents using induction law.
- Need to modify this for case considered.

- $\nabla \wedge B = j_{CR} + j_{th}$ $j_{th} = \nabla \wedge B - j_{CR}$
 - $F = j_{th} \wedge B$
 - $= (\nabla \wedge B) \wedge B j_{CR} \wedge B$

• If CR are strongly scattered then the to an additional cosmic ray pressure,

instability.

additional force term can be shown to reduce

 $\langle j_{CR} \wedge B \rangle \approx \nabla P_{CR}$

• But on scales where the CR are not scattered appears as a current driven magnetic field



Figure 4. The paths of four magnetic field lines in (x,y,z) at t = 6.

(from Bell 2005, MNRAS 358 181)



Figure 11. Slices in the xy plane (Top) and xz plane (Bottom) of magnetic field strength B for the marked geometries and times. The four left-hand panels show the structure of the turbulence at early non-linear times; the plasma consists of tori with scale $R(t) \sim \lambda e^{\gamma t}$ in the xy plane and width $\sim \lambda$ in the z direction. At late times, shown in the four right-hand panels, the turbulence has mostly lost its preferred orientation and the typical scale-lengths in each direction are similar.

MNRAS 000, 1–13 (2015)

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Amplification of perpendicular and parallel magnetic fields by cosmic ray currents

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Good account and confirmation of Bell's magnetic field amplification process in arXiv0801.4486 by Zirakashvili, Ptuskin and Völk.



Instability driven by the cosmic ray diffusion current causes spirals of magnetic field to expand and interact.

Turbulence and multiple local MHD shocks in precursor!

Field saturates at about

- Shock precursors are almost certainly highly "turbulent" - not clear what implications if any this has for the modification theories.
- Easy to amplify small-scale magnetic field by stretching and twisting.
- Field can plausibly be increased by orders of magnitude, if not to equipartition (Bell predicts saturation a factor U/c below).

Summary

- scaling according to JVink).
- Allows acceleration of protons to "knee (but scale issue?).

 Strong observational indications of amplified fields in young SNRs (with possible U^3

region" with ease - otherwise a bit difficult

• NB - upstream amplification is needed to reach higher energies, but the observational evidence is only for downstream fields!

A new twist

- Suggestions that magnetic effects may soften spectra!
- Bell and co-workers energy given upstream to field must come at expense of particle acceleration?
- Caprioli downstream decay of amplified field?

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Cosmic ray acceleration by shocks: spectral steepening due to turbulent magnetic field amplification

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ABSTRACT

We show that the energy required to turbulently amplify magnetic field during cosmic ray (CR) acceleration by shocks extracts energy from the CR and steepens the CR energy spectrum.





The Issue with Diffusive Shock Acceleration

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We discuss the recent developments in the theory of diffusive shock acceleration (DSA) by using both first-principle kinetic plasma simulations and analytical theory based on the solution of the convection/diffusion equation. In particular, we show how simulations reveal that the spectra of accelerated particles are significantly steeper than the E^{-2} predicted by the standard theory of DSA for strong shocks, in agreement with several observational pieces of evidence. We single out which standard assumptions of test-particle and non-linear DSA are violated in the presence of strong (self-generated) magnetic turbulence and put forward a novel theory in better agreement with the particle spectra inferred with multi-wavelength observations of young SN remnants, radio-SNe, and Galactic cosmic rays.

2019 Sep \mathcal{O} $\overline{}$ [astro-ph.HE] arXiv:1909.06288v1

Relativistic shocks

See arXiv:0807.3459 by Pelletier, Lemoine and Marcowith for a good account.

- In principle the same basic acceleration work.
- well as at least one serious problem.

process, multiple shock crossings with magnetostatic scattering on either side, should

• But there are a number of major differences as

- Distributions are highly anistropic at certainly not diffusive!
- while upstream.

relativistic shocks, and the energy changes are not small - relativistic shock acceleration is

• Relativistic shocks with magnetic fields are generically superluminal - not clear that particles can in fact recross the shock if they are at all magnetised, or that they have time to be scattered in angle before being overtaken

- moves faster (super-luminal shocks).
- In sub-luminal case can boost into de rest.

• If large scale regular field with well defined field lines, can divide shocks into those where the point of intersection between shock front and field line moves at less than the speed of light (sub-luminal shocks) and those where it

Hoffman-Teller frame where this point is at

• In super-luminal case can boost to infinite velocity - ie field is strictly perpendicular



Sub-luminal case $U \parallel B$

Super-luminal case $U \perp B$

- random field).
- speed non-relativistic shocks (Jokipii).
- magnetised relativistic shocks though.

• If particles are tied to field lines clear that superluminal shocks are not good sites for Fermi acceleration - requires fast cross-field diffusion and strong turbulence (or very

• NB cross-field diffusion at perpendicular shocks can give Fermi acceleration at low

Hard to see how this could work for strongly

- formed.
- Fermi acceleration in relativistic PIC simulations.

• However, if one ignores these issues and just assumes that a Fermi type acceleration occurs, then general agreement that a universal spectrum with exponent about 4.2 to 4.3 is

• Recent development is very promising work by Anatoly Spitkovsky on pure electron positron shocks with self-generated Weibel fields where he see first direct evidence for

- dominate).
- as well as pulsar wind nebulae.

 Suggests that the solution to relativistic shock acceleration is that you need unmagnetised upstream media (or at least ones where the field is weak enough that the Weibel fields can

• However some form of relativistic shock acceleration is clearly needed for GRB models

Magnetic reconnection

- Relatively rapid change in the topology of the magnetic field leading to release of energy stored in the field.
- Definitely occurs seen in the Earth's magnetosphere, the Sun and in laboratory plasmas.
- Not easy to model no simple geometry or scaling relations and expensive to simulate on computers.

- acceleration!

• In the reconnection region can have significant electric fields and weak magnetic fields with obvious potential for particle acceleration.

 However much of the acceleration observed in simulations appears to come from plasma compression resulting from the removal of magnetic pressure and is thus back to Fermi

- spectra ($E^{-2.5}$) but these are wrong.

Can find in the literature claims of universal

• What is true is that reconnection can produce quite hard spectra, but maximum energy is typically less than for shock acceleration reflecting small size of the reconnection sites.

 Compression in reconnection depends on how much of the released magnetic energy goes into heating and how much into kinetic energy of the outflow, but can be very large.

Mon. Not. R. Astron. Soc. 422, 2474–2476 (2012)

First-order *Fermi* acceleration driven by magnetic reconnection

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For a recent review see Che and Zank, arXiv:1908.09155

A Brief Review on Particle Acceleration in Multi-island Magnetic Reconnection

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Guo et al also argue for compression....

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Determining the Dominant Acceleration Mechanism during Relativistic Magnetic **Reconnection in Large-scale Systems**

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While a growing body of research indicates that relativistic magnetic reconnection is a prodigious source of particle acceleration in high-energy astrophysical systems, the dominant acceleration mechanism remains controversial. Using a combination of fully kinetic simulations and theoretical analysis, we demonstrate that Fermi-type acceleration within the large-scale motional electric fields dominates over direct acceleration from non-ideal electric fields within small-scale diffusion regions. This result has profound implications for modeling particle acceleration in large-scale astrophysical problems, as it opens up the possibility of modeling the energetic spectra without resolving microscopic diffusion regions.

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Abstract





- Definitely can produce very strong electric fields across "gaps", but only in very small regions.
- Pulsar magnetosphere and wind not really understood, but clear evidence for electron and positron acceleration.
- Crab flares a total mystery! Fast reconnection?
- Probably source of CR electrons, but hard to see how they could accelerate ions with observed composition.

Pulsars?

Conclusions

- Fermi type processes made first order by compression seem to be the dominant acceleration mechanisms in most systems.
- Still mysteries though in particular reconnection and relativistic shocks are not well understood.
- Computer simulations are now powerful enough to study some of these issues, but are expensive and need to be treated with caution.